

Results from tests of stellar physics uncertainties

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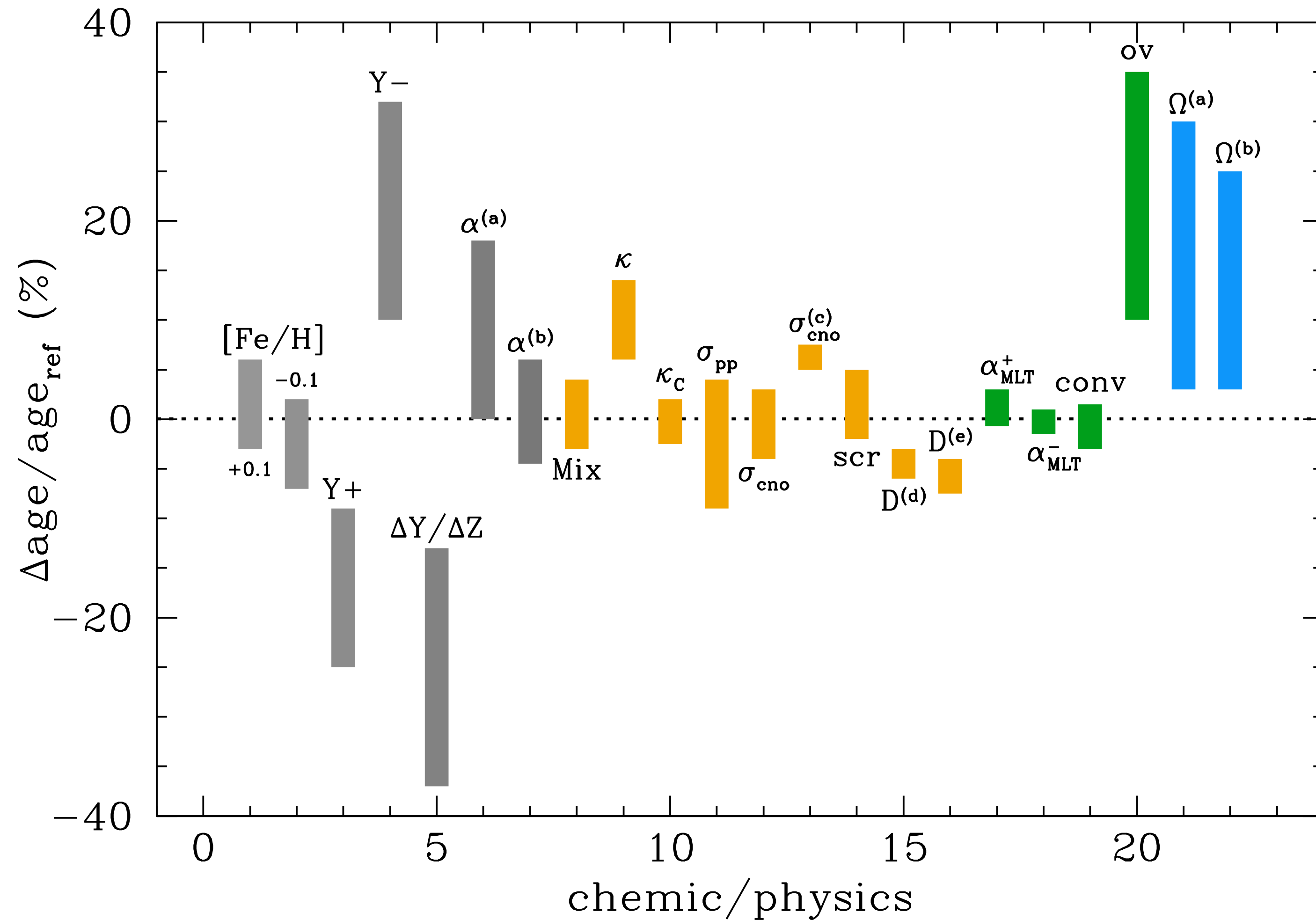
UNIVERSITY OF
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SCHOOL OF
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ASTRONOMY

Ingredients for a stellar model

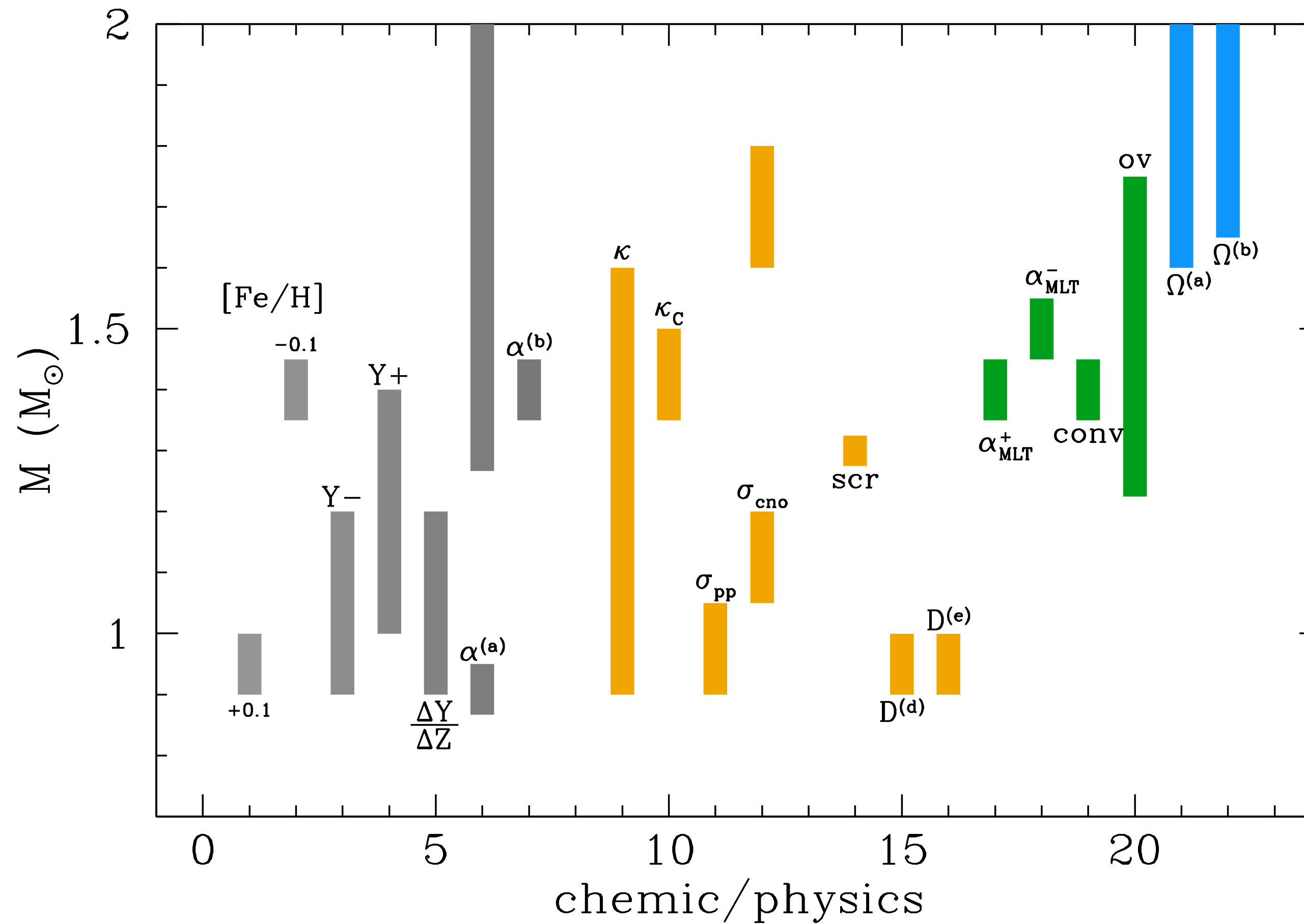
- Opacity tables (interior and low temperature) OPAL, OP, OPAS, OPLIB
 - Chemical composition : [Fe/H], Y, and [X/H] AGSS09, GN93, GS98, CLSFB11...
 - Equation of State OPAL, SAHA-S, freeEOS.
 - Nuclear reaction rates NACRE, NACREII, Solar FusionII
 - Surface boundary conditions: Atm. Models 1D , 3D, grey/non-grey, Eddington , KS, Val-C..
 - Treatment of superadiabatic convection MLT/FST, 3D simulations
 - Boundaries of convective regions Overshooting instantaneous, diffusive one...
 - Microscopic diffusion and radiative acceleration Microscopic diffusion and radiative acceleration
-
- Transport of angular momentum and chemicals induced by stellar rotation.
 - Magnetic fields.
 - Tidal effects in binaries.
-

Effect on TO age of uncertainties in micro/macro physical inputs in stellar models



- Y : +/- 0.03 respect to solar
- $\Delta Y/\Delta Z$: +3 respect to solar
- α -elements enhancement of +0.4 dex at $[\text{Fe}/\text{H}]=0.0$ (a) and -1.0 dex (b)
- κ : +10%
- κ_c : Iben 75 vs. Cassisi et al. 07
- OV: α_{ov} : 0 vs. 0.2
- Rotation: 50 km/s at $[\text{Fe}/\text{H}]=0$ (Ω_a); $[\text{Fe}/\text{H}]=-1.0$ (Ω_b)

Mass domain affected by those uncertainties



INPUT PHYSICS TEST

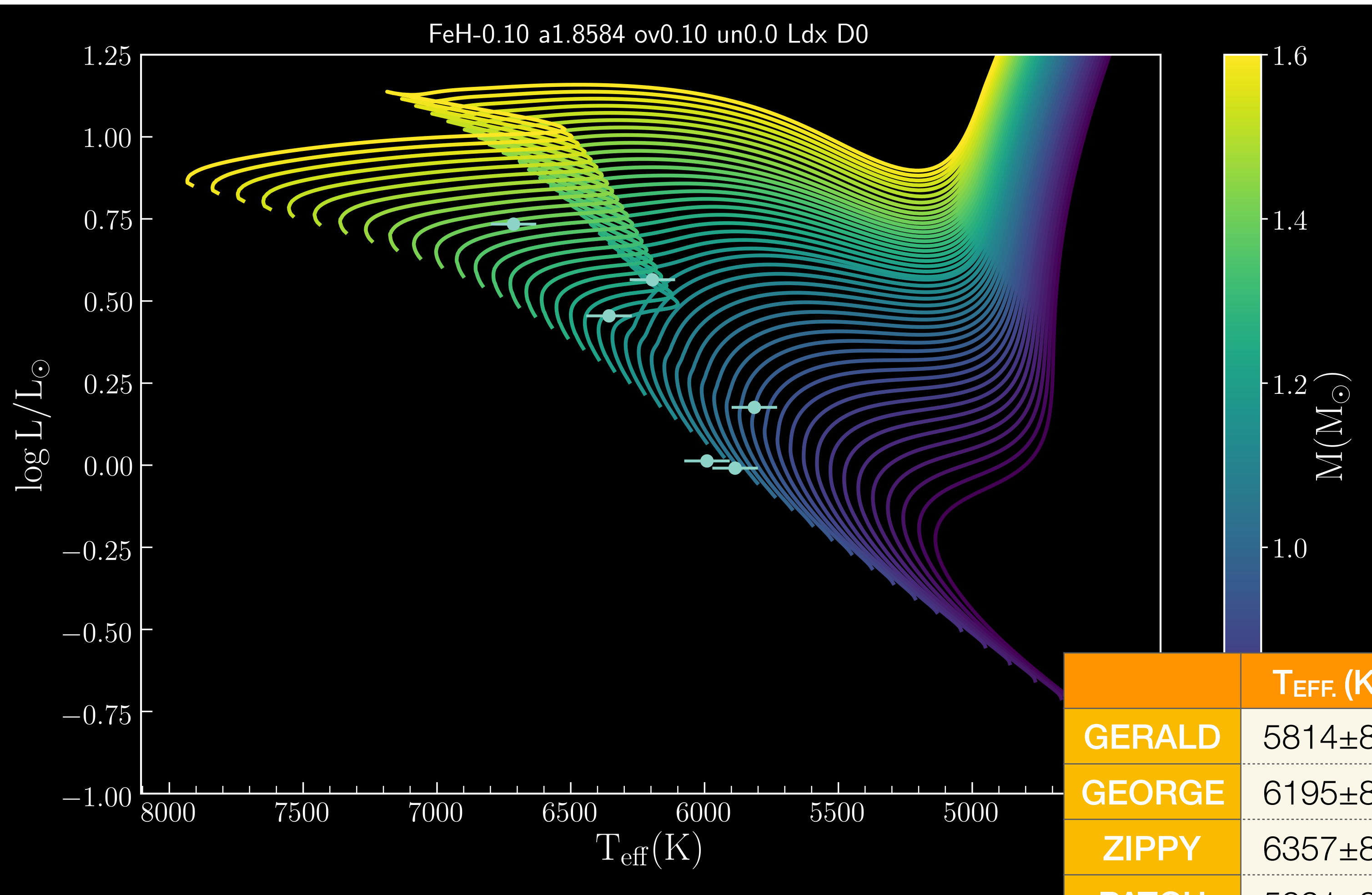
- Opacity tables (interior and low temperature) OPAL/OP
 - Chemical composition : [Fe/H], Y, and [X/H] AGSS09/GN93
 - Equation of State
 - Nuclear reaction rates $^{14}\text{N}, p$ and pp
 - Surface boundary conditions: Atm. Models
 - Treatment of superadiabatic convection
 - Boundaries of convective regions Overshooting & semiconvection
 - Microscopic diffusion and radiative acceleration MP93 / Burgers Eq.
 - Transport of angular momentum and chemicals induced by stellar rotation.
 - Magnetic fields.
 - Tidal effects in binaries.
-

TARGETS

6 Synthetic Main Sequence Stars used by WP124 in H&H and by WP121

- v_{\max} and Δv
- T_{eff} [Fe/H]
- Luminosity
- ~ 30 individual frequencies with angular degree : 0, 1 and 2

In each test L, Teff, [Fe/H] and individual frequencies are used as observational constraints, and the corresponding grid of stellar uses solar calibrated convection parameter for the corresponding physics



| | $T_{\text{EFF.}}$ (K) | Lum/ L_{\odot} | [Fe/H] | v_{\max} (μHz) | Δv (μHz) | N modes |
|----------------|-----------------------|------------------|------------------|-------------------------------|-------------------------------|---------|
| GERALD | 5814 ± 85 | 1.50 ± 0.05 | 0.03 ± 0.09 | 2207 ± 108 | 106.3 ± 2.1 | 28 |
| GEORGE | 6195 ± 85 | 3.67 ± 0.11 | 0.35 ± 0.09 | 1284 ± 68 | 68.8 ± 1.4 | 35 |
| ZIPPY | 6357 ± 85 | 2.85 ± 0.09 | -0.17 ± 0.09 | 1660 ± 85 | 86.4 ± 1.7 | 33 |
| PATCH | 5991 ± 85 | 1.03 ± 0.03 | -0.28 ± 0.09 | 2906 ± 143 | 132.9 ± 2.7 | 25 |
| ZEBEDEE | 5886 ± 85 | 0.98 ± 0.03 | 0.10 ± 0.09 | 3254 ± 167 | 136.5 ± 2.8 | 23 |
| FRED | 6714 ± 85 | 5.42 ± 0.16 | -0.04 ± 0.09 | 1393 ± 69 | 67.0 ± 1.4 | 32 |

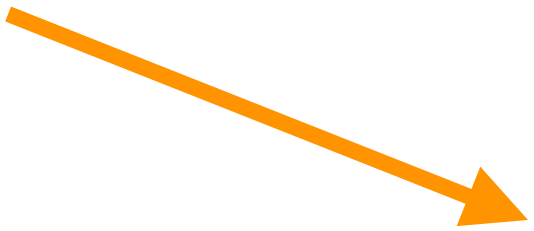
CHARACTERIZATION OF TARGETS

- Stellar evolution CODE : [GARSTEC](#) (Weiss & Schlattl, 2008)
- Nuclear reaction rates : [Solar Fusion](#) (Aldelberger et al 2011)
- [FreeEOS](#) (Cassisi et al 2003)
- Convection: [MLT](#)
- Solar mixture : [GN93](#) ($Z/H=0.0245$), (Grevesse & Noels 1993)
- Undershooting (Formalism Vandenberg et al.2012)
- Diffusive Overshooting ($f=0.02 \sim 0.25H_p$)
- Microscopic diffusion (Thoul et al.1994) + attenuation between 1.25-1.35 Msun
- $T(\tau)$: [Eddington](#) relation

- Adiabatic oscillation code [ADIPLS](#) (Christensen-Dalsgaard 2008)
- Optimization/Inference : [AIMS](#) (Lund & Reese 2018, Rendle et al 2019) with [Ball & Gizon \(2014\)](#) for surface effects correction
- Constraints : L , T_{eff} , $[Fe/H]$ and individual frees

Grid of stellar models :

M in $[0.7, 1.6] M_{\text{sun}}$ $\Delta M = 0.01 M_{\text{sun}}$
 $[Fe/H]$ in $[-0.95, +0.6]$, $\Delta([Fe/H]) = 0.05 \text{dex}$

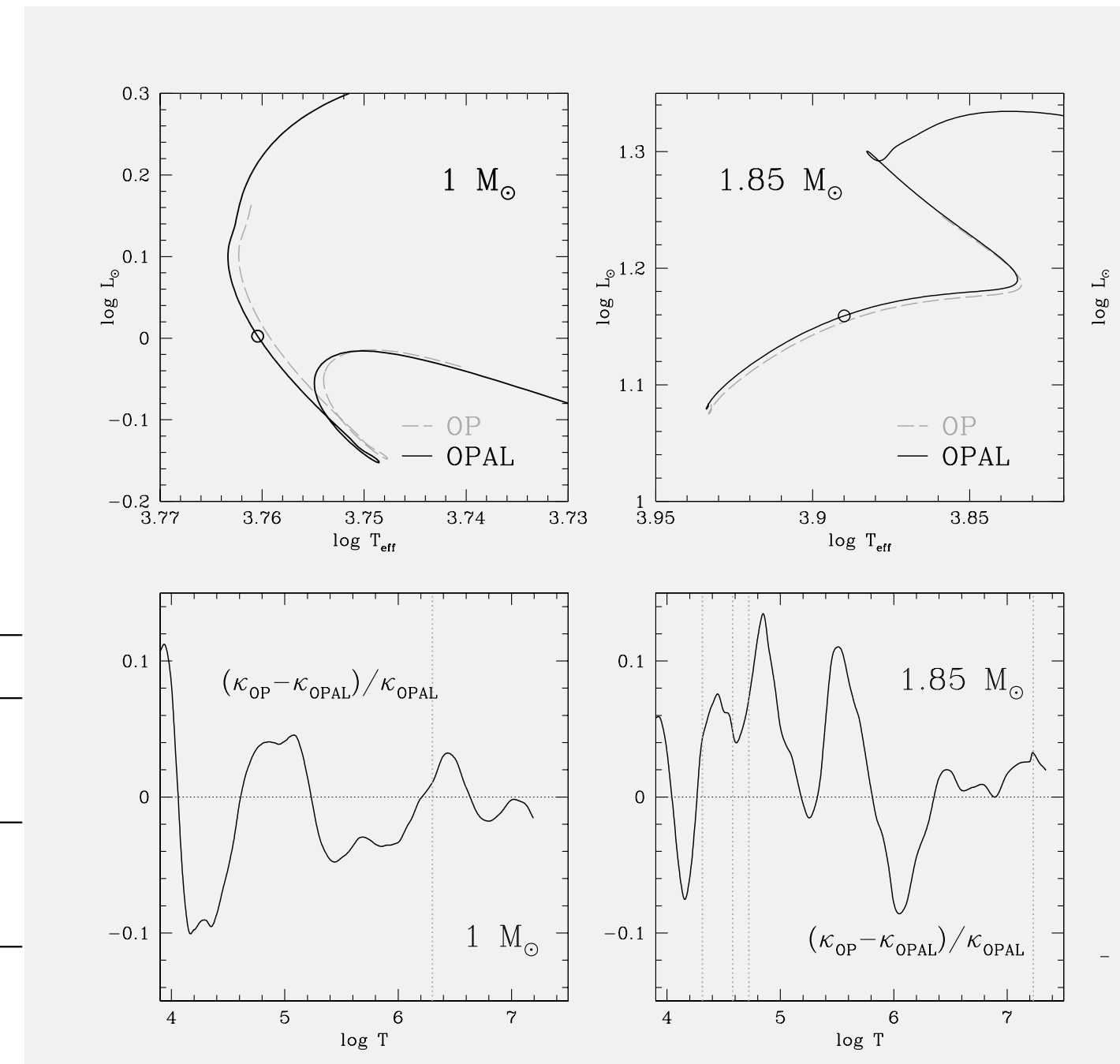
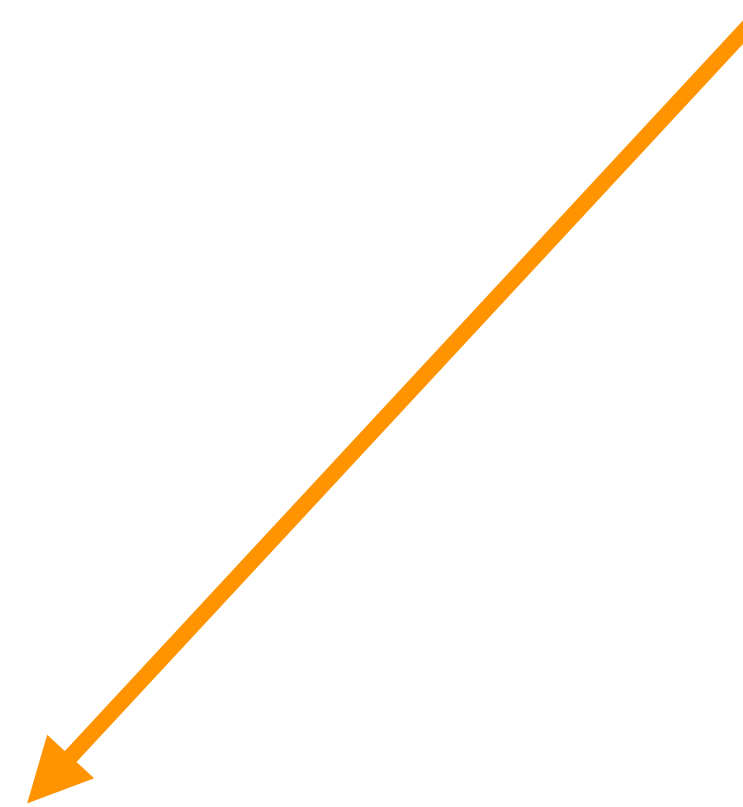


| ID | Mass (M_{\odot}) | Radius (R_{\odot}) | Age (Gyr) | $\log g$ | ρ (g.cm^{-3}) | Z_{ini} | $[Fe/H]$ |
|---------|----------------------|------------------------|-----------------|-----------------|-------------------------------|-------------------|-------------------|
| Fred | 1.41 ± 0.05 | 1.715 ± 0.027 | 1.85 ± 0.20 | 4.12 ± 0.01 | 0.396 ± 0.003 | 0.016 ± 0.005 | -0.039 ± 0.12 |
| Georges | 1.38 ± 0.01 | 1.737 ± 0.001 | 3.11 ± 0.03 | 4.10 ± 0.01 | 0.307 ± 0.001 | 0.032 ± 0.001 | 0.28 ± 0.01 |
| Gerald | 1.00 ± 0.02 | 1.119 ± 0.005 | 8.41 ± 0.30 | 4.28 ± 0.01 | 0.828 ± 0.002 | 0.019 ± 0.002 | -0.04 ± 0.05 |
| Patch | 0.89 ± 0.01 | 0.966 ± 0.002 | 7.54 ± 0.10 | 4.42 ± 0.01 | 1.397 ± 0.003 | 0.009 ± 0.003 | -0.37 ± 0.01 |
| Zebedee | 1.02 ± 0.01 | 0.966 ± 0.002 | 2.34 ± 0.15 | 4.48 ± 0.01 | 1.596 ± 0.002 | 0.019 ± 0.001 | 0.02 ± 0.01 |
| Zippy | 1.16 ± 0.03 | 1.409 ± 0.015 | 3.76 ± 0.30 | 4.21 ± 0.01 | 0.589 ± 0.004 | 0.014 ± 0.003 | -0.19 ± 0.08 |

OPACITY TABLES

- Stellar evolution CODE : [CESTAM](#) (Morel & Lebreton , 2008, Marques et al .2013)
- Nuclear reaction rates : [NACRE](#) (Angulo 1999)
- [OPAL2005 EoS](#)
- Convection: [FST](#) (Canuto et al 1996)
- Solar mixture : [AGSS09](#) (Z/H=0.0181), + Serenelli (2010)
- Adiabatic oscillation code [ADIPLS](#) (Christensen-Dalsgaard 2008)
- Optimization/Inference : [AIMS](#) (Lund & Reese 2018, Rendle et al 2019) with [Ball & Gizon \(2014\)](#) for surface effects correction

OPAL versus **OP**
 (Rogers & Nayfonov 2002) (Seaton 2005)



| ID | Opacities | Mass (M_{\odot}) | Radius (R_{\odot}) | Age (Gyr) | $\log g$ | ρ (g.cm^{-3}) | Z_{ini} | [Fe/H] |
|---------|-----------|----------------------|------------------------|-----------------|-----------------|-------------------------------|---------------------|--------------------|
| Gerald | OPAL | 1.02 ± 0.01 | 1.202 ± 0.005 | 9.62 ± 0.45 | 4.29 ± 0.0 | 0.828 ± 0.003 | 0.0124 ± 0.0013 | -0.044 ± 0.046 |
| | OP | 1.02 ± 0.01 | 1.201 ± 0.004 | 9.61 ± 0.42 | 4.29 ± 0.0 | 0.829 ± 0.002 | 0.0122 ± 0.0012 | -0.052 ± 0.044 |
| Patch | OPAL | 0.82 ± 0.02 | 0.935 ± 0.007 | 9.67 ± 0.46 | 4.41 ± 0.0 | 1.404 ± 0.006 | 0.0055 ± 0.0008 | -0.37 ± 0.062 |
| | OP | 0.82 ± 0.02 | 0.939 ± 0.006 | 9.81 ± 0.48 | 4.41 ± 0.0 | 1.4 ± 0.006 | 0.0056 ± 0.0009 | -0.366 ± 0.067 |
| Zebedee | OPAL | 0.98 ± 0.01 | 0.951 ± 0.002 | 2.5 ± 0.17 | 4.47 ± 0.0 | 1.601 ± 0.006 | 0.0129 ± 0.0002 | 0.005 ± 0.007 |
| | OP | 0.98 ± 0.01 | 0.951 ± 0.002 | 2.53 ± 0.17 | 4.47 ± 0.0 | 1.601 ± 0.006 | 0.0129 ± 0.0002 | 0.005 ± 0.008 |
| Zippy | OPAL | 1.24 ± 0.0 | 1.425 ± 0.0 | 3.82 ± 0.0 | 4.22 ± 0.0 | 0.601 ± 0.0 | 0.0114 ± 0.0 | -0.085 ± 0.001 |
| | OP | 1.24 ± 0.0 | 1.424 ± 0.0 | 3.83 ± 0.0 | 4.22 ± 0.0 | 0.603 ± 0.0 | 0.0114 ± 0.0 | -0.085 ± 0.0 |
| Fred | OPAL | 1.38 ± 0.04 | 1.687 ± 0.023 | 1.74 ± 0.13 | 4.12 ± 0.01 | 0.405 ± 0.011 | 0.0129 ± 0.0011 | 0.005 ± 0.043 |
| | OP | 1.43 ± 0.06 | 1.71 ± 0.033 | 1.81 ± 0.16 | 4.13 ± 0.01 | 0.403 ± 0.01 | 0.013 ± 0.0023 | -0.007 ± 0.085 |

$\Delta M = 0.025 M_{\odot}$,
 From ZAMS to $X_c = 0.05$,

ATOMIC DIFFUSION

- Stellar evolution CODE : [CESTAM](#) (Morel & Lebreton , 2008, Marques et al .2013)
- Nuclear reaction rates : [NACRE](#) (Angulo 1999)
- [OPAL2005 EoS](#) + OPAL opacities (Rogers & Nayfonov 2002)
- Convection: [FST](#) (Canuto et al 1996)
- Solar mixture : [AGSS09](#) (Z/H=0.0181), + Serenelli (2010)
- Adiabatic oscillation code [ADIPLS](#) (Christensen-Dalsgaard 2008)
- Optimization/Inference : [AIMS](#) (Lund & Reese 2018, Rendle et al 2019) with [Ball & Gizon \(2014\)](#) for surface effects correction

MP93 versus **Burgers eqs.**
 (Michaud & Proffitt 1993) (Burgers 1969)

Initial Helium:

Gerald: 0.222 Burgers, 0.223 MP3

Patch: 0.279 Burgers, 0.281 MP93

Zippy: 0.275 Burgers, 0.281 MP93

Zebedee: 0.281 Burgers, 0.282 MP93

| ID | Opacities | Mass (M_{\odot}) | Radius (R_{\odot}) | Age (Gyr) | $\log g$ | ρ (g.cm^{-3}) | Z_{ini} | [Fe/H] |
|---------|-----------|----------------------|------------------------|-----------------|-----------------|-------------------------------|---------------------|--------------------|
| Gerald | MP93 | 1.06 ± 0.01 | 1.22 ± 0.004 | 8.59 ± 0.4 | 4.29 ± 0.0 | 0.826 ± 0.002 | 0.0151 ± 0.0011 | -0.078 ± 0.033 |
| | Burgers | 1.07 ± 0.01 | 1.222 ± 0.004 | 8.63 ± 0.44 | 4.29 ± 0.0 | 0.825 ± 0.002 | 0.0155 ± 0.001 | -0.065 ± 0.029 |
| Patch | MP93 | 0.85 ± 0.02 | 0.949 ± 0.008 | 7.96 ± 0.42 | 4.41 ± 0.0 | 1.399 ± 0.005 | 0.0072 ± 0.0009 | -0.386 ± 0.057 |
| | Burgers | 0.85 ± 0.02 | 0.951 ± 0.008 | 7.99 ± 0.38 | 4.41 ± 0.0 | 1.397 ± 0.004 | 0.0071 ± 0.0008 | -0.386 ± 0.05 |
| Zebedee | MP93 | 0.98 ± 0.01 | 0.954 ± 0.005 | 2.75 ± 0.22 | 4.47 ± 0.0 | 1.599 ± 0.005 | 0.0142 ± 0.0005 | -0.001 ± 0.017 |
| | Burgers | 0.99 ± 0.01 | 0.954 ± 0.004 | 2.72 ± 0.22 | 4.47 ± 0.0 | 1.6 ± 0.005 | 0.0142 ± 0.0005 | 0.002 ± 0.017 |
| Zippy | MP93 | 1.15 ± 0.04 | 1.402 ± 0.019 | 3.6 ± 0.31 | 4.21 ± 0.01 | 0.588 ± 0.006 | 0.0122 ± 0.0025 | -0.231 ± 0.135 |
| | Burgers | 1.19 ± 0.02 | 1.417 ± 0.01 | 3.52 ± 0.22 | 4.21 ± 0.0 | 0.586 ± 0.004 | 0.0141 ± 0.0014 | -0.15 ± 0.077 |

SOLAR MIXTURE

- Stellar evolution CODE : [MESA](#) (Paxton et al, 2011,13,15,18,19)
- Nuclear reaction rates : [NACRE](#) (Angulo 1999)
- [OPAL](#) opacities (Rogers & Nayfonov 2002)
- Convection: [MLT](#)
- Core-convective [overshoot](#) ($f_H=0.01$) and envelope [unders.](#) ($f_{und}=0.001$)
- $T(\tau)$: [Eddington](#) relation
- Adiabatic oscillation code: [GYRE](#) (Townsend & Taler 2013)
- Optimization/Inference : [AIMS](#) (Lund & Reese 2018, Rendle et al 2019) with [Ball & Gizon](#) (2014) for surface effects correction

GN93

(Grevesse & Noels 1993)

$Z/X_{\odot}=0.0245$

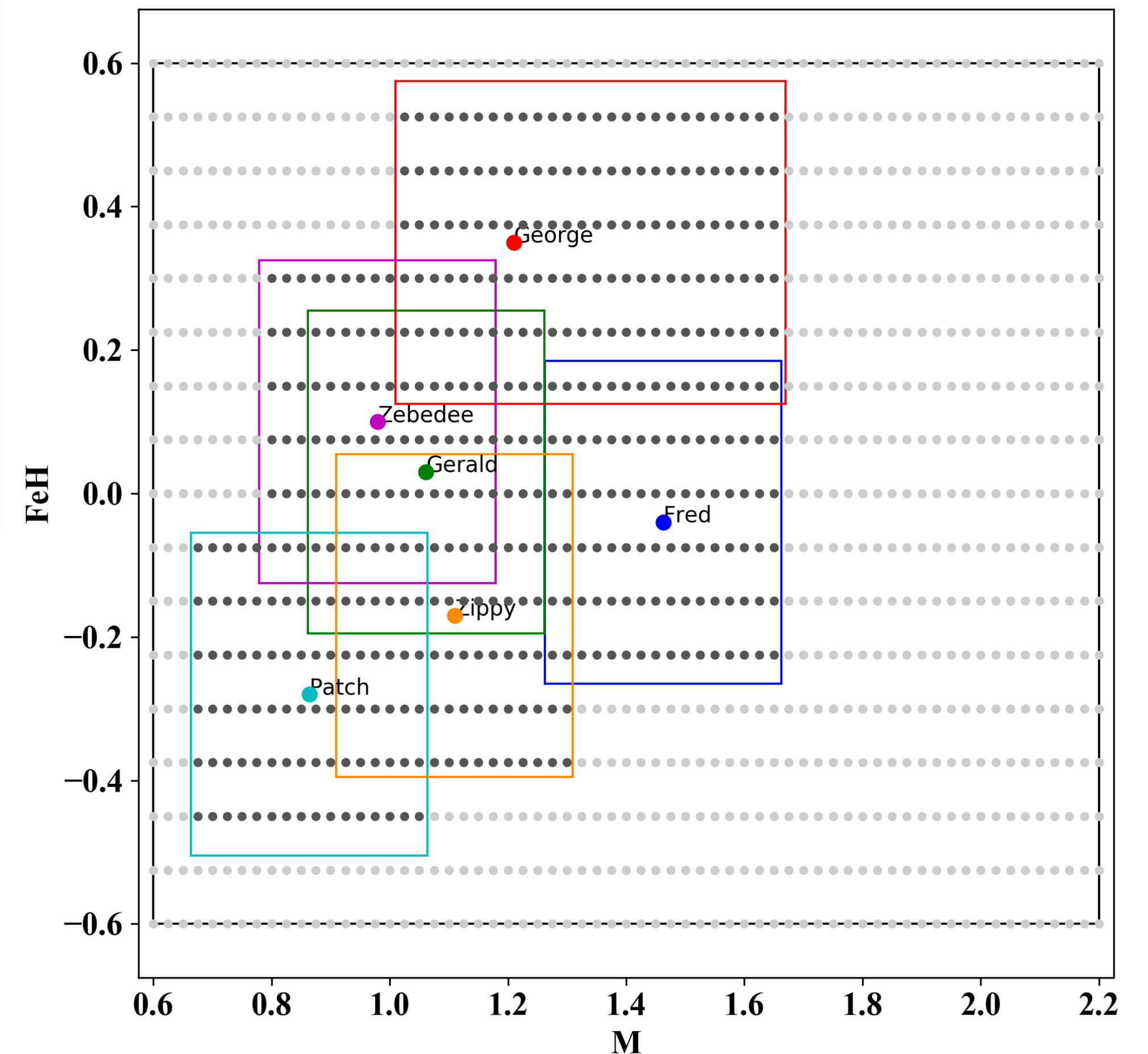
versus

AS09

(Asplund et al. 2009)

$Z/X_{\odot}=0.0178$

From ZAMS to $\Delta\nu=50\mu\text{Hz}$,
 $\Delta M=0.025M_{\odot}$,



SOLAR MIXTURE

GN93
(Grevesse & Noels 1993)
 $Z/X_{\odot}=0.0245$

versus

AS09
(Asplund et al. 2009)
 $Z/X_{\odot}=0.0178$

Effect on MASS ~ 2-3%

| Star | solar mixture | Mass (M_{\odot}) | Radius (R_{\odot}) | Age (Myr) | Z | Y | [Fe/H] |
|---------|---------------|------------------------------|------------------------------|-----------------------------------|------------------------------|------------------------------|-------------------------------|
| Fred | AS09 | 1.4520112 ± 0.0313322 | 1.7368232 ± 0.0131829 | 1734.3556567 ± 102.9618230 | 0.0162393 ± 0.0013886 | 0.2691657 ± 0.0087745 | -0.0070742 ± 0.0395177 |
| | GN93 | 1.4107382 ± 0.0299732 | 1.7205811 ± 0.0135264 | 1761.4803993 ± 131.8551179 | 0.0165016 ± 0.0023768 | 0.2733705 ± 0.0083805 | -0.0002677 ± 0.0674557 |
| George | AS09 | 1.5080332 ± 0.0170804 | 1.7844191 ± 0.0064186 | 2549.6326232 ± 73.3457807 | 0.0378276 ± 0.0016073 | 0.2712146 ± 0.0047804 | 0.3760763 ± 0.0199648 |
| | GN93 | 1.4310626 ± 0.0180073 | 1.7565156 ± 0.0071807 | 2441.1683126 ± 71.9964592 | 0.0441737 ± 0.0019816 | 0.3045219 ± 0.0087744 | 0.4690995 ± 0.0233207 |
| Gerald | AS09 | 0.9978135 ± 0.0173275 | 1.1927779 ± 0.0067718 | 7754.1934137 ± 492.7894911 | 0.0169618 ± 0.0013688 | 0.2901987 ± 0.0074182 | 0.0255513 ± 0.0379937 |
| | GN93 | 1.0111999 ± 0.0130081 | 1.1995666 ± 0.0049810 | 8206.0673394 ± 445.9463890 | 0.0200796 ± 0.0014249 | 0.2747576 ± 0.0057391 | 0.0915194 ± 0.0332891 |
| Zebedee | AS09 | 0.9913308 ± 0.0113865 | 0.9559299 ± 0.0036741 | 2187.9353606 ± 349.2418451 | 0.0149003 ± 0.0010425 | 0.2889081 ± 0.0047937 | -0.0324369 ± 0.0319693 |
| | GN93 | 0.9991787 ± 0.0156676 | 0.9591417 ± 0.0051438 | 2385.8829856 ± 422.0671433 | 0.0179562 ± 0.0019757 | 0.2819127 ± 0.0119327 | 0.0447010 ± 0.0527891 |
| Patch | AS09 | 0.8949380 ± 0.0137749 | 0.9663672 ± 0.0051295 | 7994.8342642 ± 472.2130038 | 0.0077414 ± 0.0007264 | 0.2570170 ± 0.0037845 | -0.3414580 ± 0.0420514 |
| | GN93 | 0.8709476 ± 0.0131182 | 0.9582489 ± 0.0049491 | 8726.4757855 ± 511.9232755 | 0.0086889 ± 0.0008745 | 0.2652811 ± 0.0047973 | -0.2860752 ± 0.0452687 |
| Zippy | AS09 | 1.1581361 ± 0.0155773 | 1.4080307 ± 0.0067626 | 4088.0162638 ± 157.7592445 | 0.0114439 ± 0.0007166 | 0.2638339 ± 0.0046896 | -0.1643385 ± 0.0273974 |
| | GN93 | 1.1377886 ± 0.0149818 | 1.4011171 ± 0.0064578 | 3790.4283438 ± 132.2327115 | 0.0138913 ± 0.0010639 | 0.2846720 ± 0.0074006 | -0.0664169 ± 0.0362219 |

Effect on AGE



6%

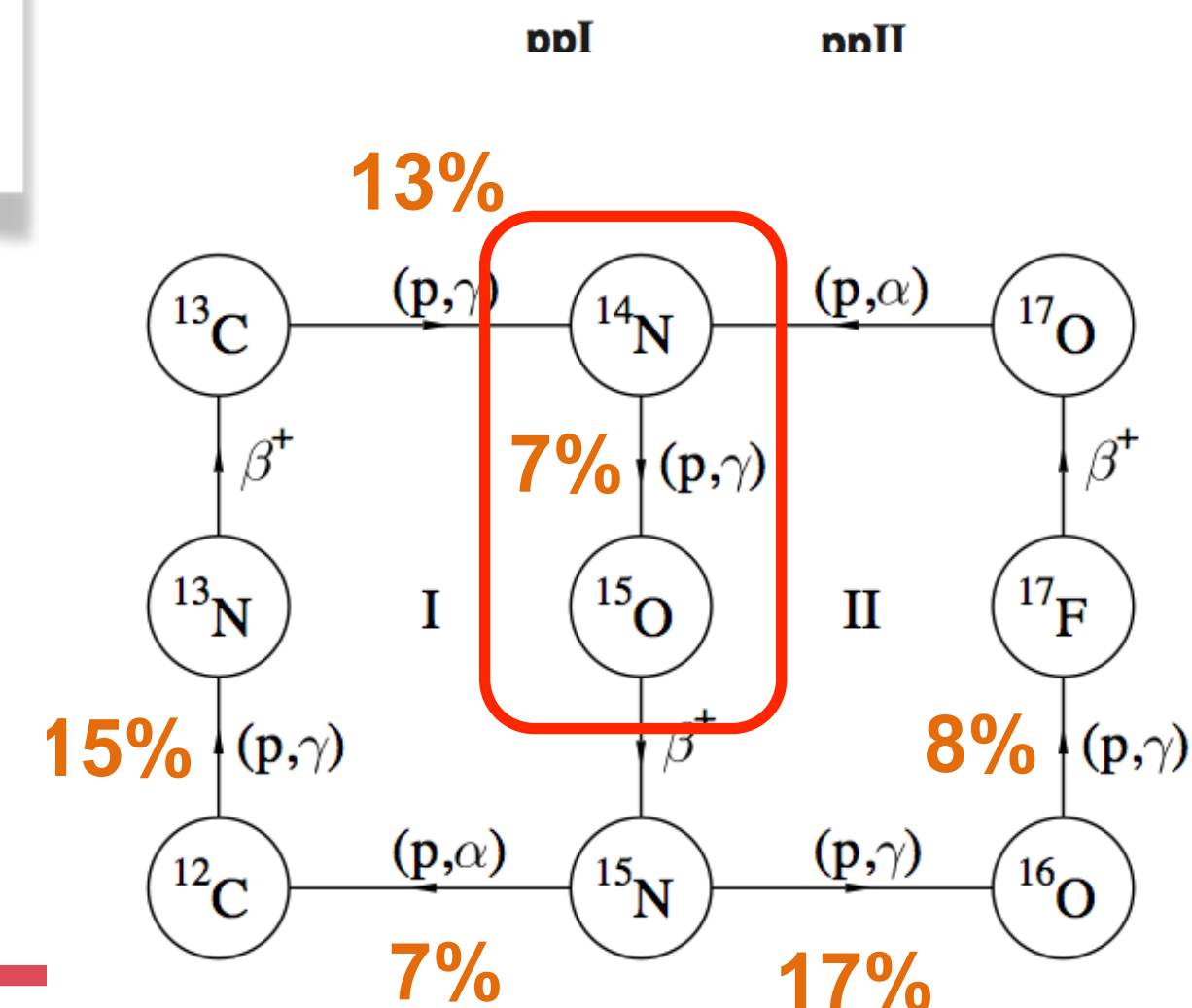
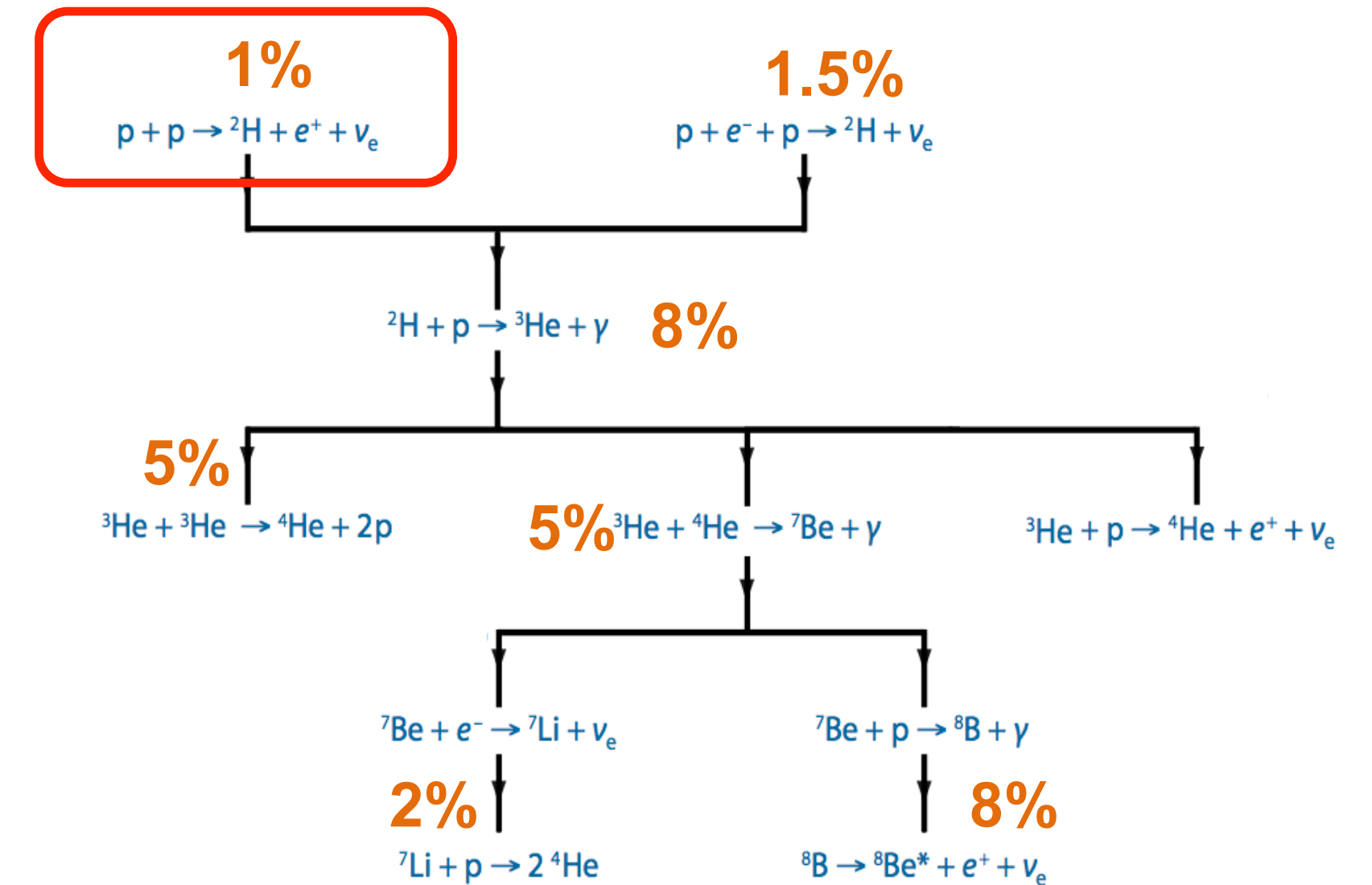
9%

8%

NUCLEAR REACTION RATES

- Stellar evolution CODE : [STAREVOL](#) (Siess et al.2000, Amard et al. 2019)
- Nuclear reaction rates : [NACRE](#) (Angulo 1999)
- [OPAL](#) opacities (Rogers & Nayfonov 2002) + Ferguson at low T.
- Convection: [MLT](#), Schwarzschild criterium
- Core-convective classical overshoot (ov=0.10) $T(\tau)$: [Eddington](#) relation
- Grey atmospheres
- Solar mixture : [AGSS09](#)
- Adiabatic oscillation code: [ADIPLS](#) (Christensen-Dalsgaard 2008)
- Optimization/Inference : [Aldo Serenelli one](#), with [Ball & Gizon](#) (2014) for surface effects correction

$^{14}\text{N} + \text{p} \rightarrow ^{15}\text{O}, \gamma : \pm 7\% \text{ and } \pm 14\%$
 $\text{p} + \text{p} \rightarrow \text{d} + \text{e}^+ + \nu_e : \pm 2\% \text{ and } \pm 5\%$

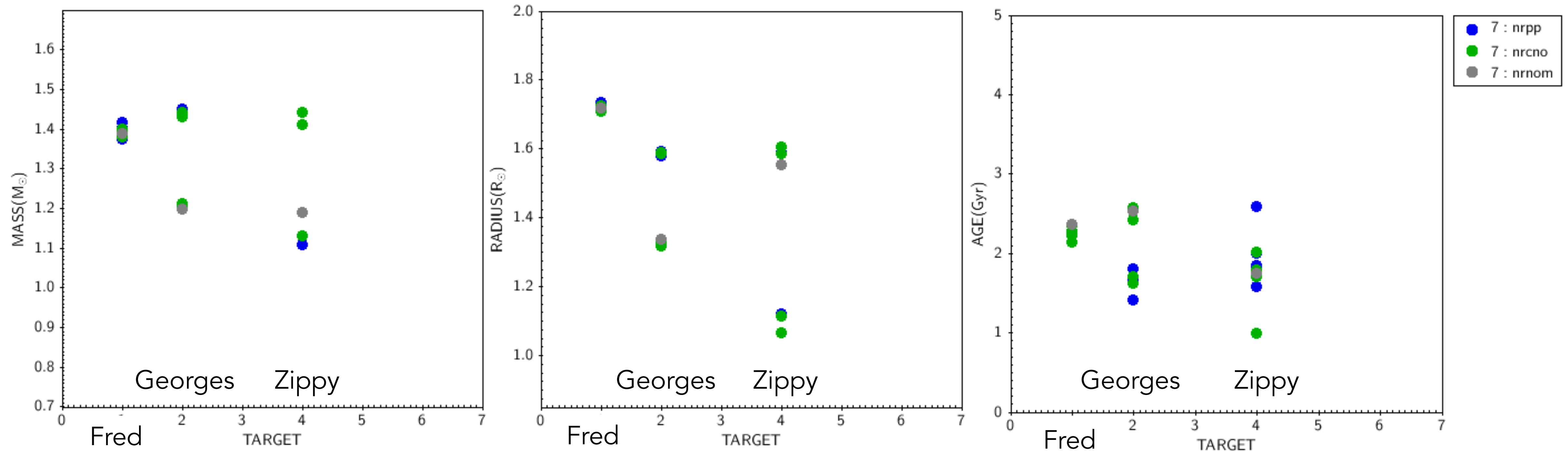


From compilation
 Solar Fusion II
 (Aldelberger et al.
 2011)

NUCLEAR REACTION RATES

From compilation Aldelberger et al. 2011

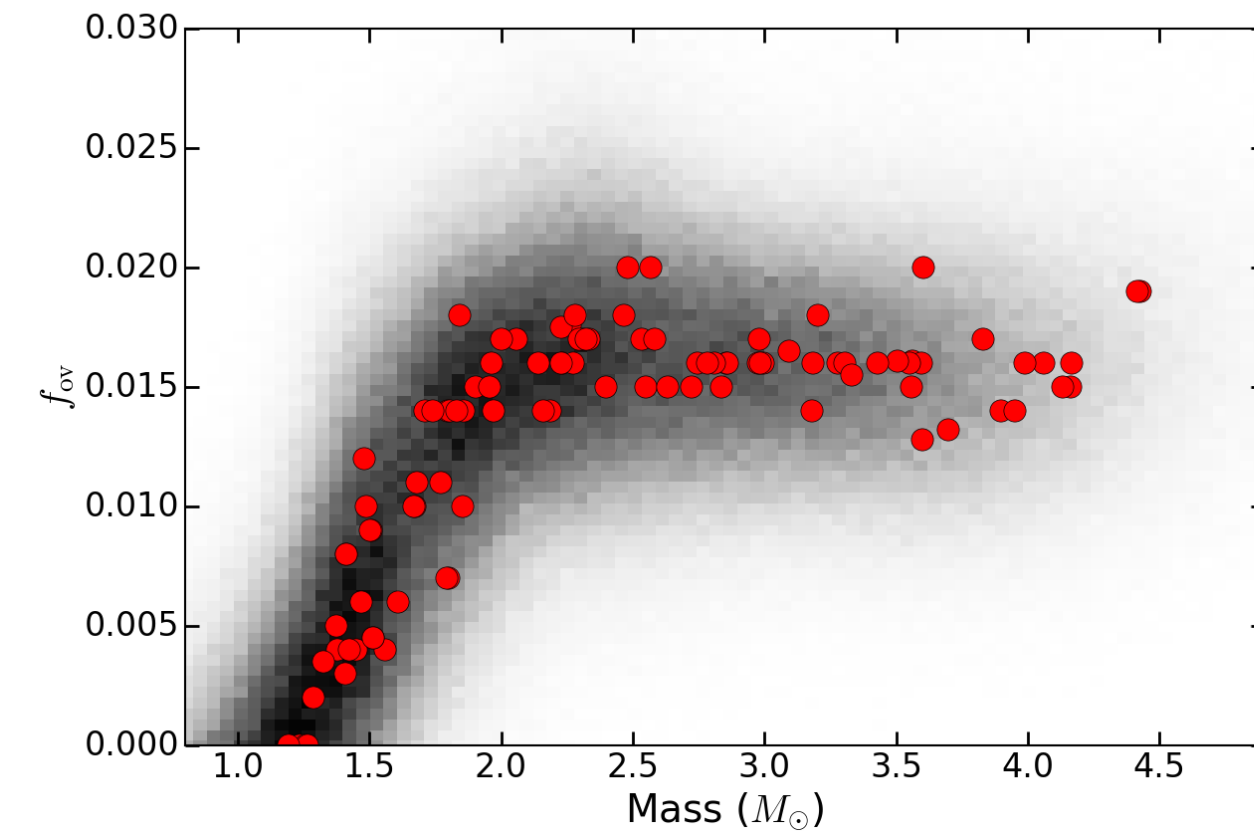
$^{14}\text{N} + \text{p} \rightarrow ^{15}\text{O}, \gamma$: +/- 7%. and +/- 14%
 $\text{p} + \text{p} \rightarrow \text{d} + \text{e}^+ + \nu_e$: +/- 2% and +/- 5%



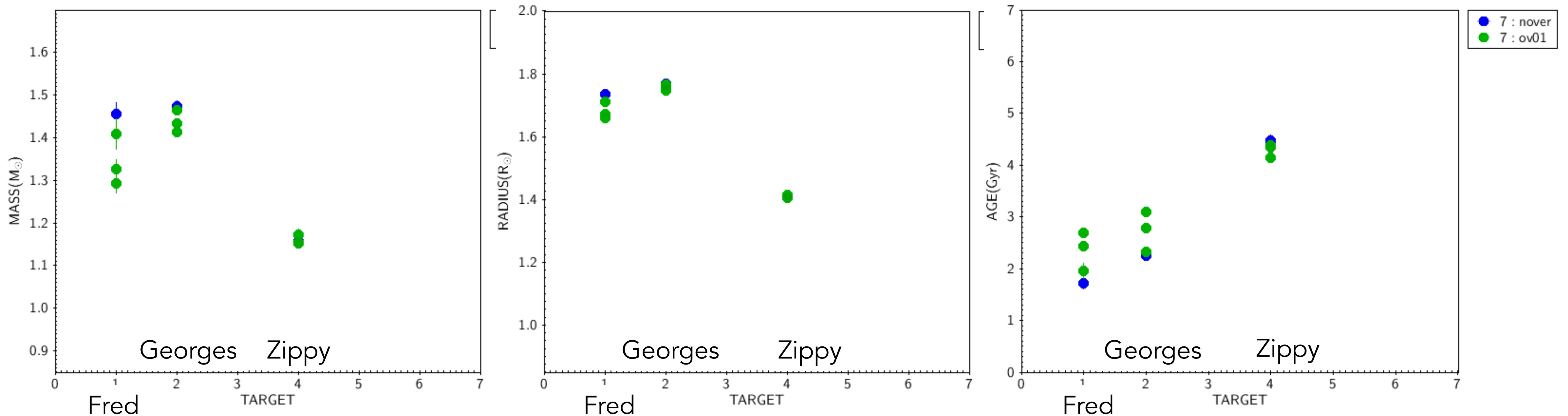
CONVECTIVE CORE OVERSHOOTING

- Diffusive overshoot, with a parameter $f_{ov}=f(M)$ between 1.1 and 1.4 M_{sun} . No overshoot at $M=1.1M_{sun}$ and full value for $M>1.4M_{sun}$. Four different values: $f_{ov}=0.$, 0.01, 0.02 and 0.03

GARSTEC models & Aldo's optimisation method



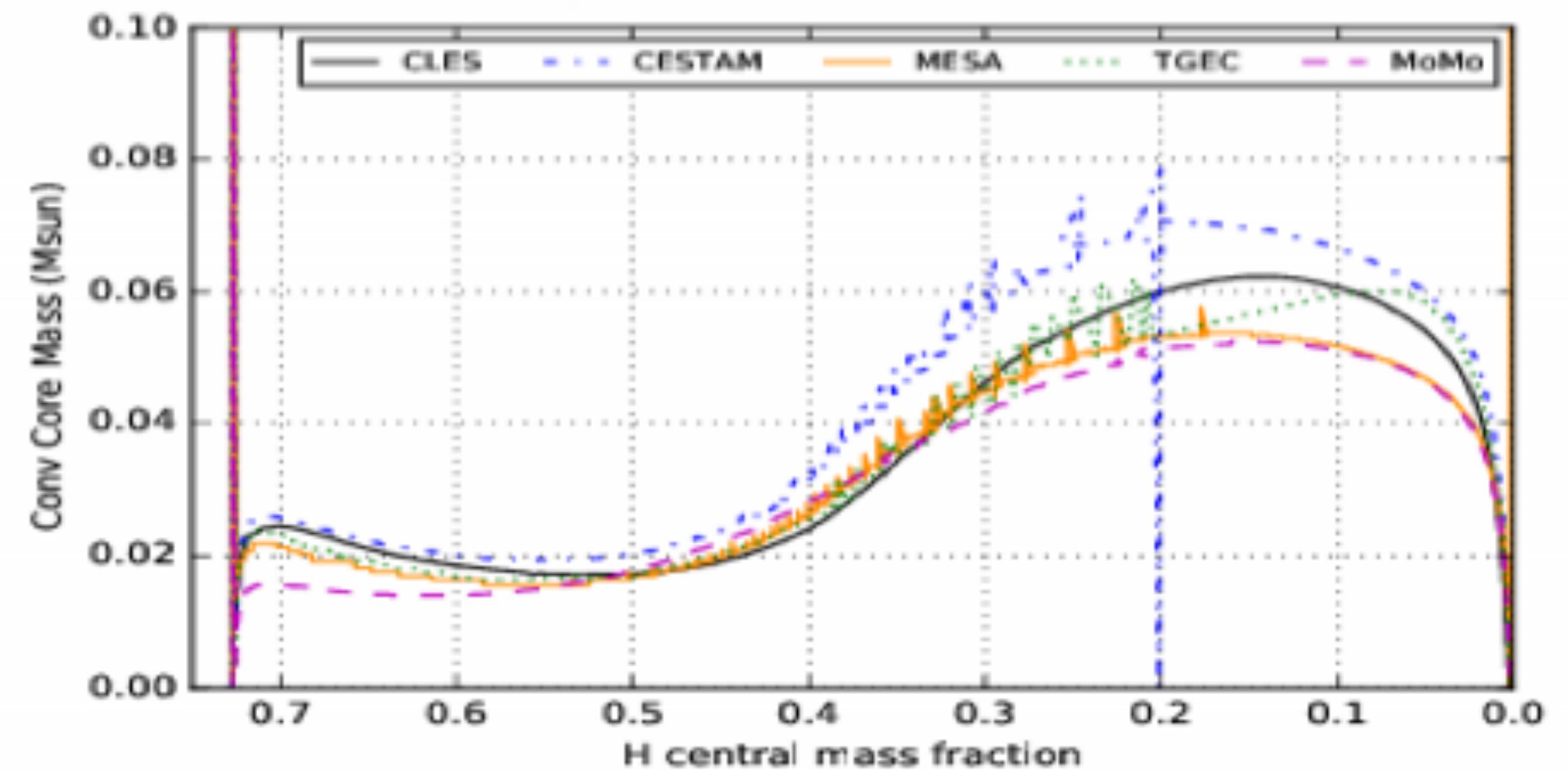
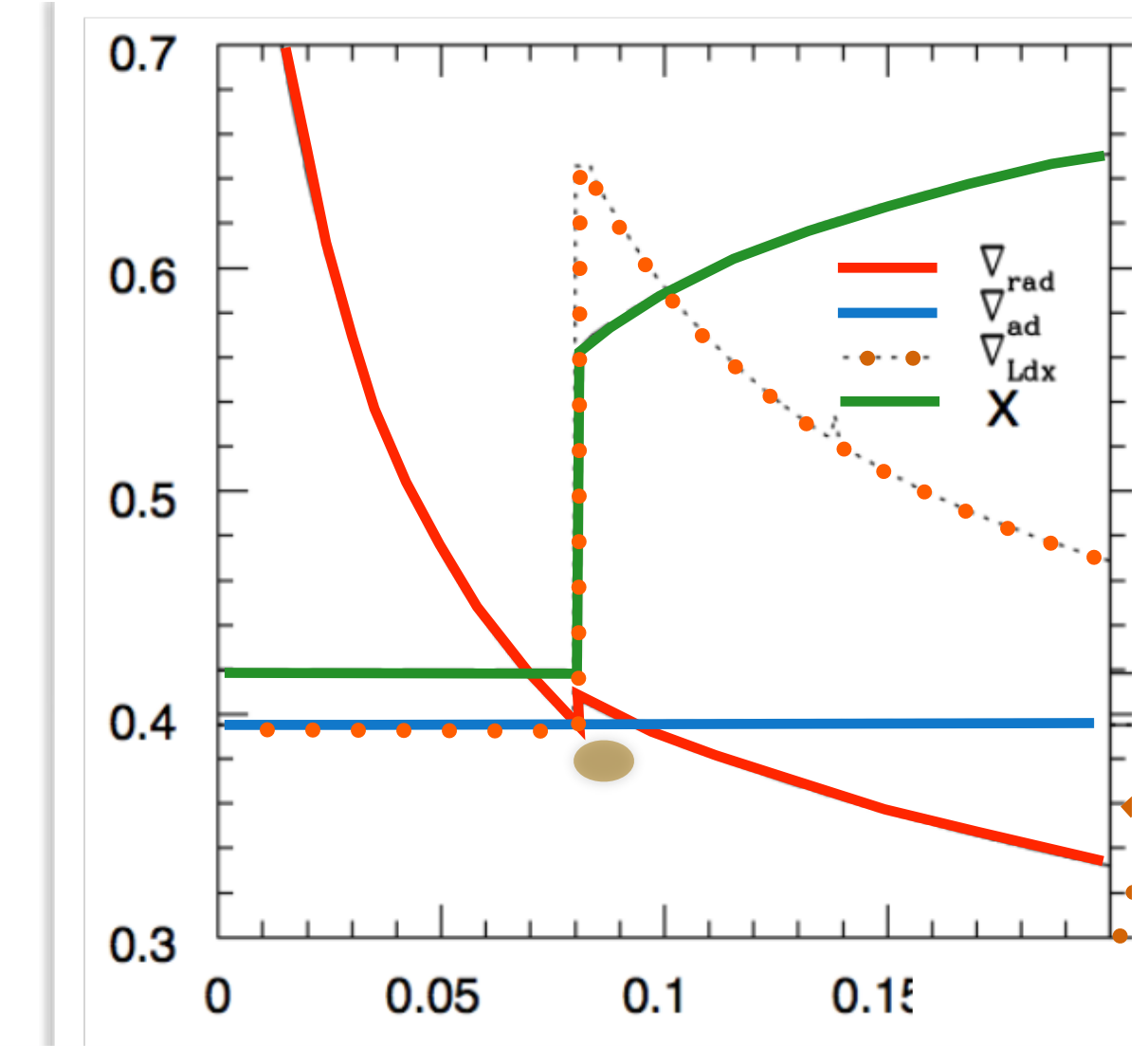
Claret & Torres 2019



SEMICONVECTION AT THE BORDER OF CONVECTIVE CORES

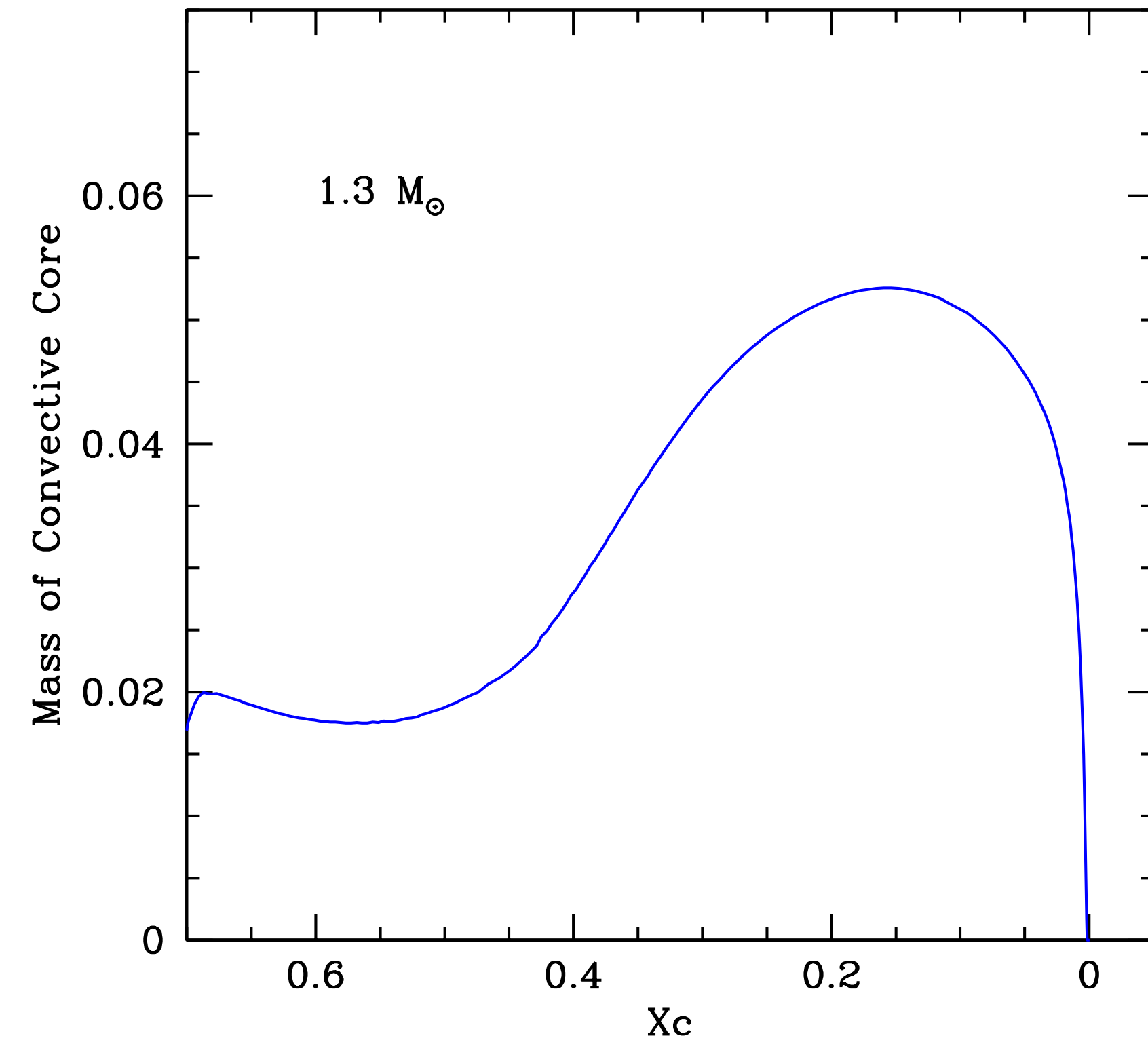
- The strong gradient of chemical composition at the border of convective cores that grows => a region that is convectively unstable after Schwarzschild criterum, and only vibrational unstable by Ledoux's one.
- HOW SHOULD WE TREAT THAT REGION?
- Partial mixing until neutrality of gradients?
- Diffusion coefficient with free parameters?
- Do not mix but set an adiabatic temperature gradient?

CLES (Scuflaire et al 2008) here used L_{dx} criterium for convection; double mesh point at the boundary of a convective region; extrapolation from the core ; no mixing of the semiconvective region + adiabatic gradient there



SEMICONVECTION AT THE BORDER OF CONVECTIVE CORES

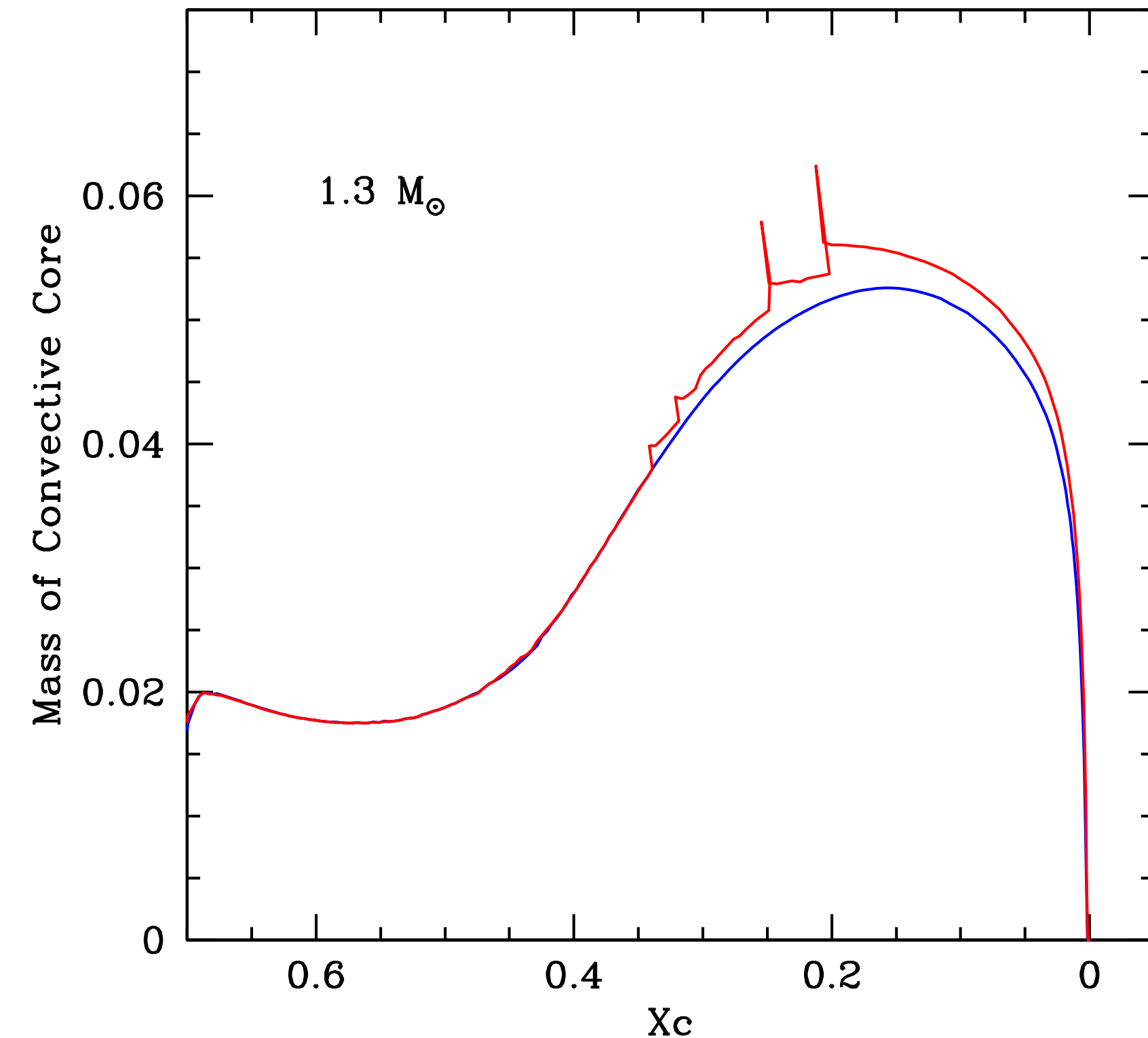
CLES here used [Ldx criterium](#) for convection; double mesh point at the boundary of a convective region; extrapolation from the core ; no mixing of the semiconvective region + adiabatic gradient there



SEMICONVECTION AT THE BORDER OF CONVECTIVE CORES

CLES here used **Ldx criterium** for convection; double mesh point at the boundary of a convective region; extrapolation from the core ; no mixing of the semiconvective region + adiabatic gradient there

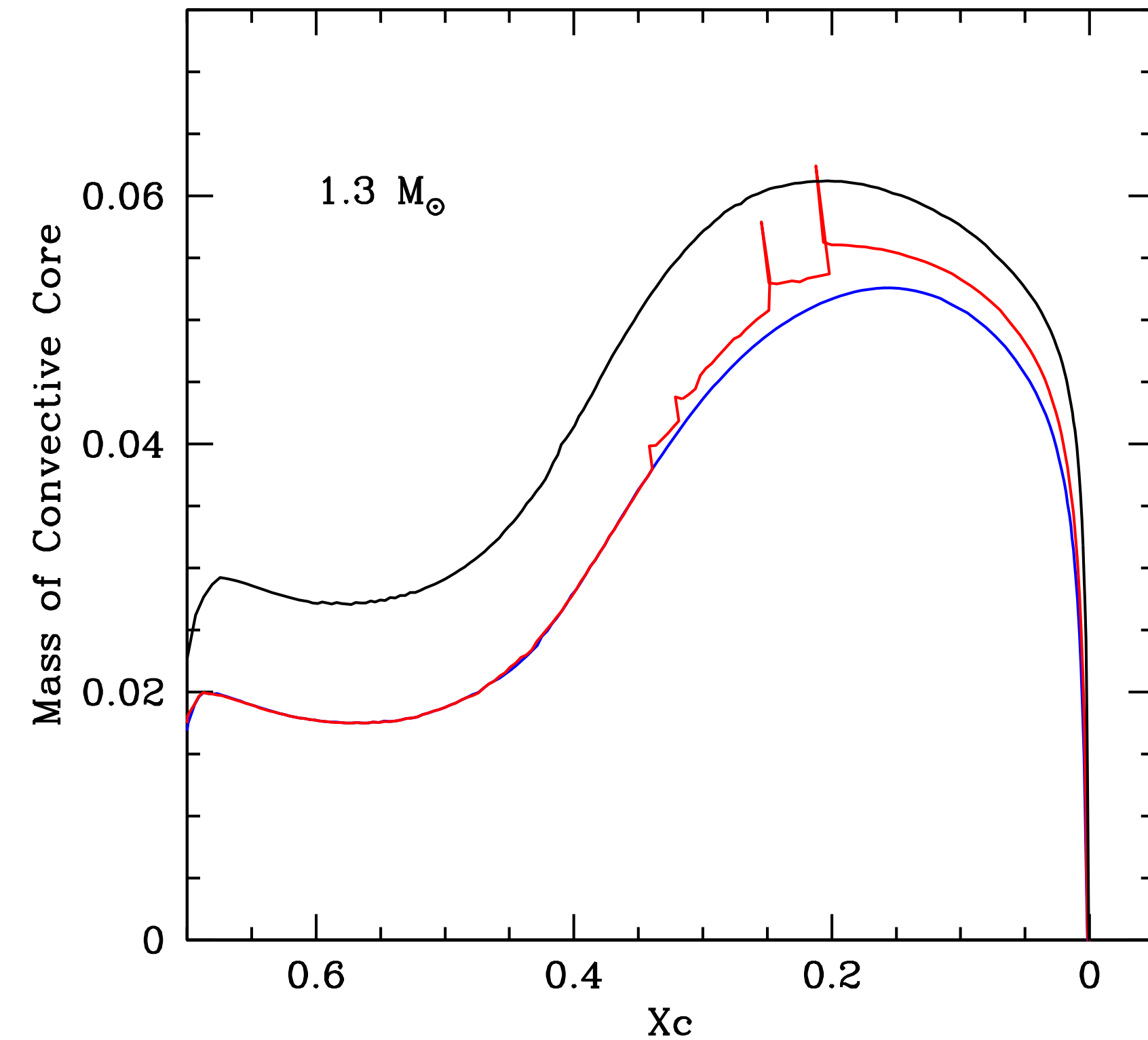
CLES with **Sch criterium** for convection;

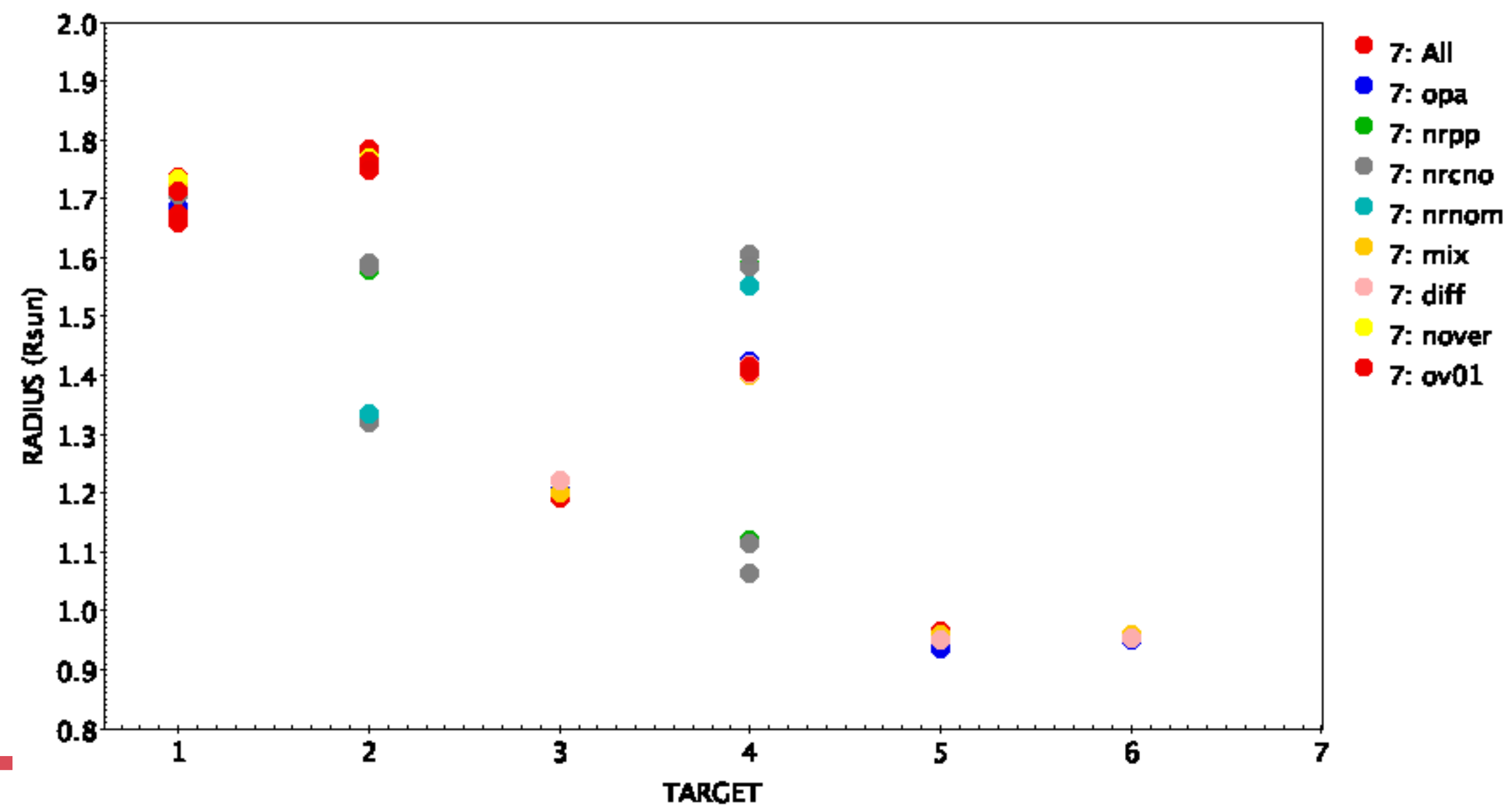
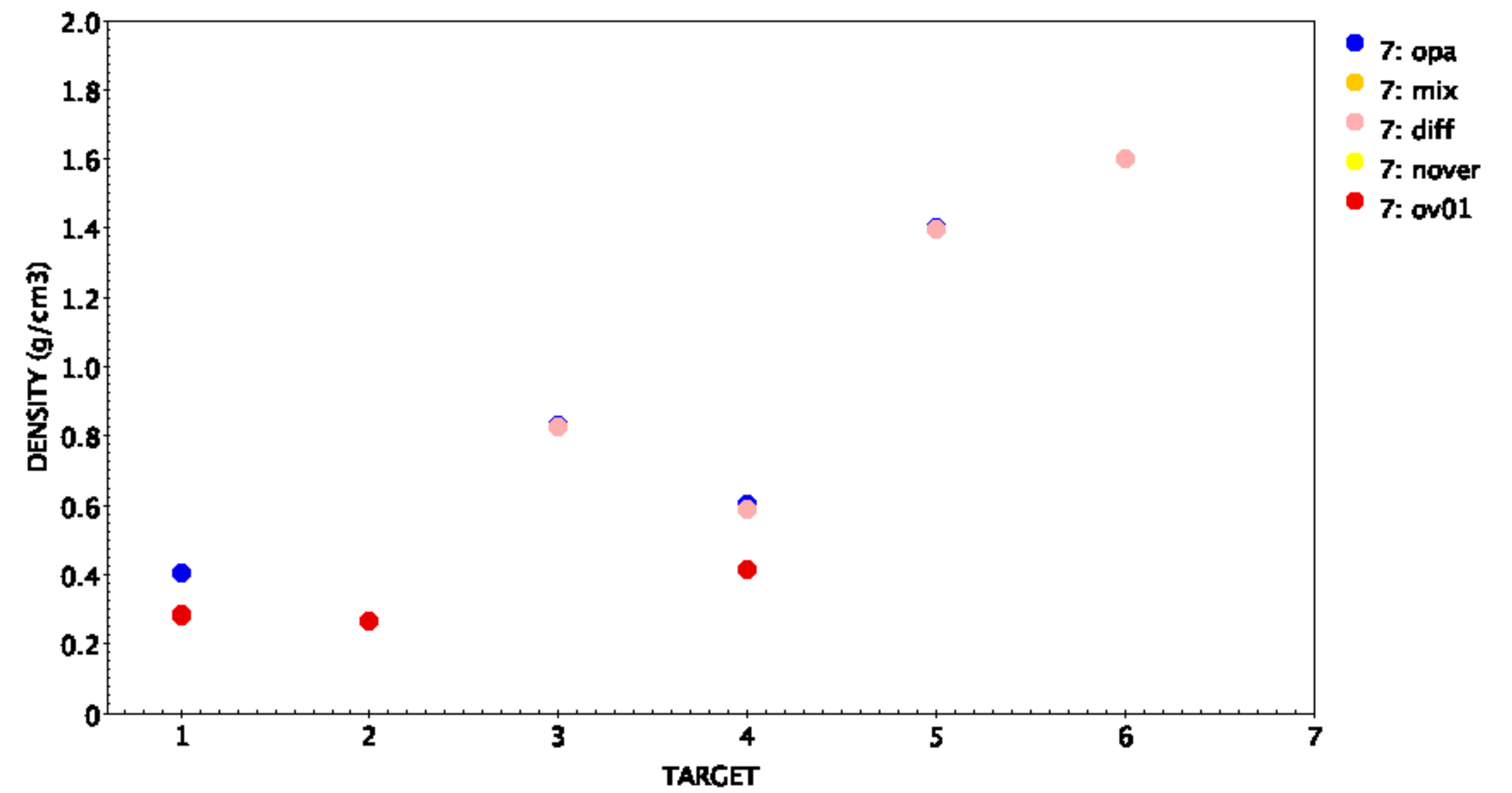
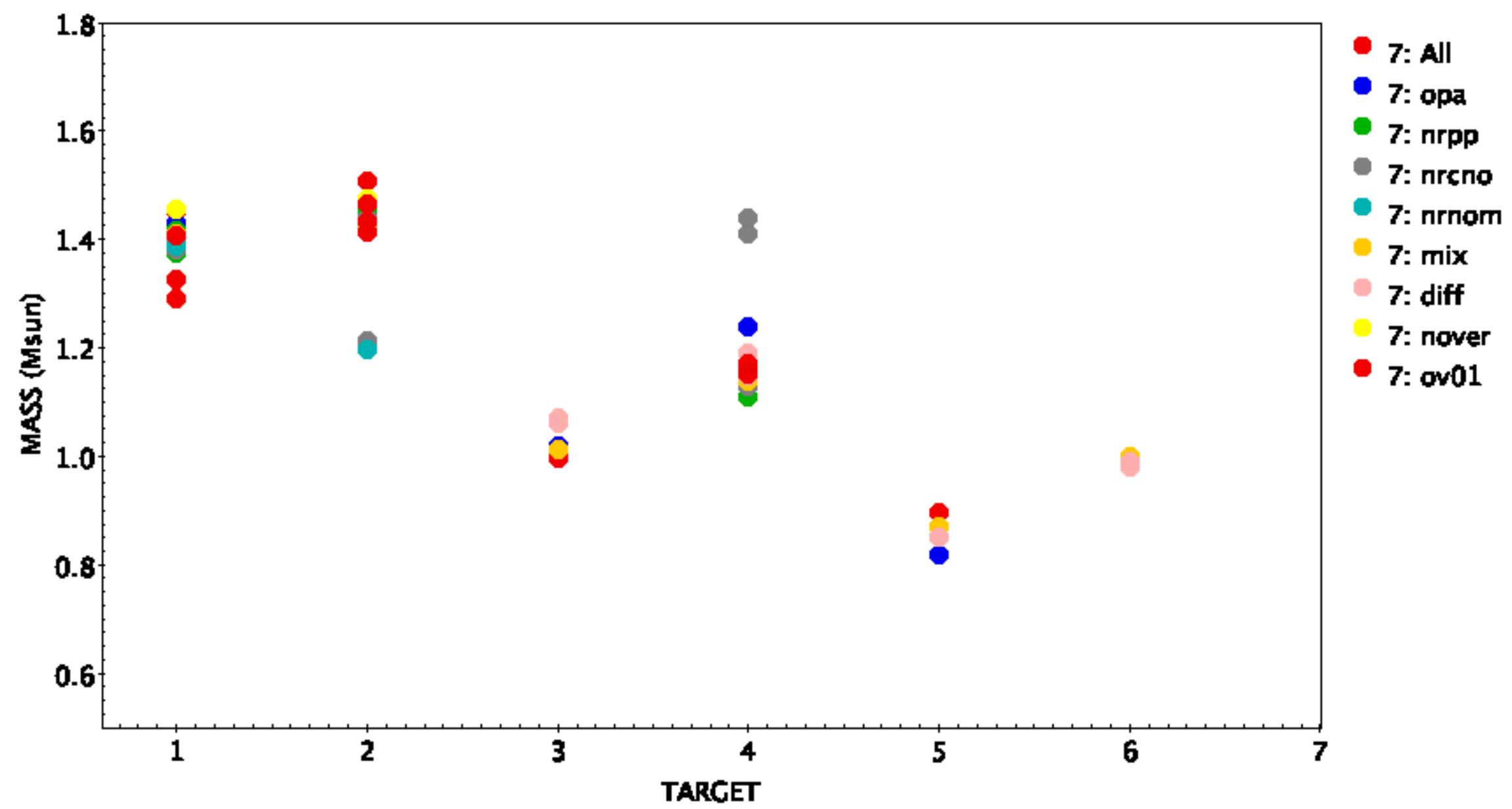


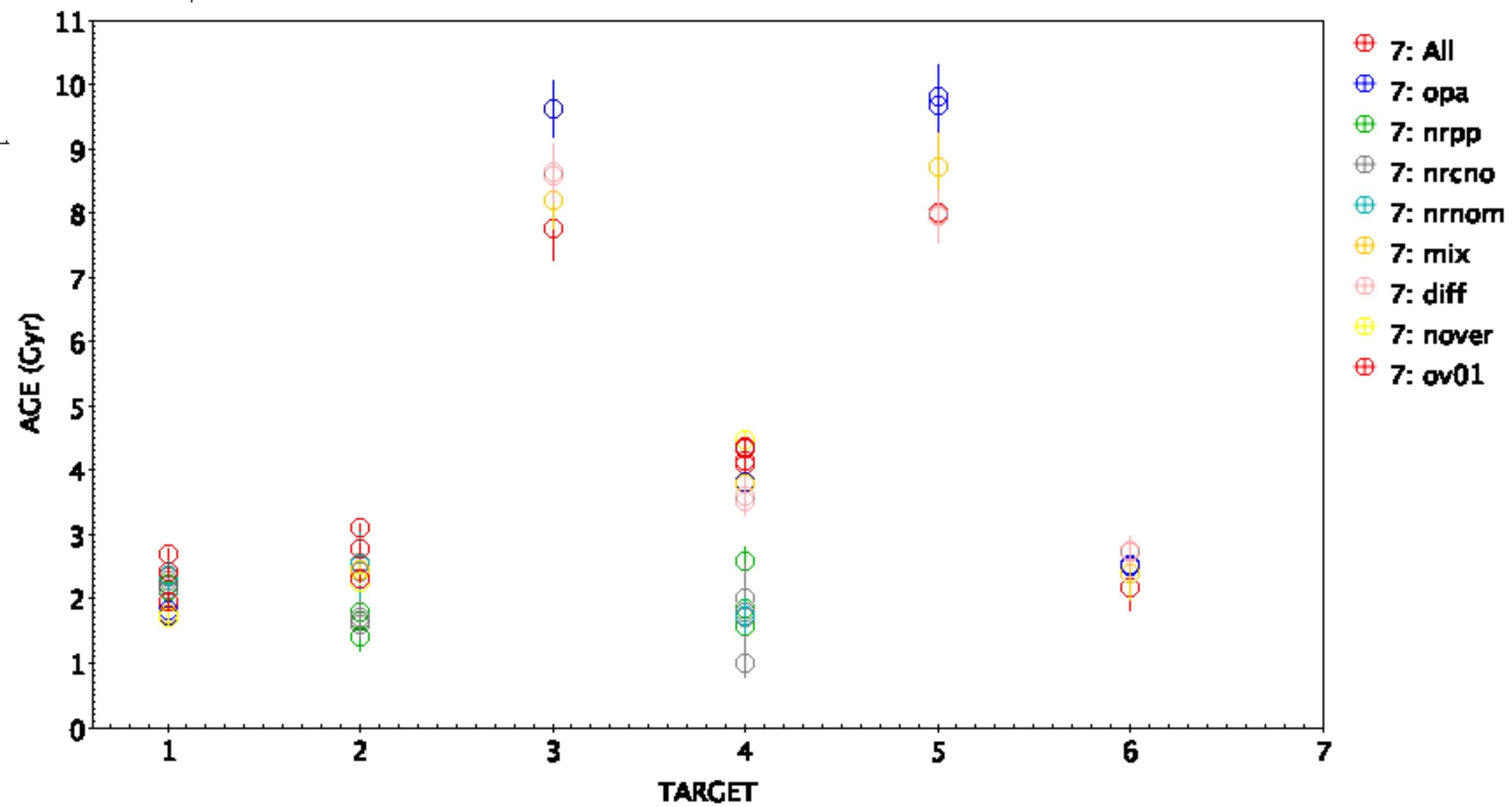
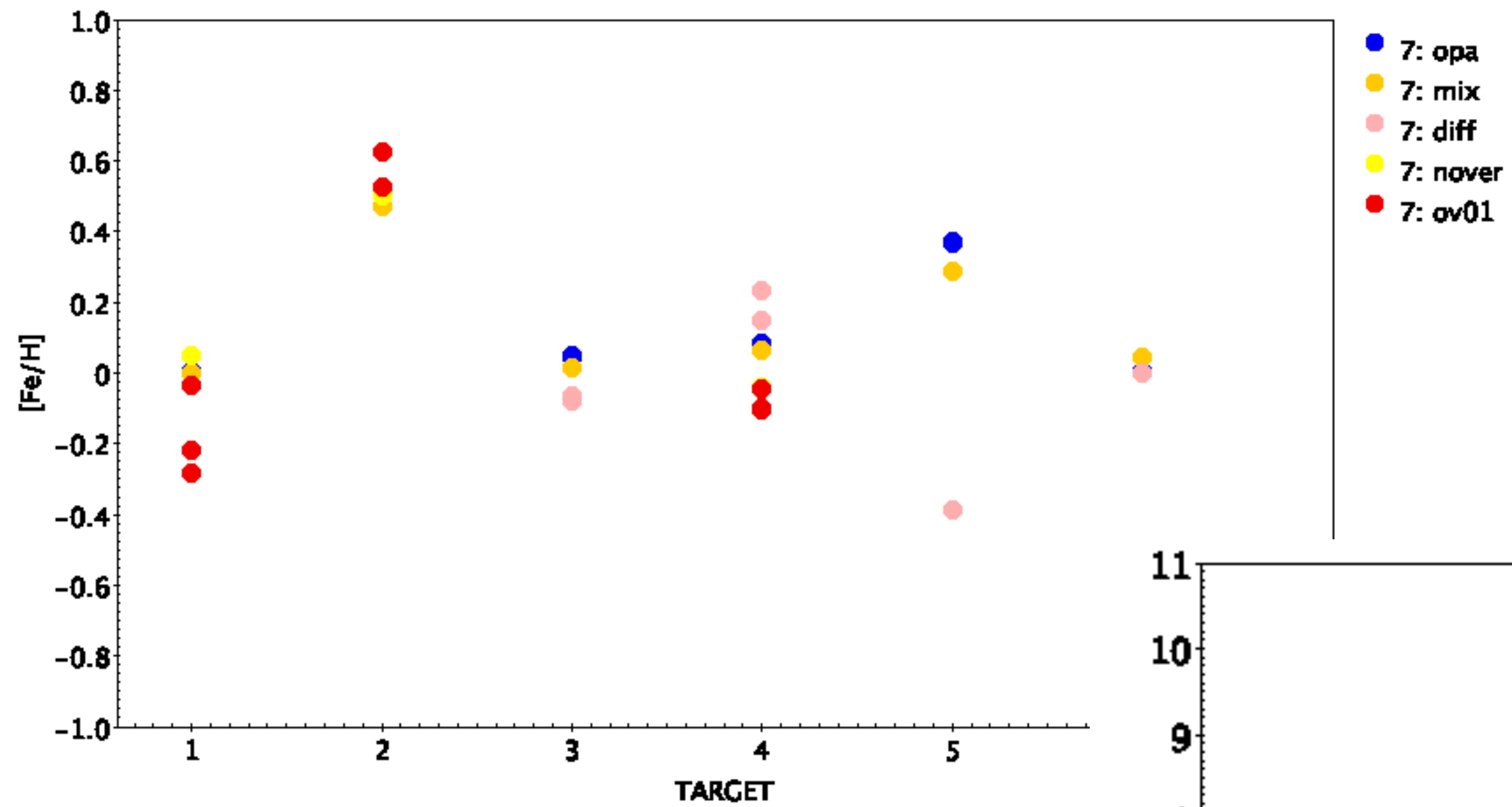
SEMICONVECTION AT THE BORDER OF CONVECTIVE CORES

CLES here used L_{dx} criterium for convection; double mesh point at the boundary of a convective region; extrapolation from the core ; no mixing of the semiconvective region + adiabatic gradient there

CLES with **Sch criterium + 0.05 H_p** of instantaneous overshooting ;







Conclusions

- As expected, mixing processes are the main contributor to the uncertainties
- Opacity tables and diffusion implementation, at least for the domain considered have a low impact
- Solar mixture can affect by 3% the mass and 9% the age
- We proceed with optimisation also with models with semiconvection vs overshooting
- To improve our study of nuclear reaction rate effects

