

# Angular momentum evolution of late-type stars

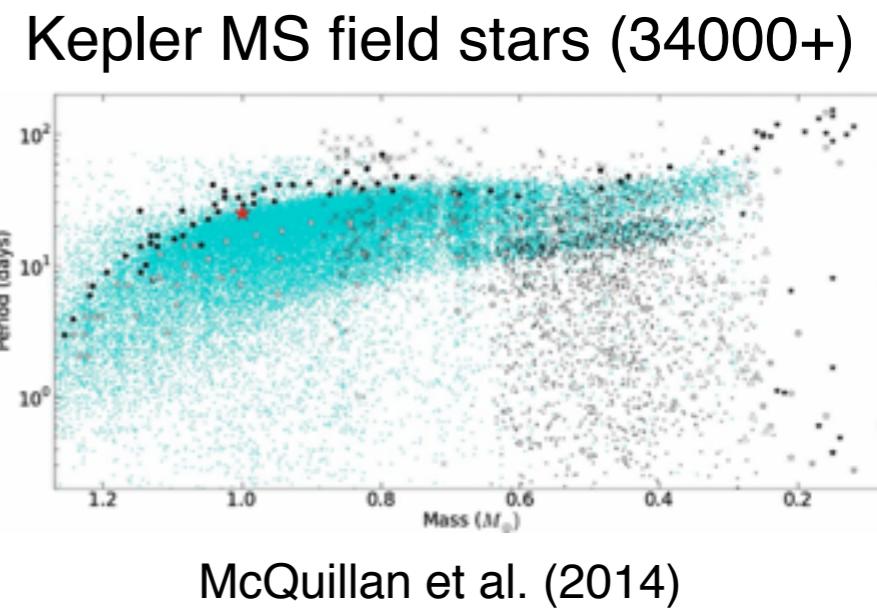
Florian Gallet

PLATO Barcelona 21/11/2019



# Context

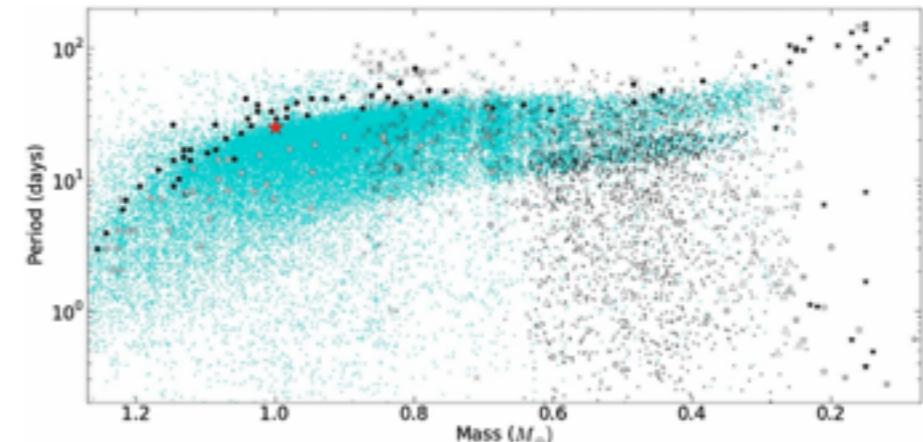
- Late-type stars =  $0.3 - 1.2 M_{\text{sun}}$
- Lots of rotational period measurements
  - CoRoT, Kepler, K2
  - Gaia DR2 (DR3/DR4)
  - Future => PLATO, JWST
- Strong observational constraints
- Two ways to model  $P_{\text{rot}}$ 
  - Stellar model (ab-initio modeling)
  - Parametric model



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Kepler MS field stars (34000+)



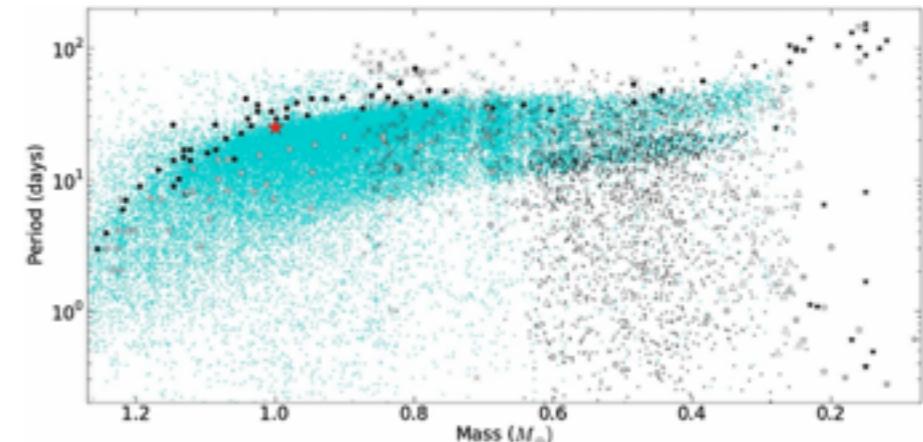
McQuillan et al. (2014)



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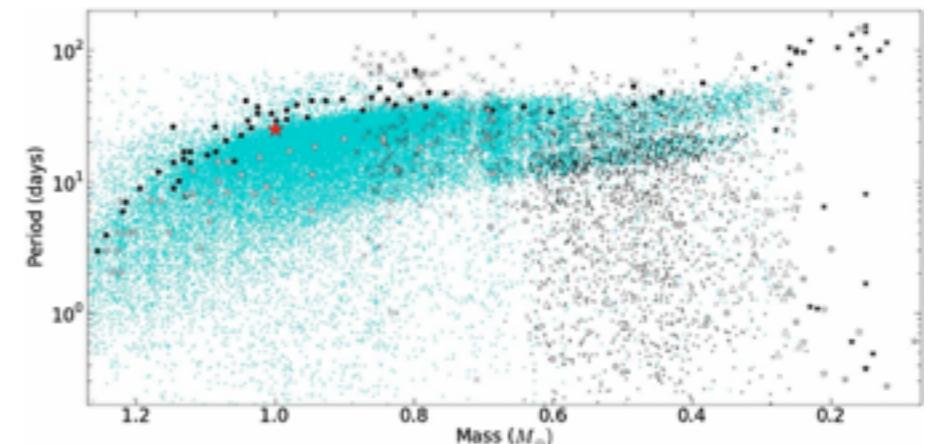
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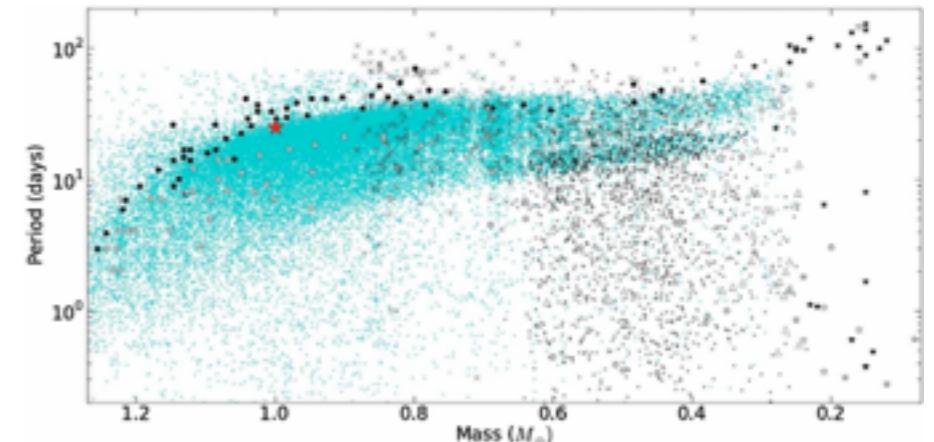
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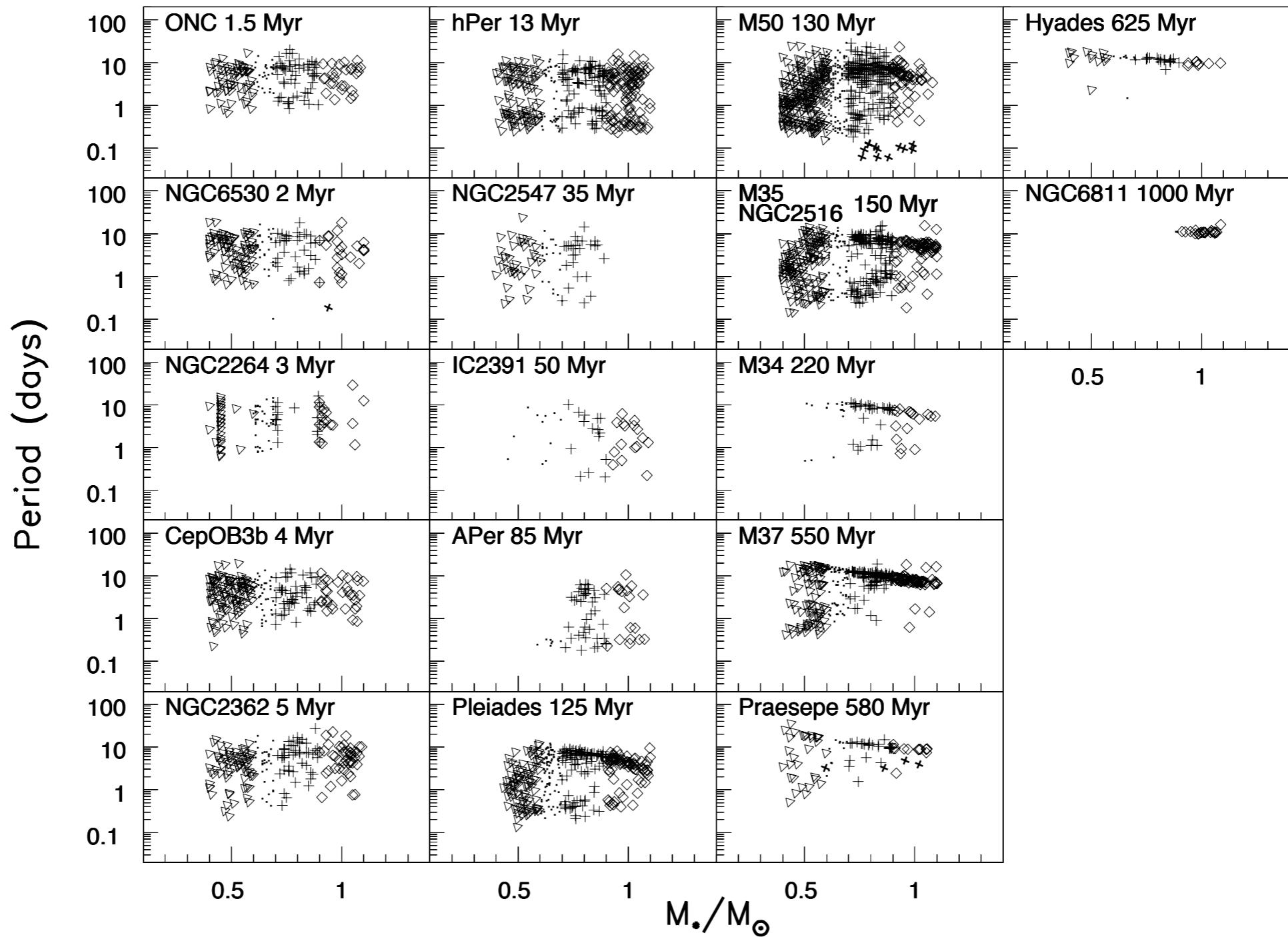
## Goal

Use these observations to understand the general mechanisms involved in the AM evolution



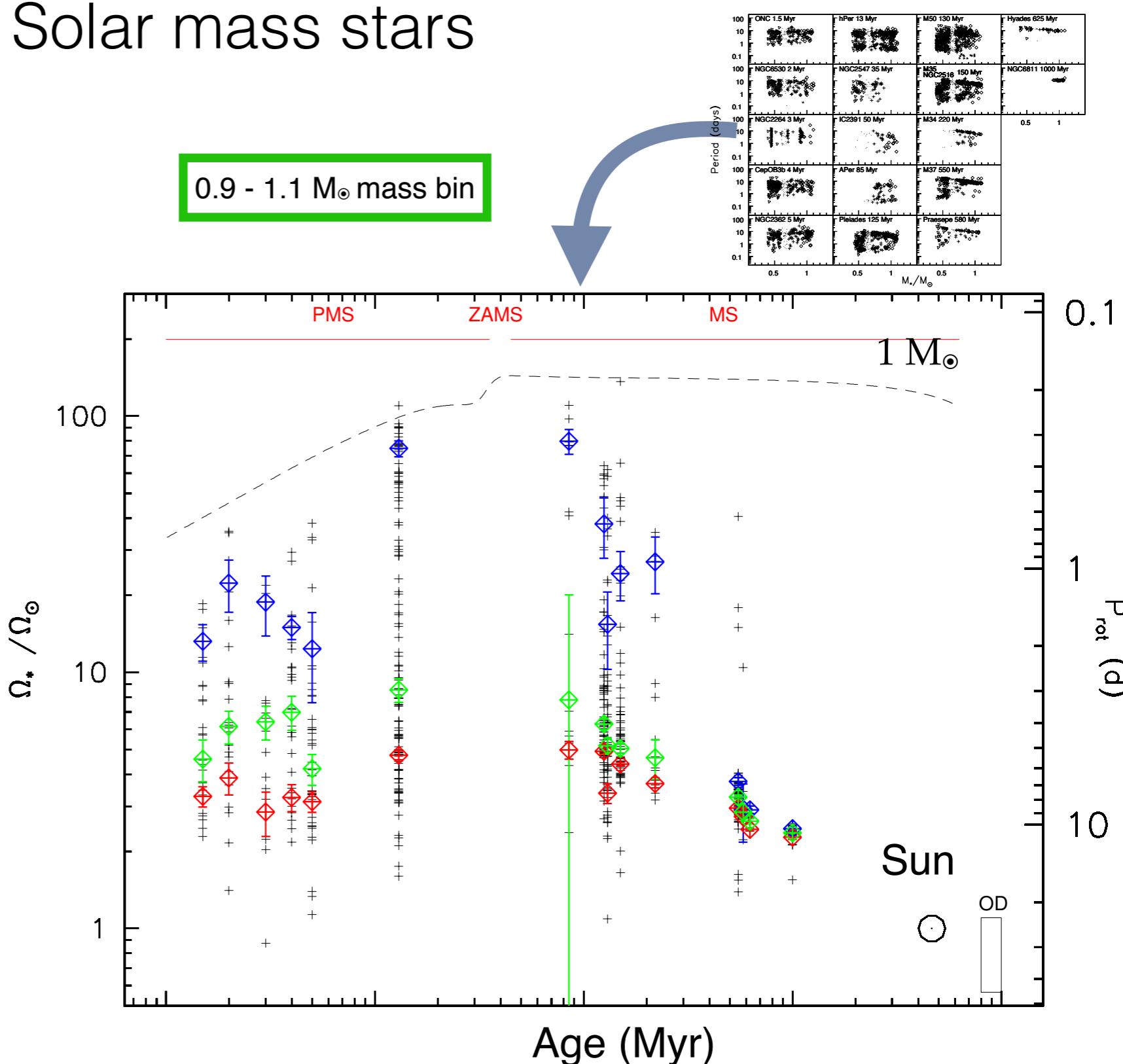
# Observed rotational evolution

## Solar mass stars



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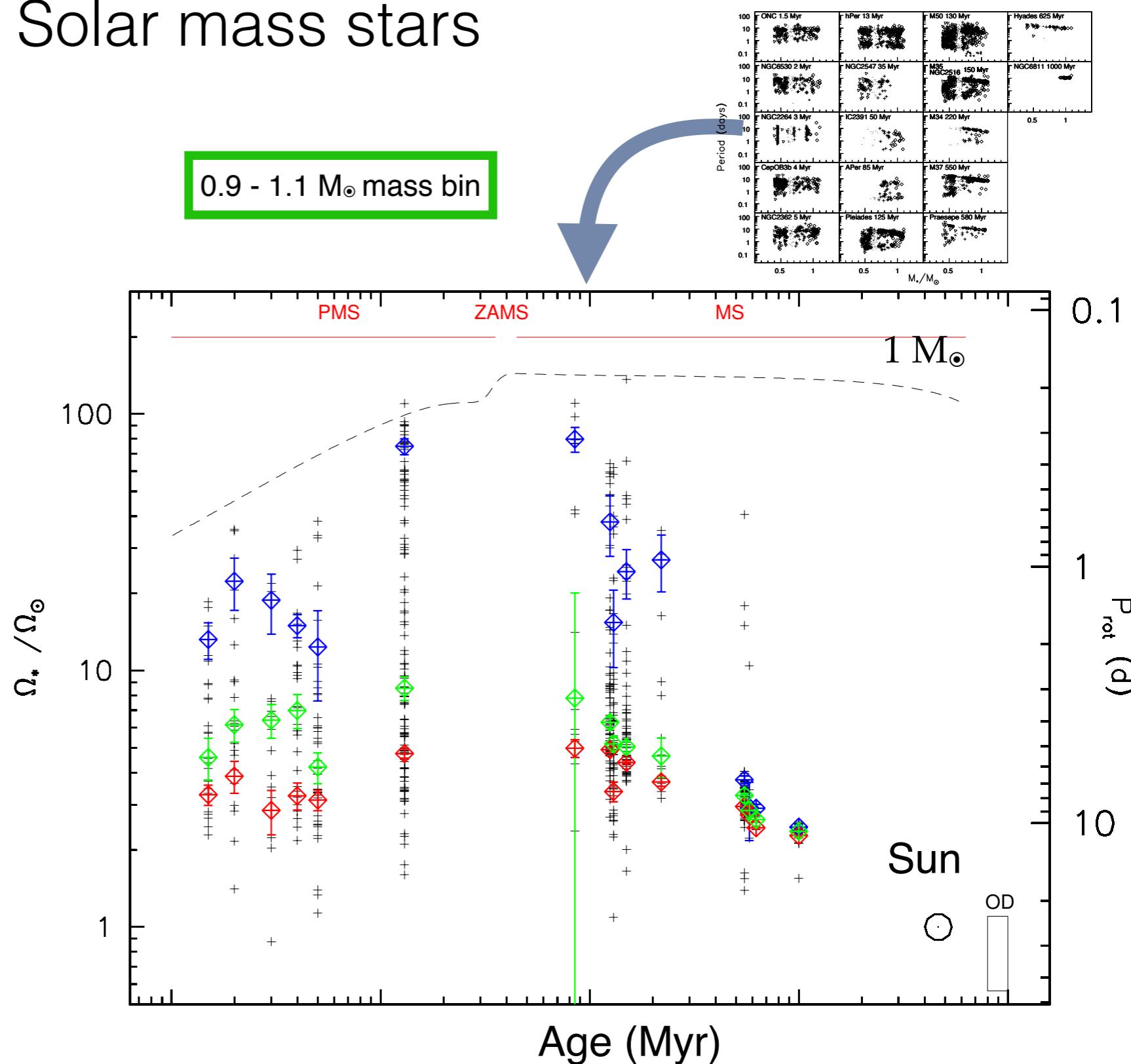
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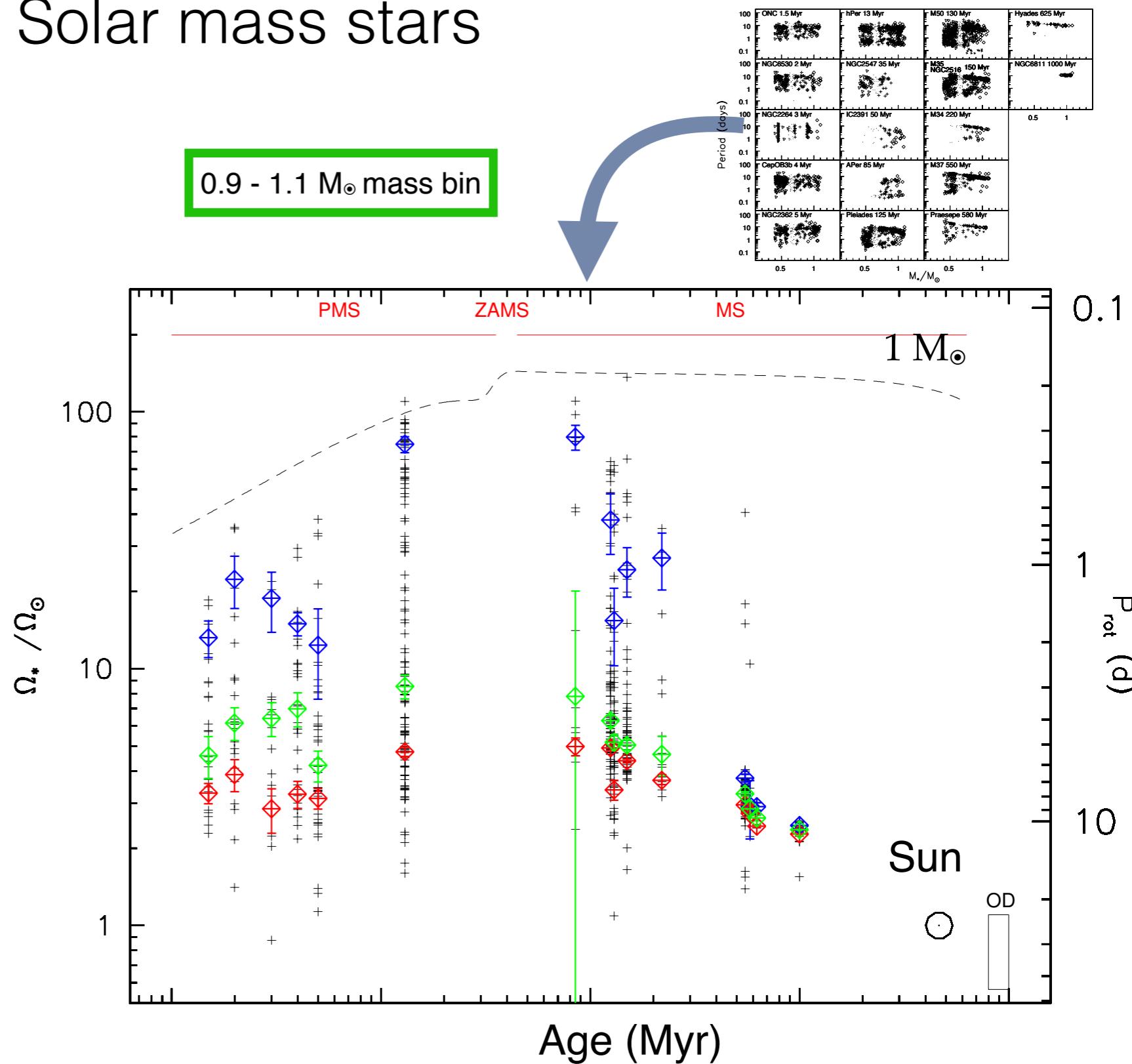
- 1st, 2nd and 3rd quartiles
  - 25th
  - median
  - 90th



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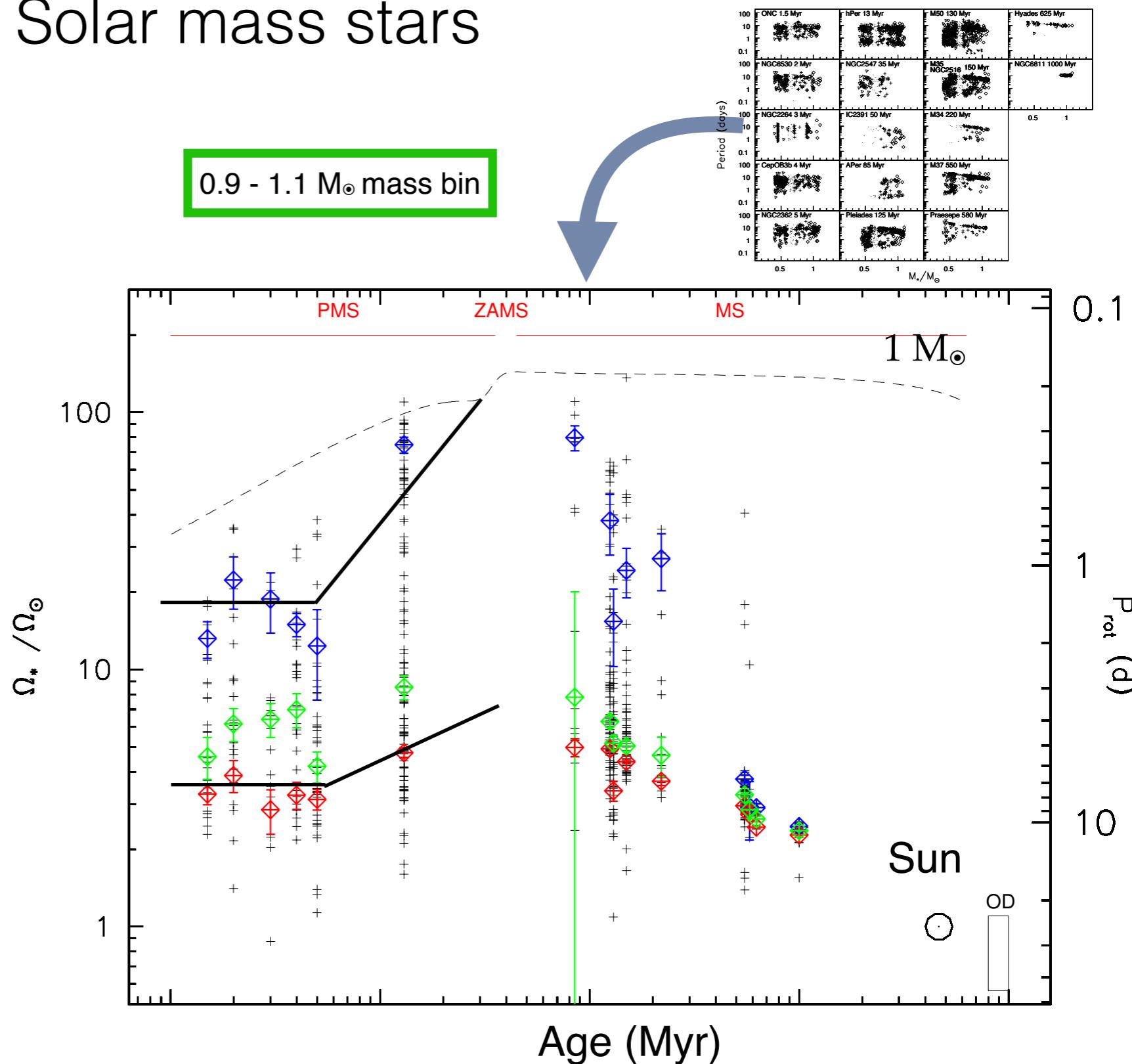
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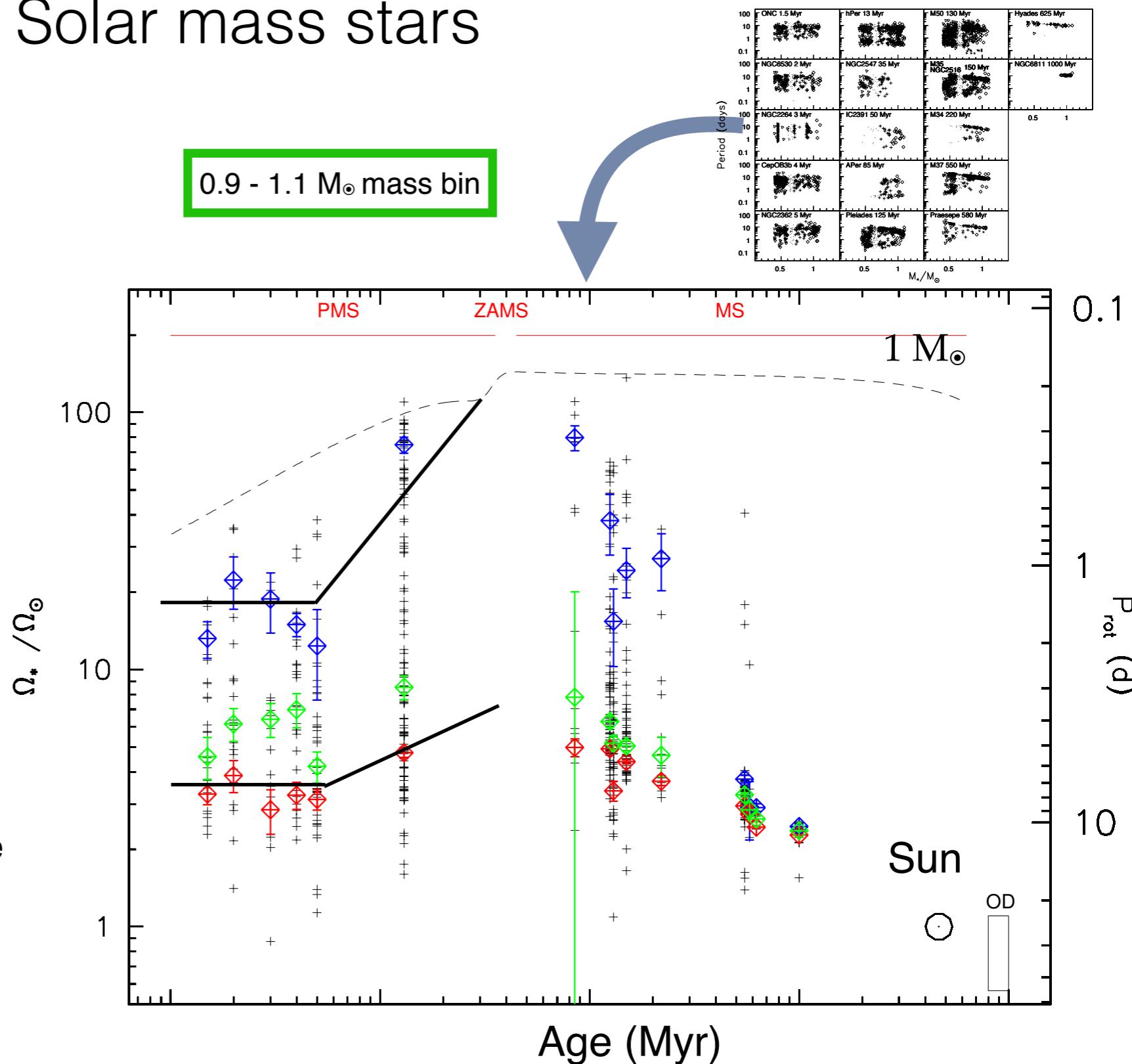
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- PMS
  - Early PMS : rotation period  $\approx$  constant
  - Late PMS : spin-up due to contraction (up to 200 km/s)



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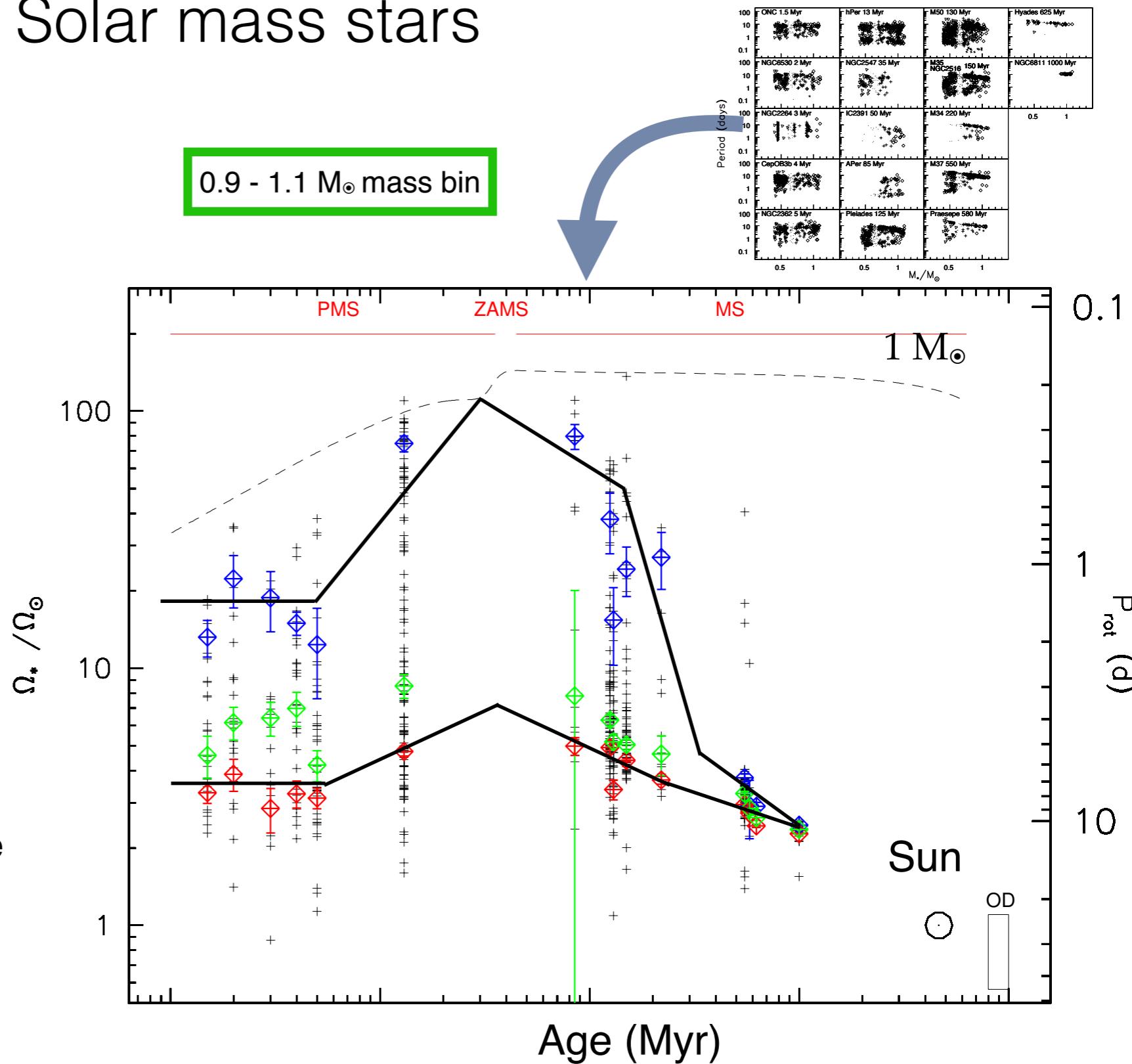
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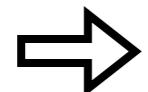
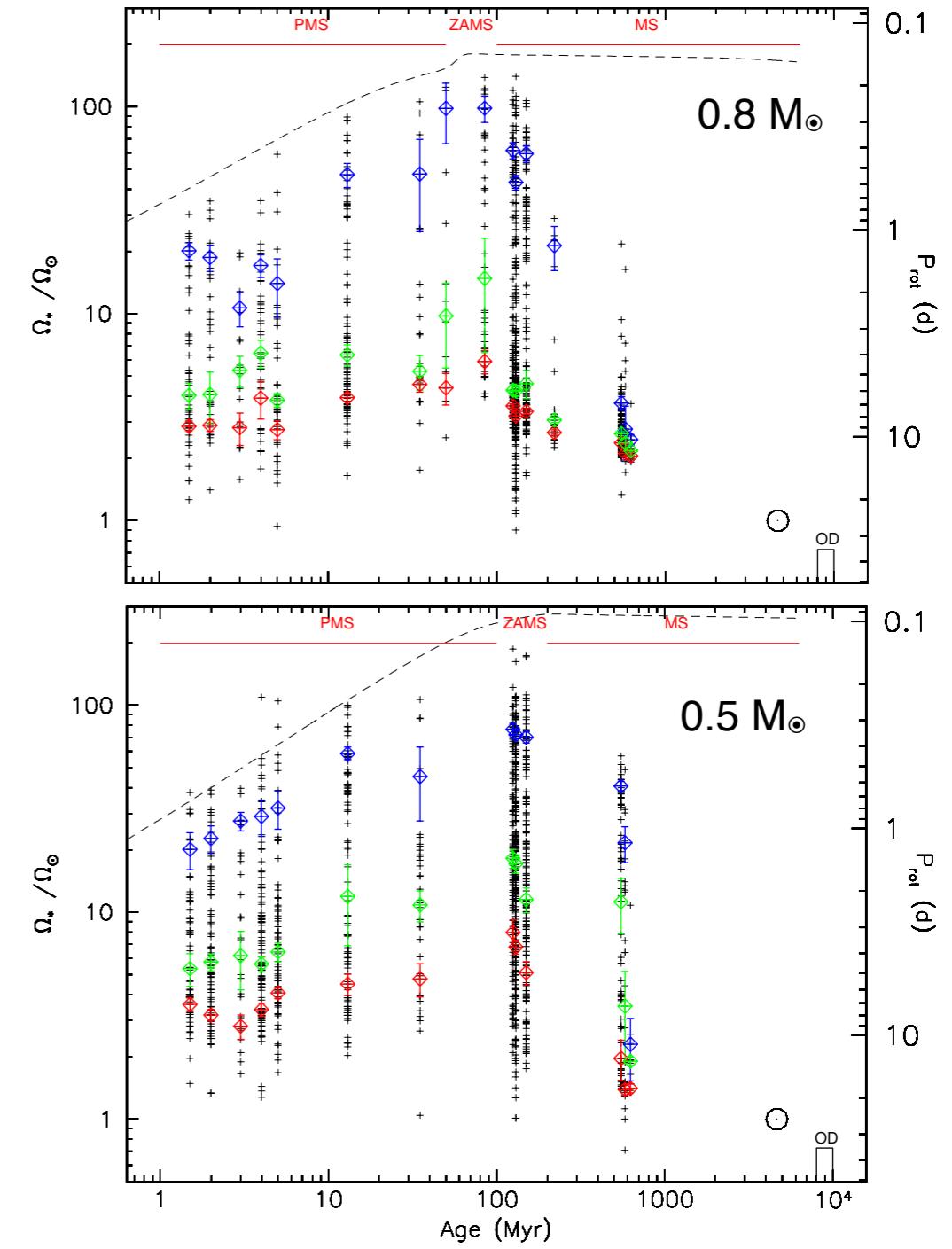
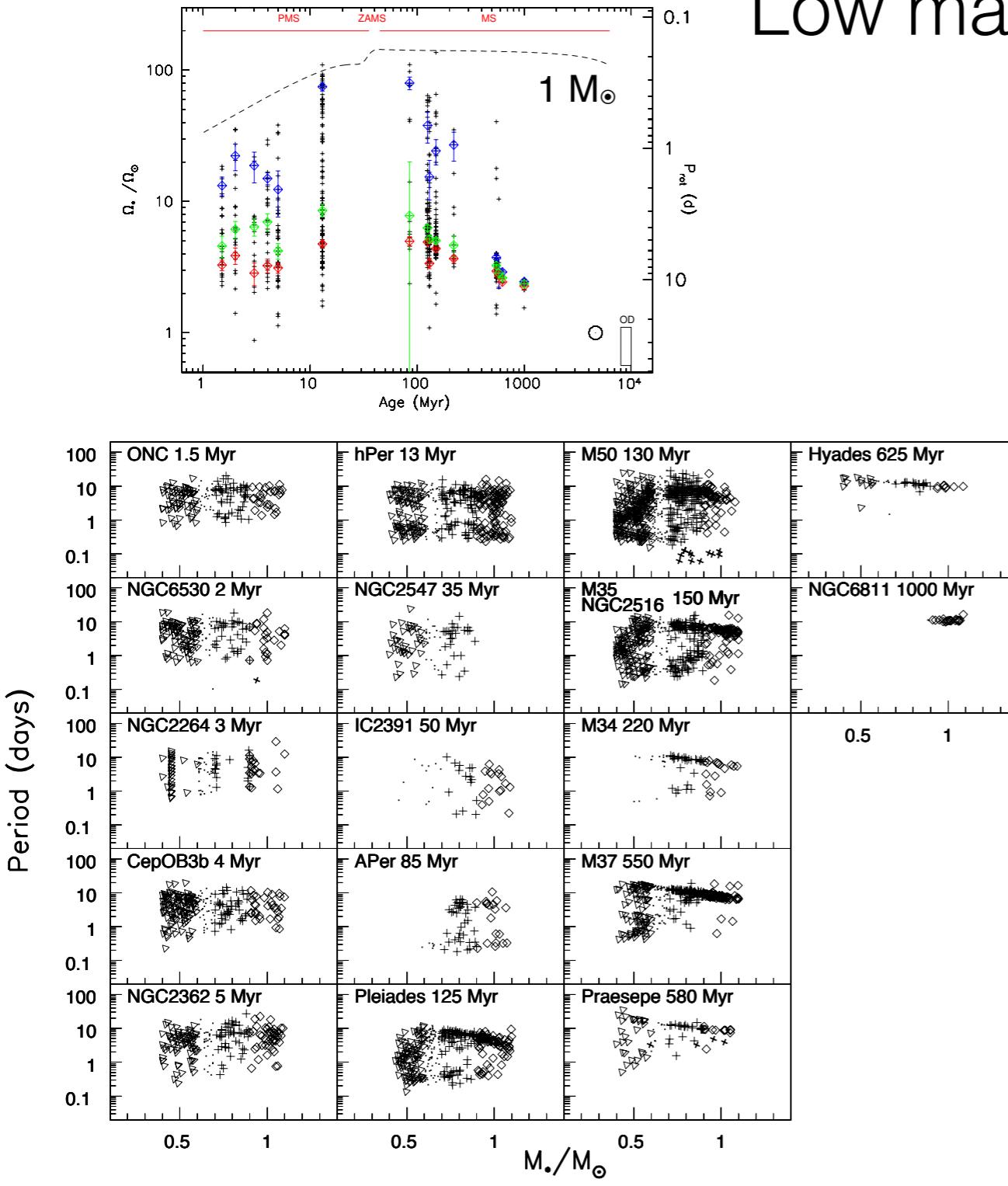
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- ZAMS
  - Stabilisation of the stellar structure
- MS
  - Rotational convergence



# Observed rotational evolution

Low mass stars



AM evolution models must reproduce these observations

# Physical ingredients

- **Stellar angular momentum:**  $J_* = \Omega_* I_*$

See also Keppens+95, Krishnamurthi+97,  
Somers & Pinsonneault15, Lanzafame & Spada15,  
Sadeghi Ardestani+16, ...

AM evolution model = **Stellar evolution model + AM evolution mechanisms**

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Weber & Davis (1967)

$$\left. \frac{dJ}{dt} \right|_{\text{wind}} \approx \Omega_* \dot{M}_{\text{wind}} r_A^2$$

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Need to link  $r_A^2$  and  $\dot{M}_{\text{wind}}$  to stellar properties

- mass-loss rate?
- magnetic field?
- open flux?
- rossby number?

See also Matt+12,15, Reiners&Mohanty12,  
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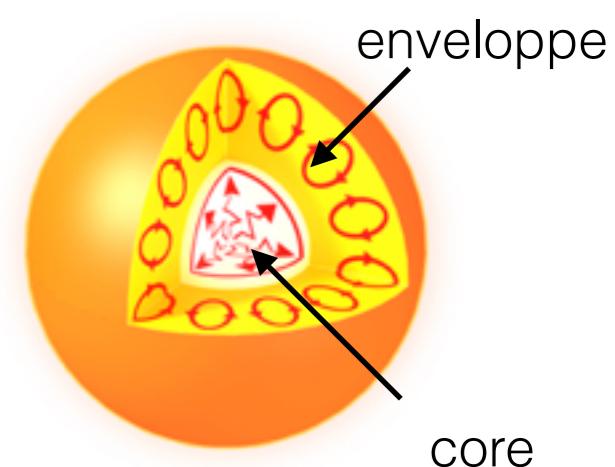
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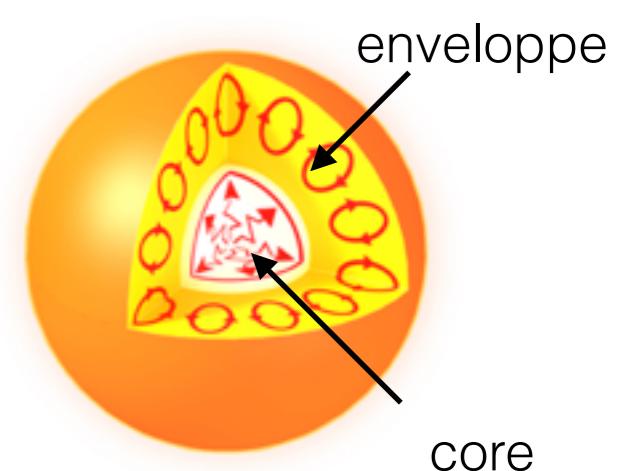
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- internal magnetic field
- internal gravity waves

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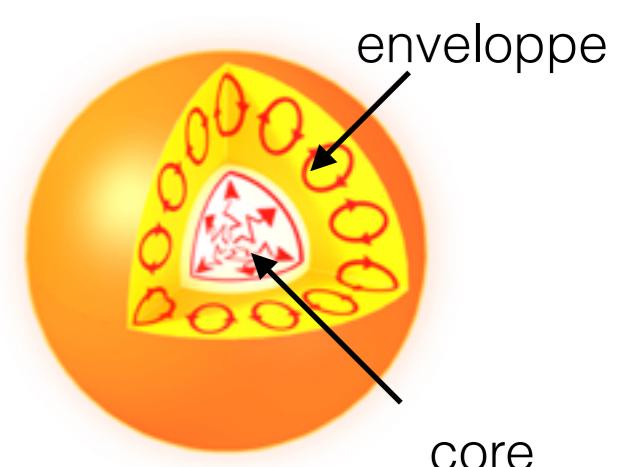
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- **Environment (extra):** Disk + Planet ?

- tidal and magnetic star-(massive) planet interaction?
- star-disk magnetic interaction?

See Matt&Pudritz08,Ogilvie&Lin13,  
Zanni&Ferreira13,Lanza&Mathis16,  
Bolmont&Mathis16,Strugarek+18,19,  
Gallet+19a,b, ...

# Modeling

Gallet & Bouvier (2013)

4 free parameters:

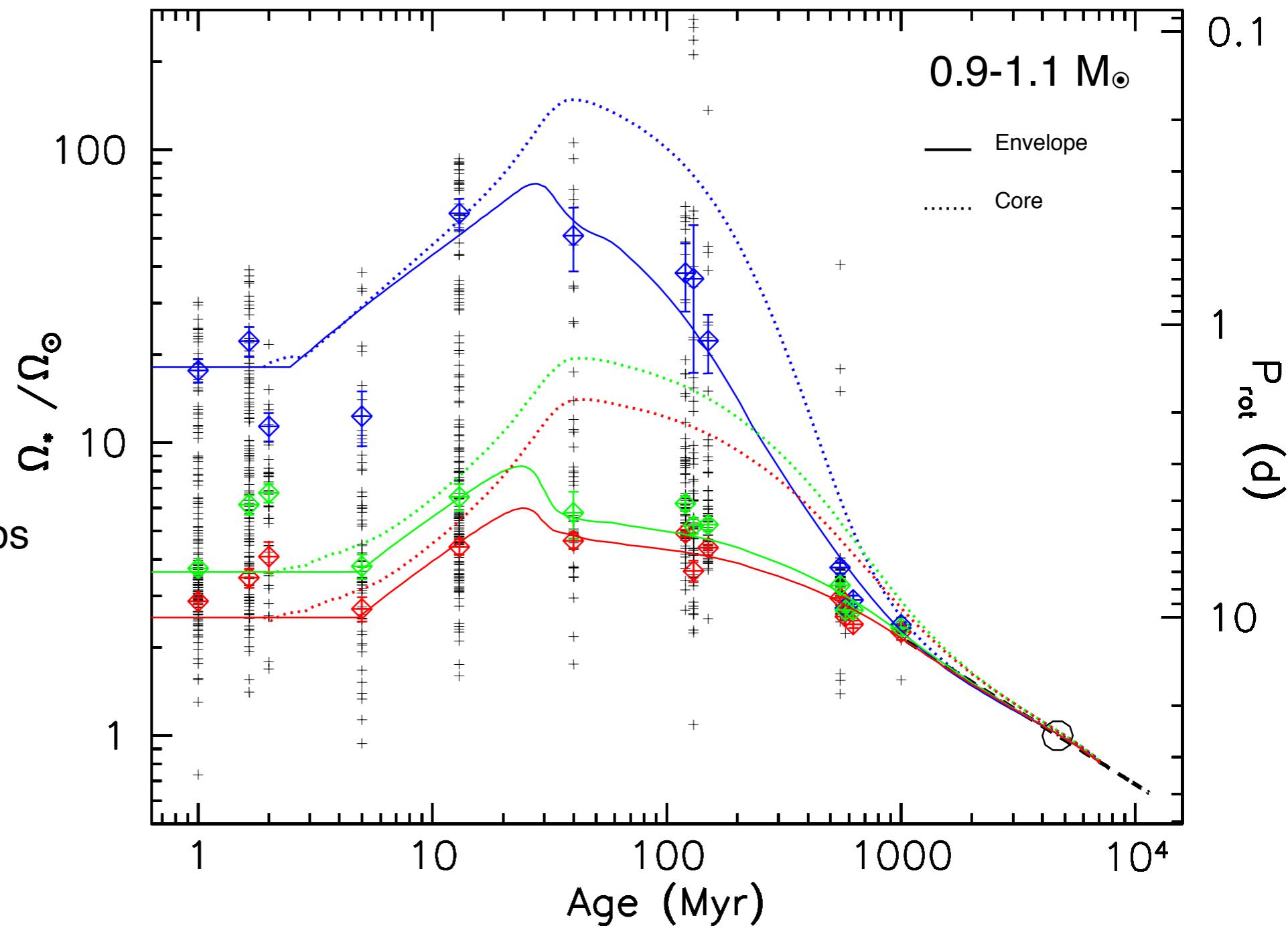
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No tidal interaction



$$r_A = K_1 \left[ \frac{B_p^2 R_*^2 (\dot{M}_{\text{wind}} v_{\text{esc}})^{-1}}{\sqrt{K_2^2 + \Omega_*^2 R_*^2 v_{\text{esc}}^{-2}}} \right]^m R_*$$

Matt et al. (2012a)

$$\Delta J = \frac{I_{\text{env}} J_{\text{core}} - I_{\text{core}} J_{\text{env}}}{I_{\text{core}} + I_{\text{env}}}$$

MacGregor & Brenner (1991)

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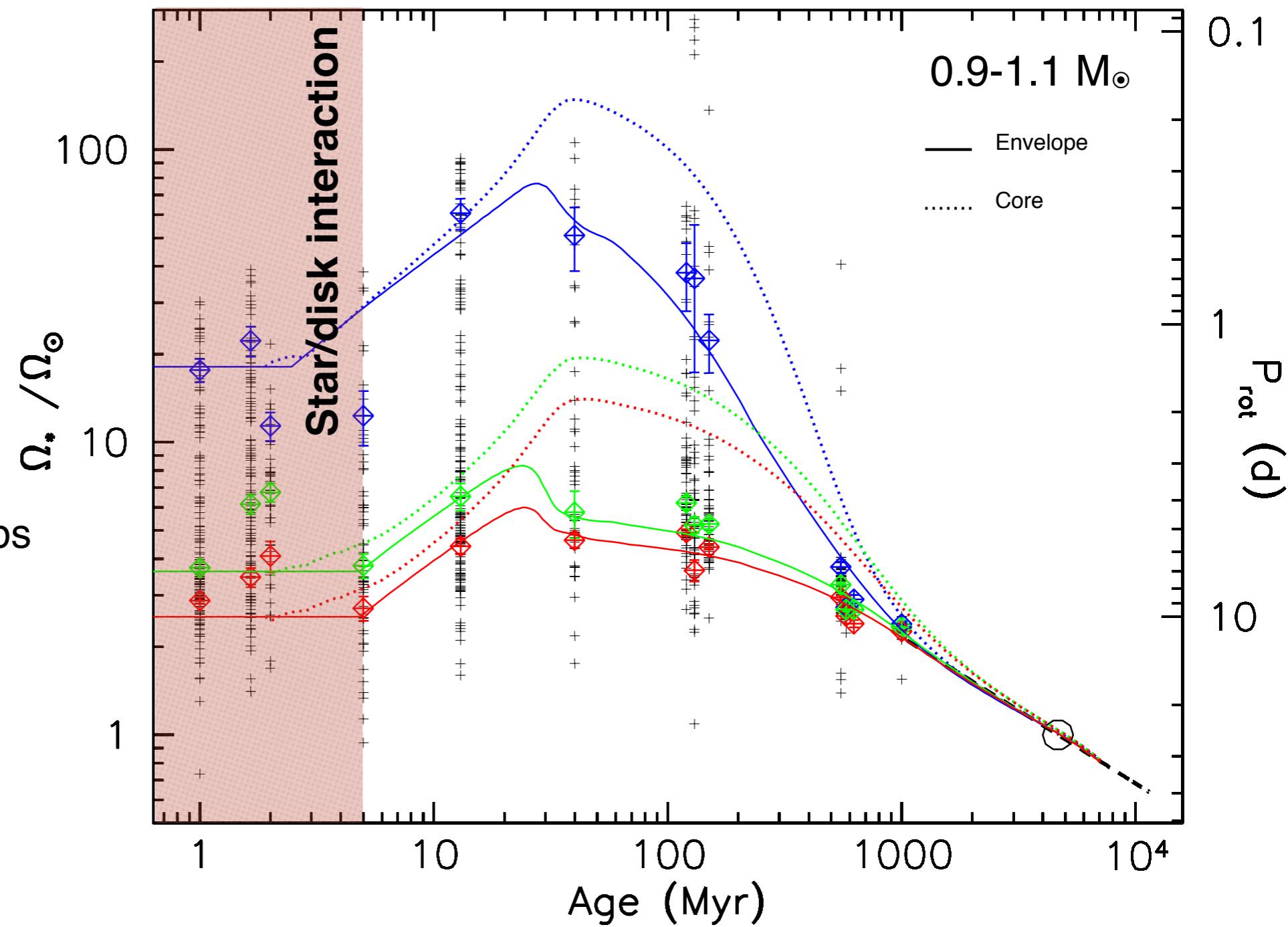
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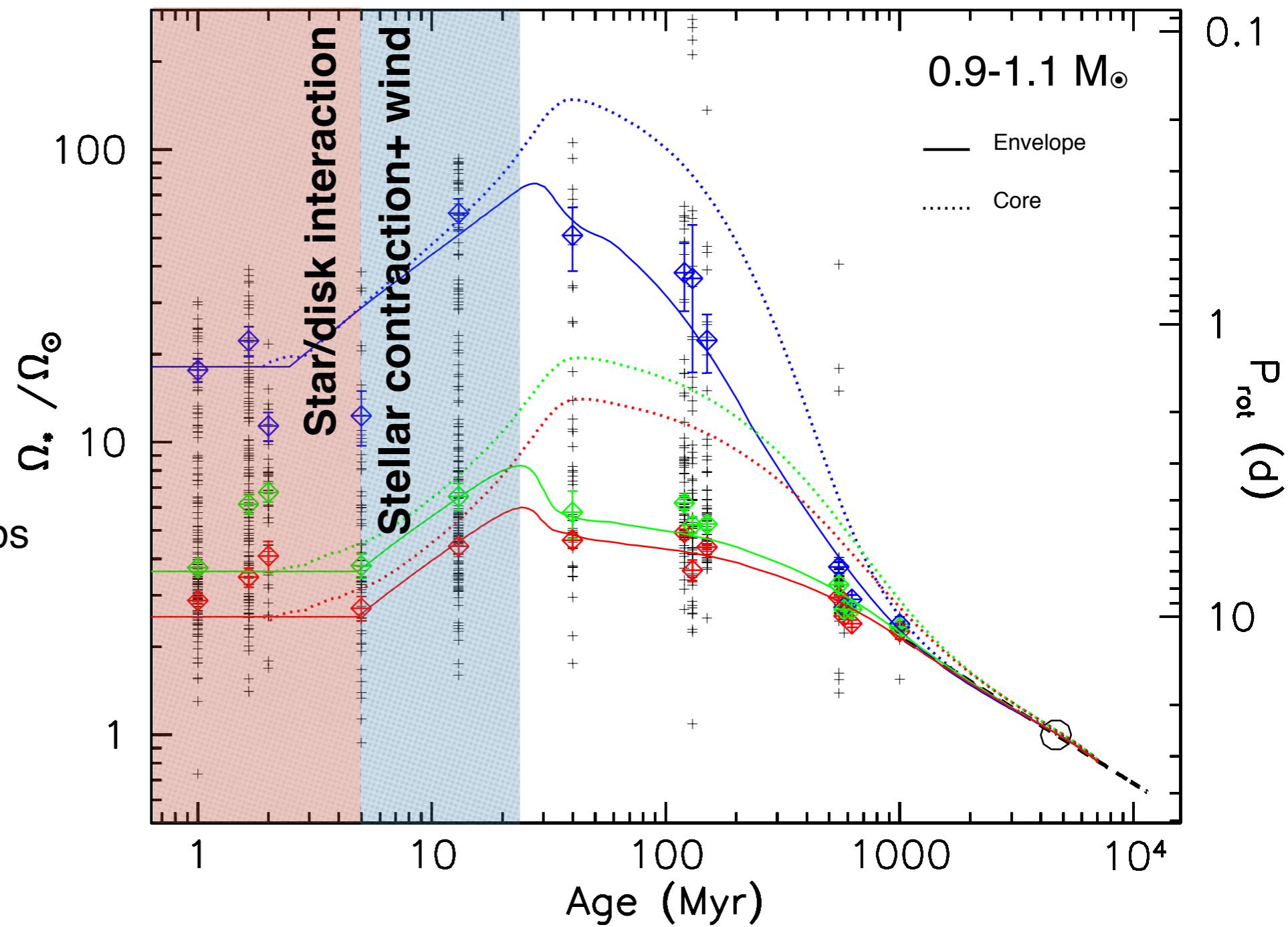
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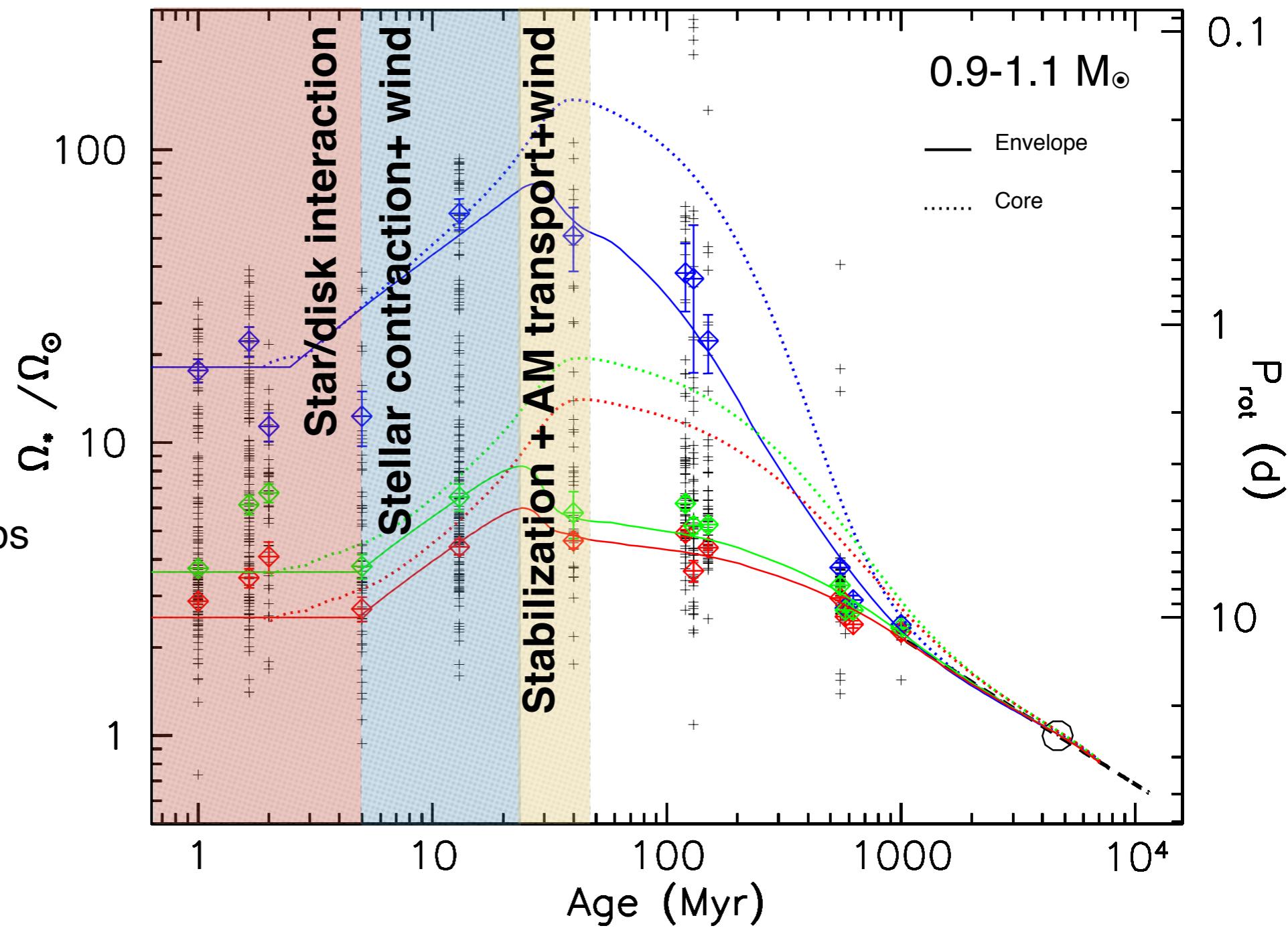
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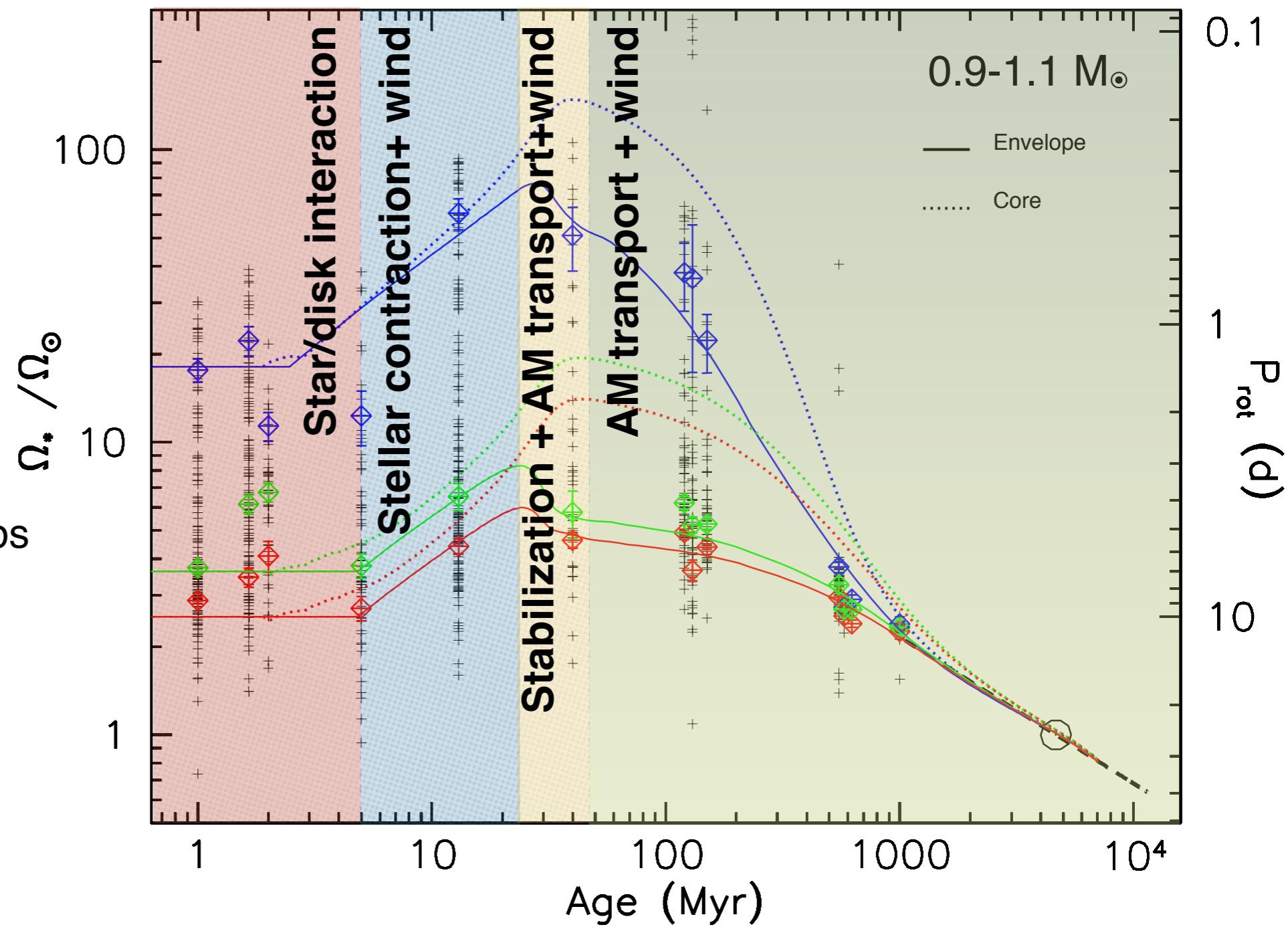
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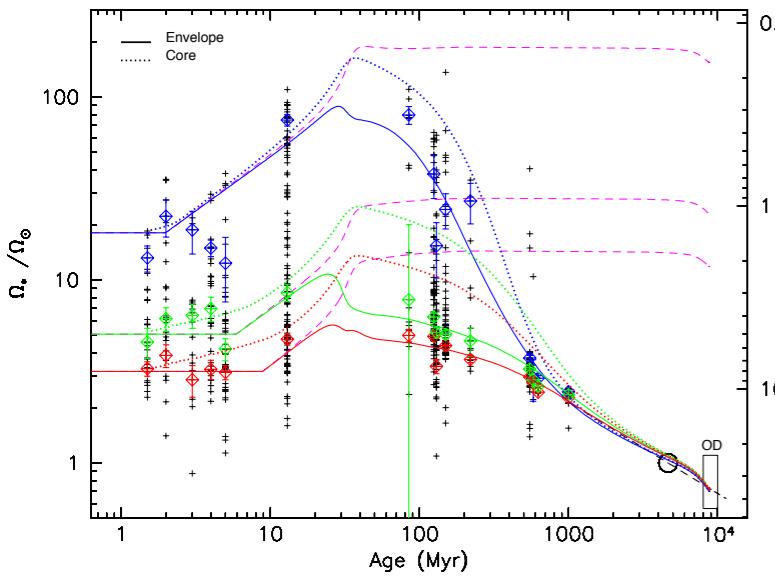
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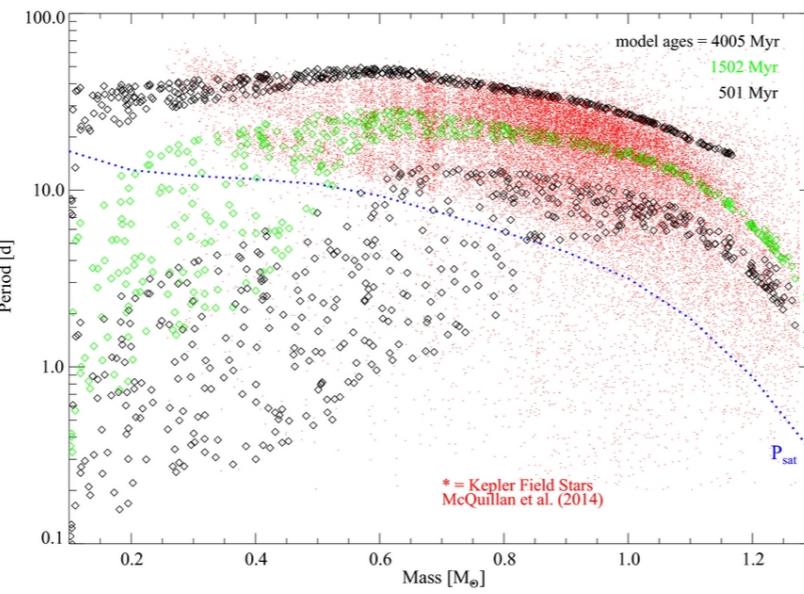
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# Models in literature

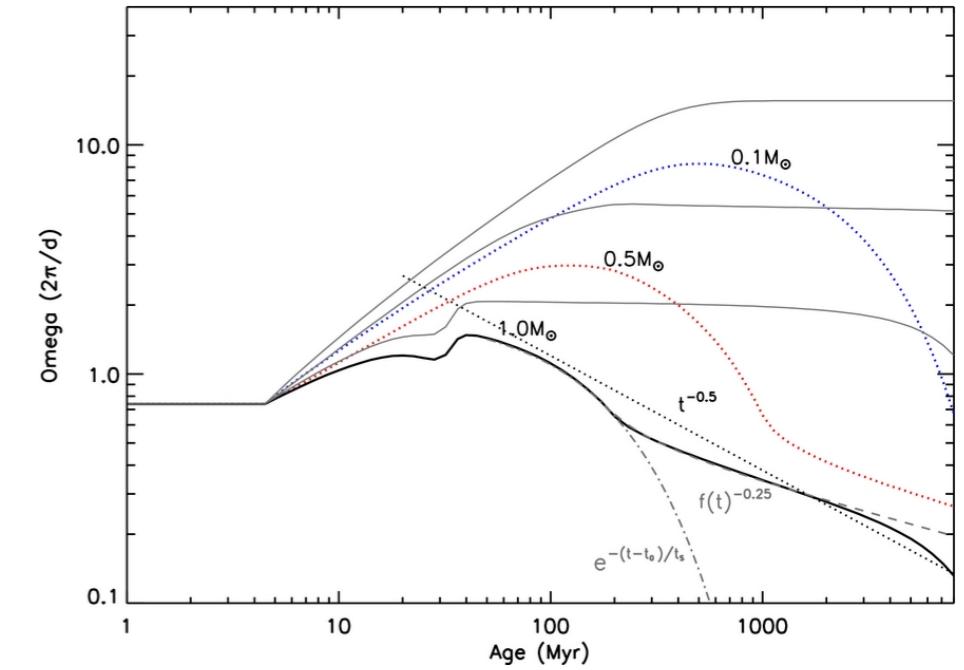
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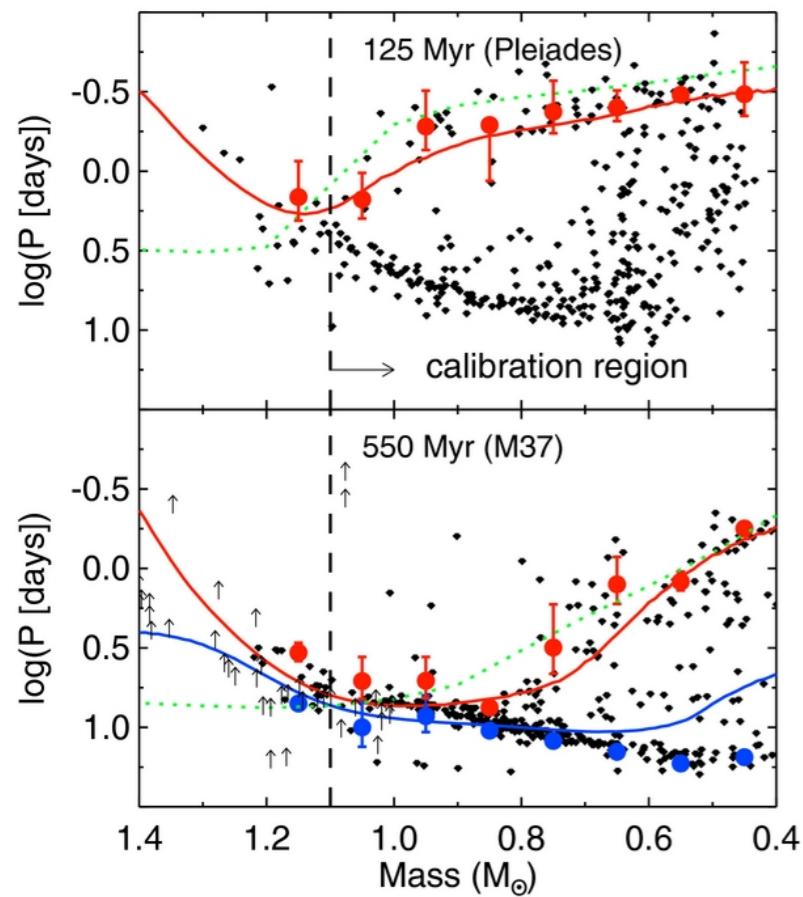
Matt+15



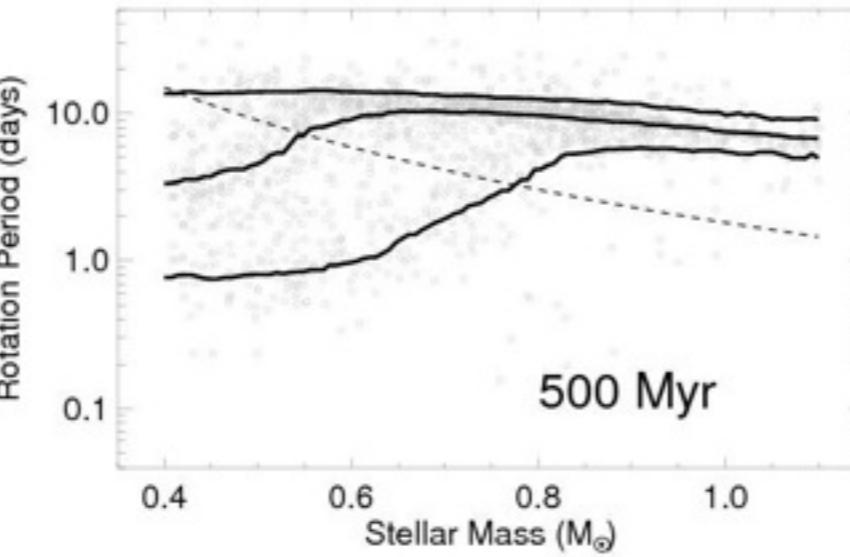
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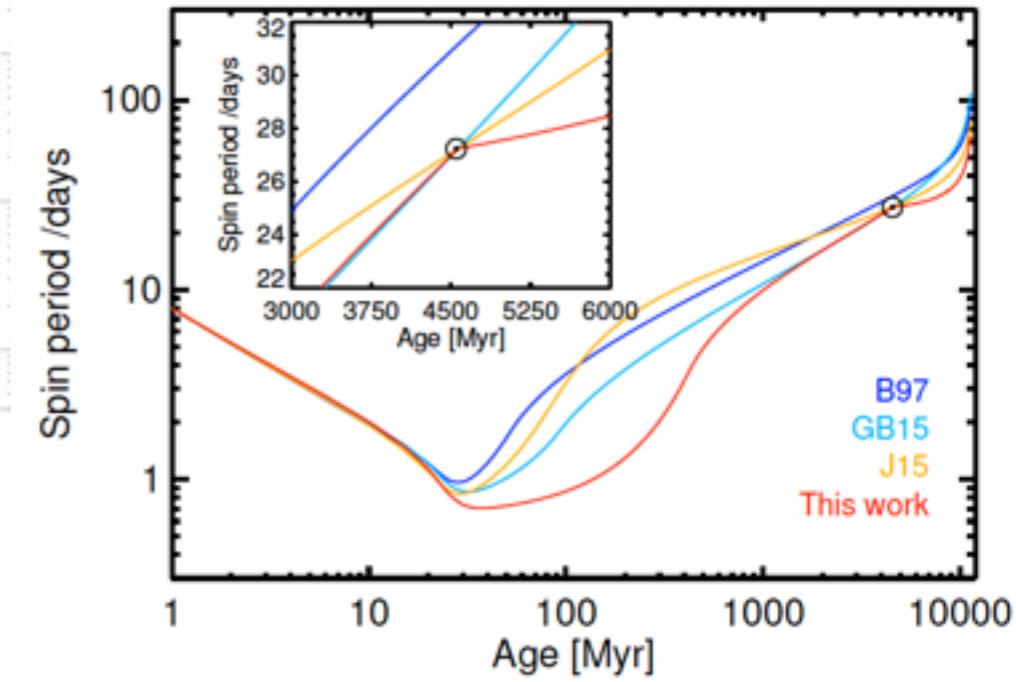
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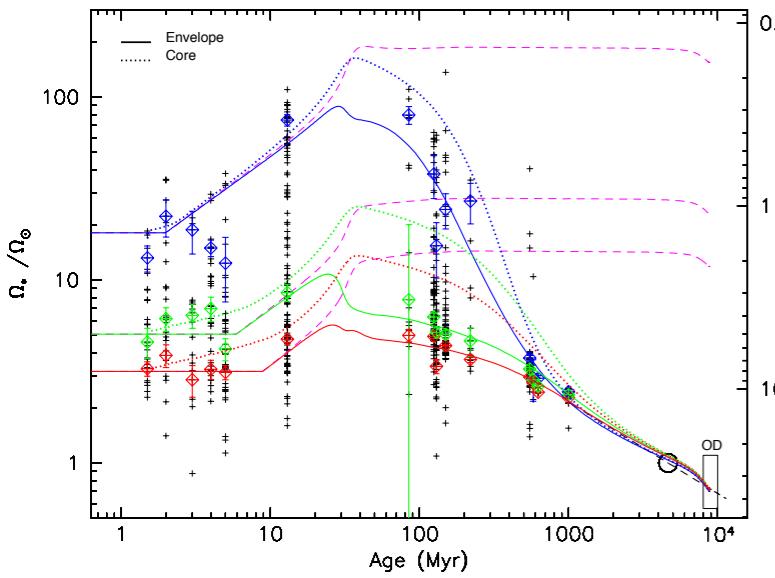


Sadeghi Ardestani+16

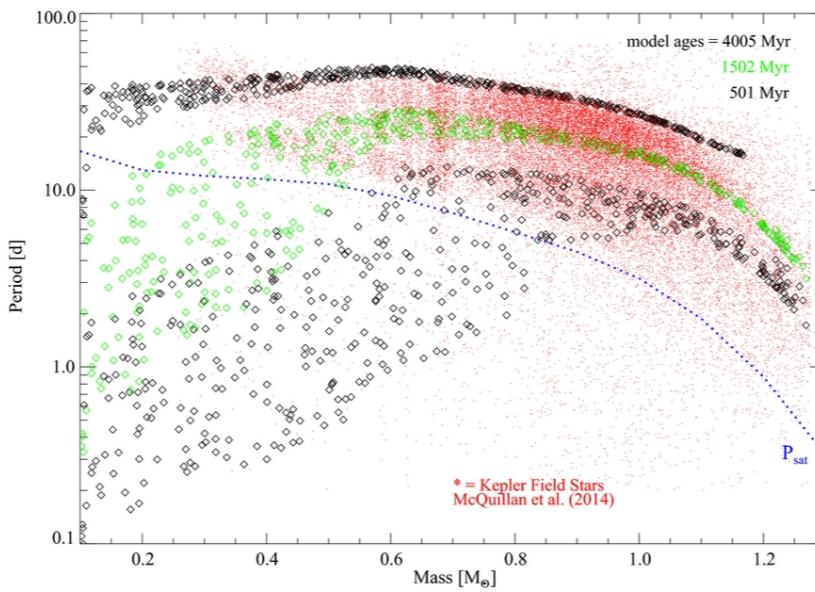


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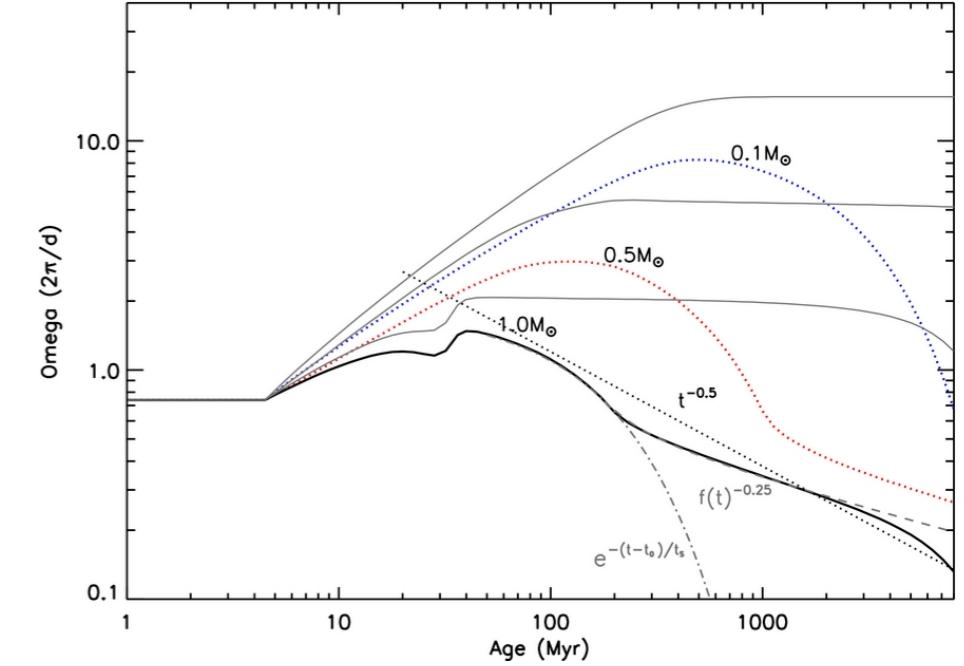
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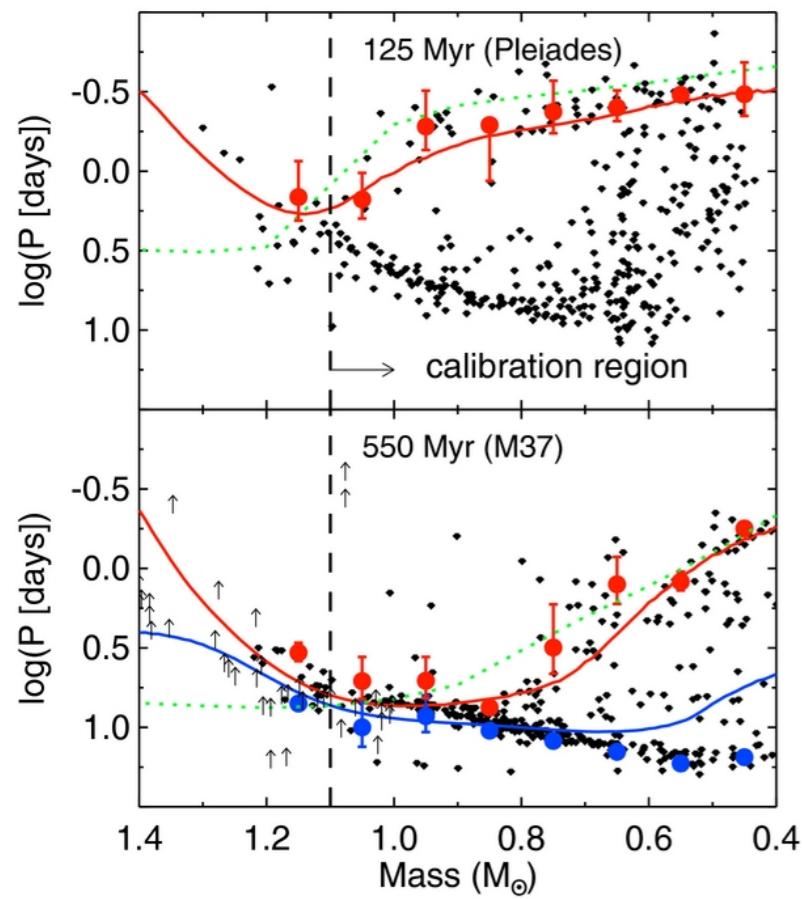
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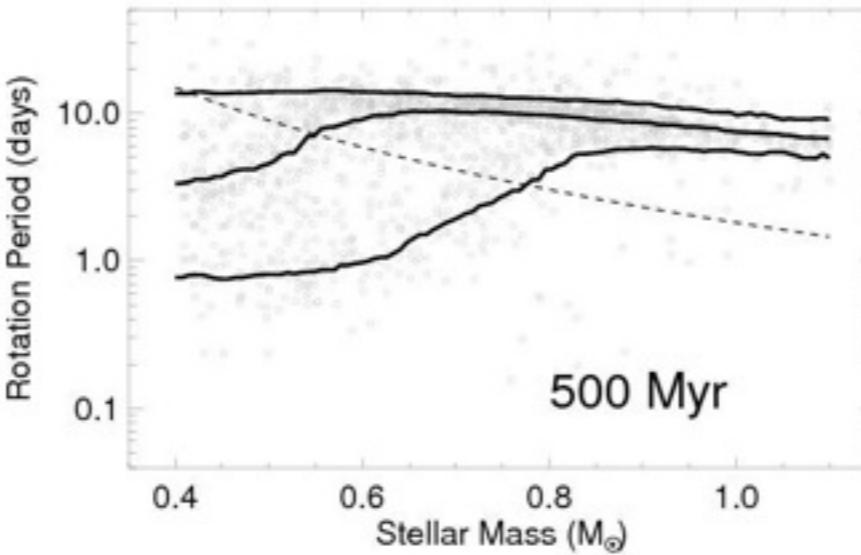
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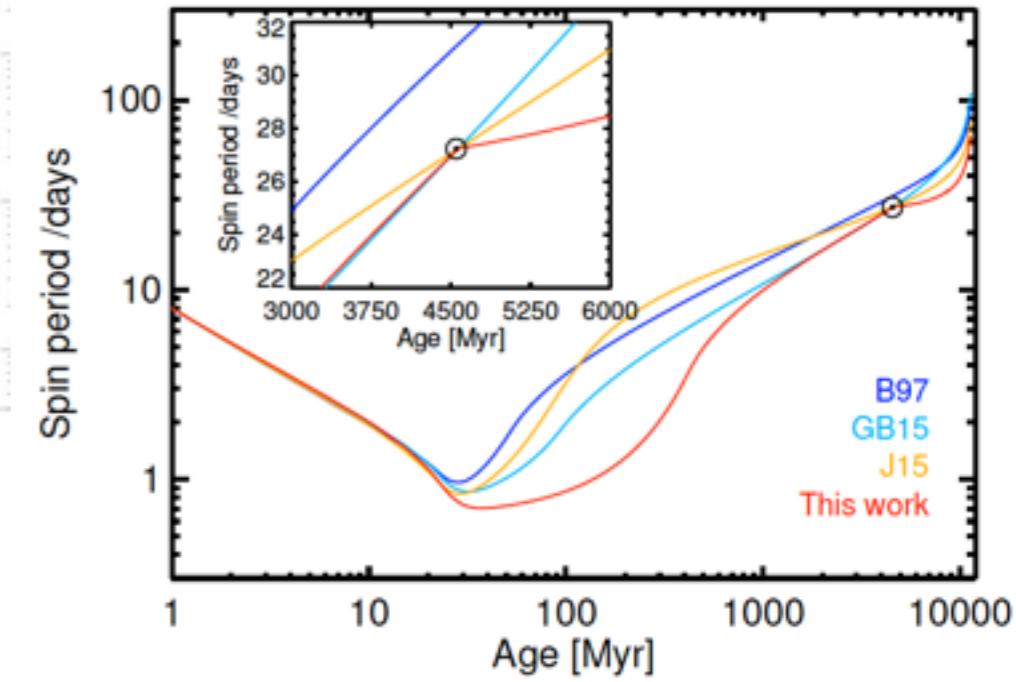
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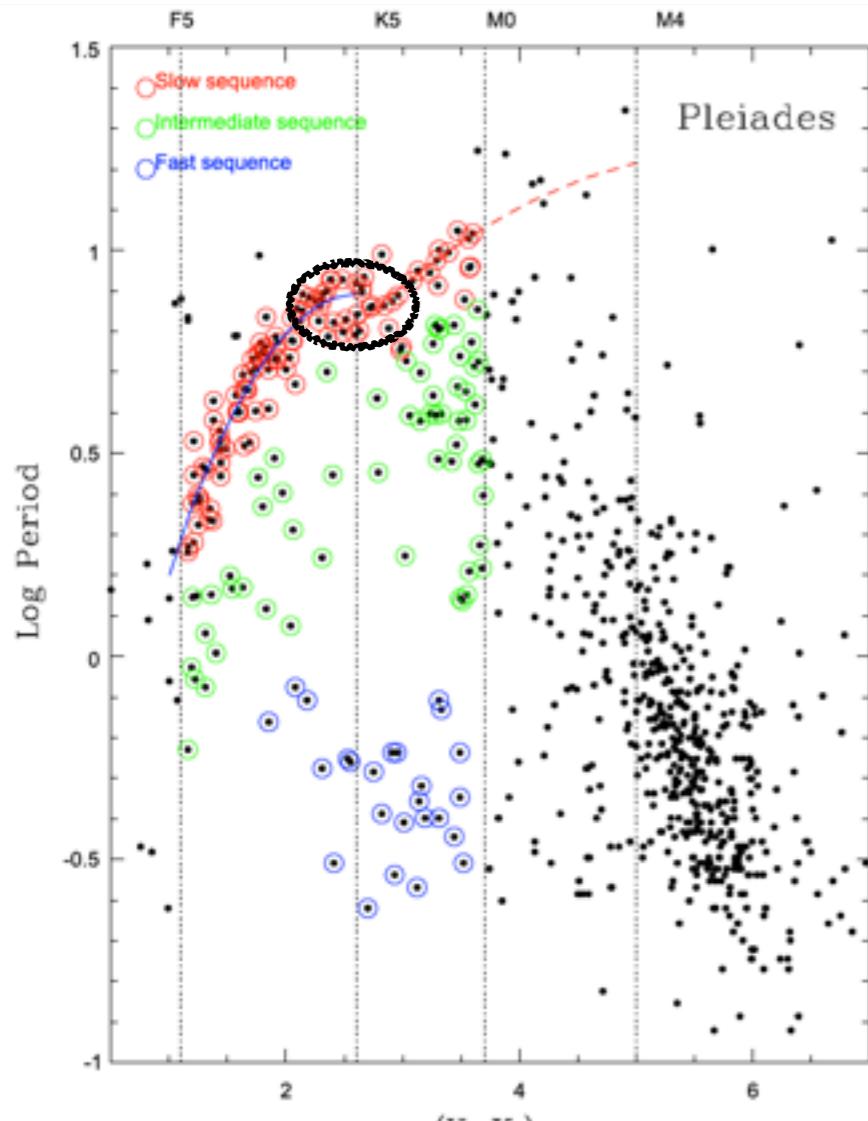
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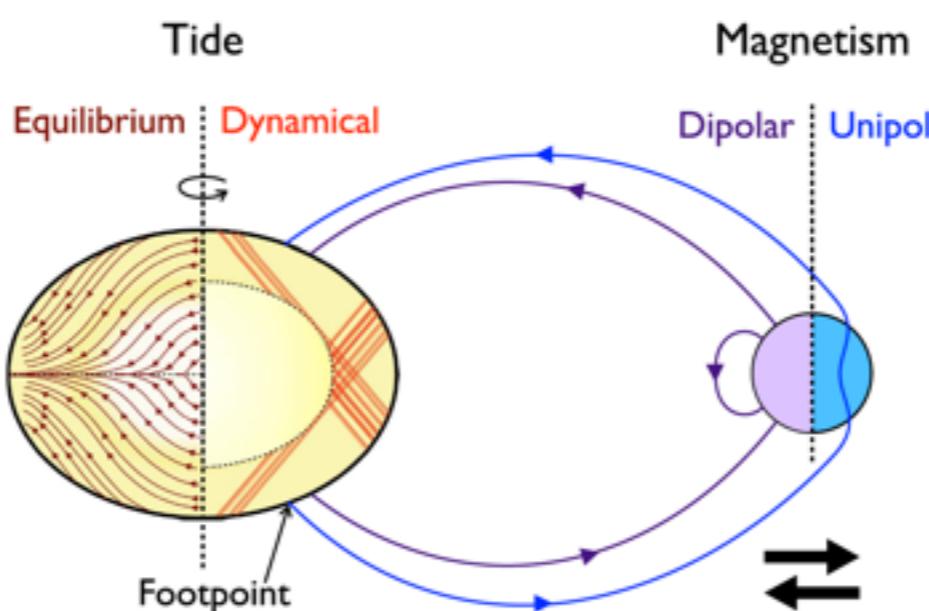
Observations quite well reproduced!

# What's next?

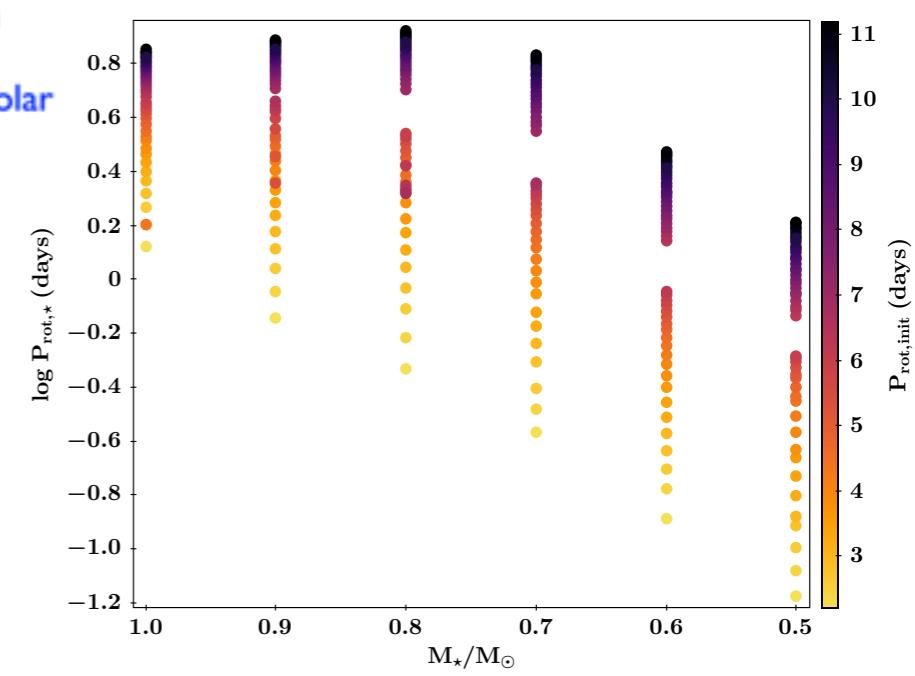
K2



Stauffer et al. (2016)



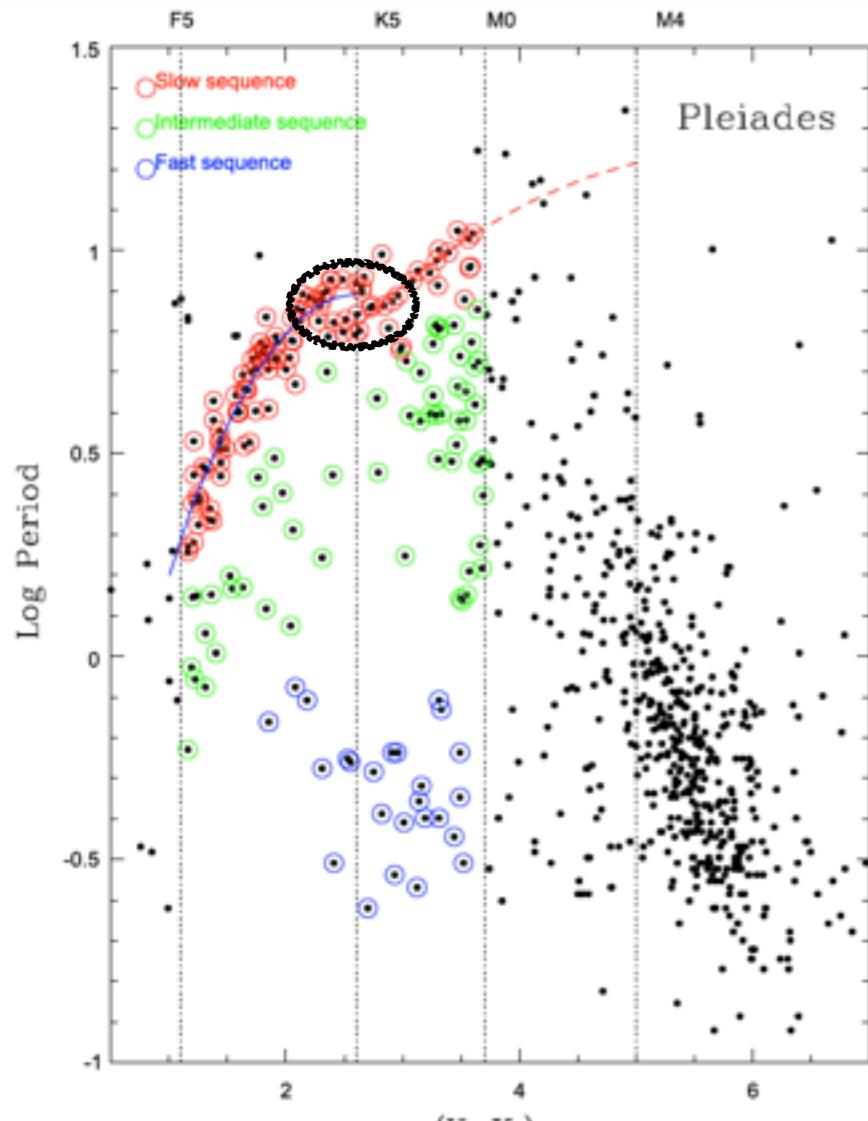
Stugarek et al. (2016)



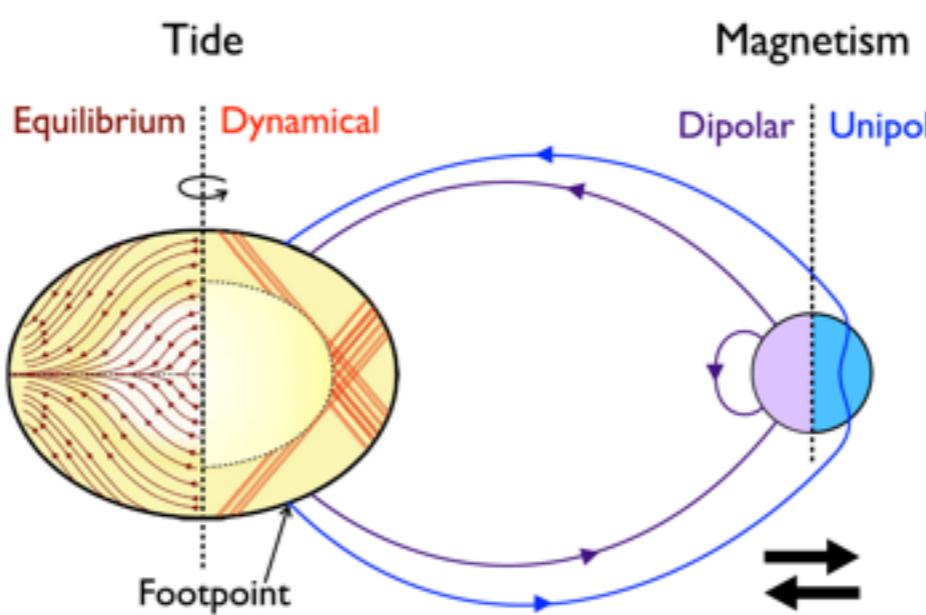
Gallet et al. (2018)

# What's next?

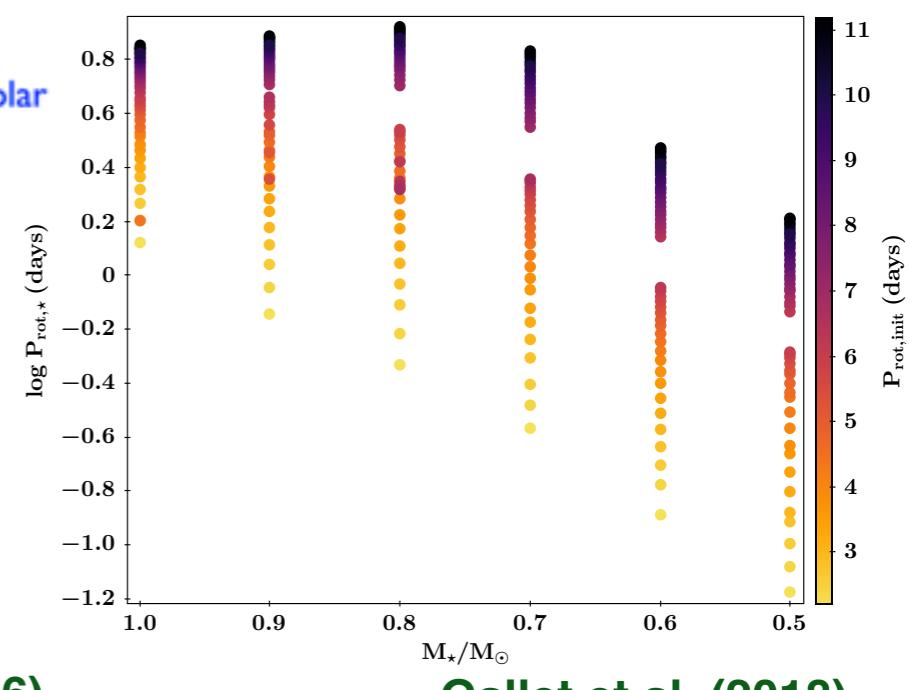
K2



Stauffer et al. (2016)



Stugarek et al. (2016)



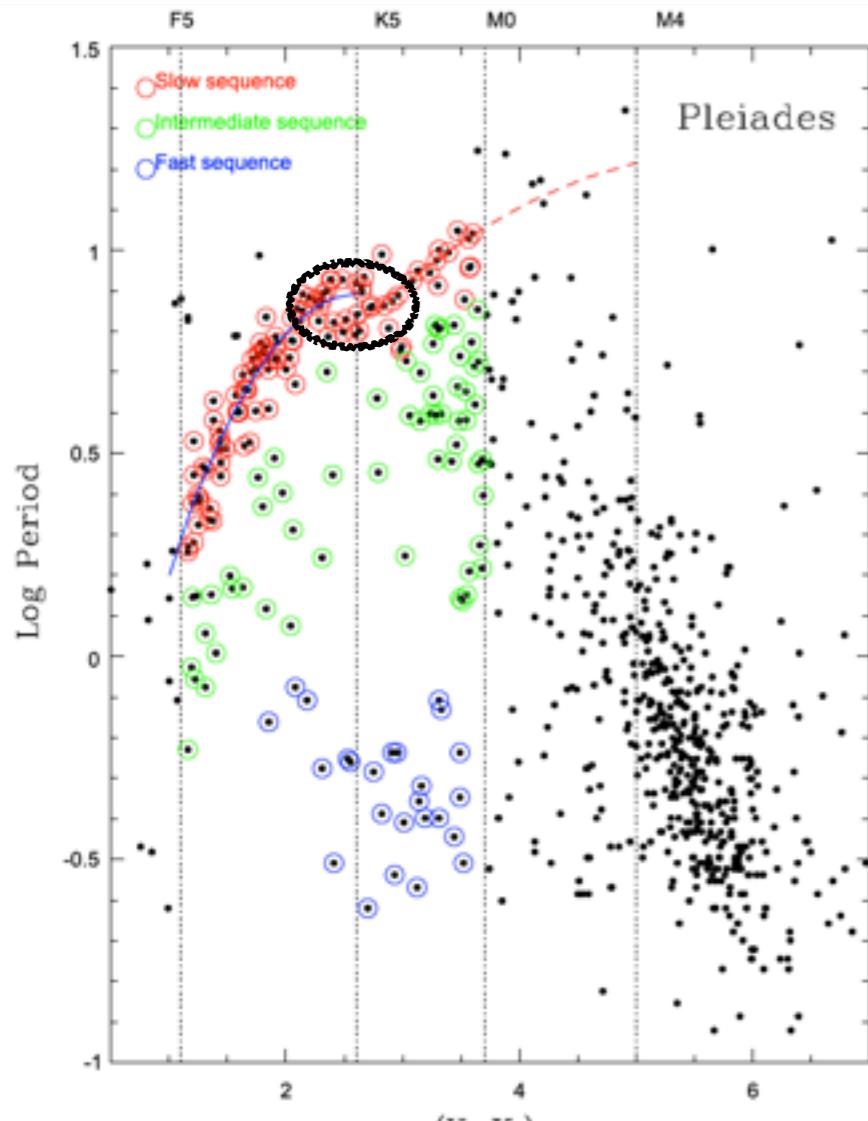
Gallet et al. (2018)

Next step in AM modeling?

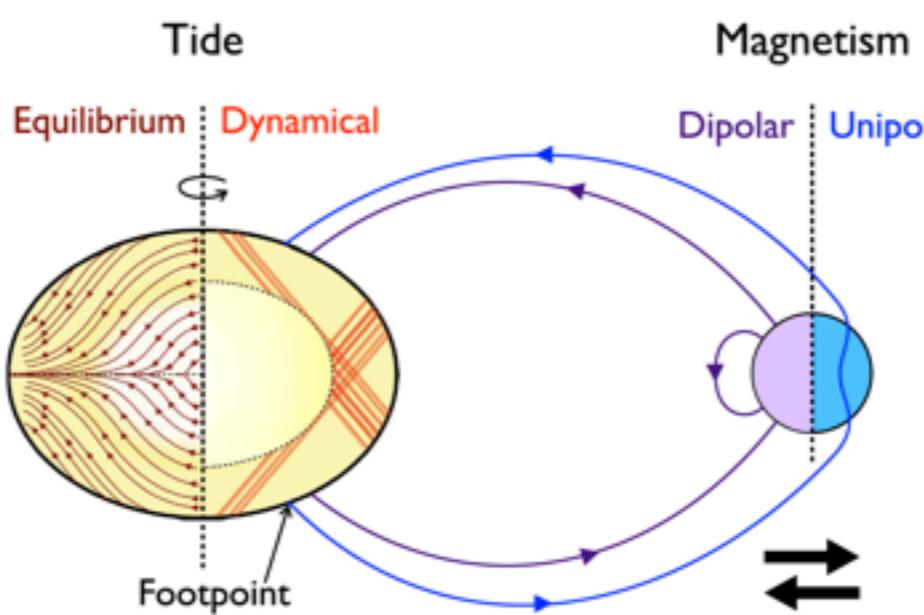
To prepare PLATO (+ Gaia DR3/DR4) data: yes!

# What's next?

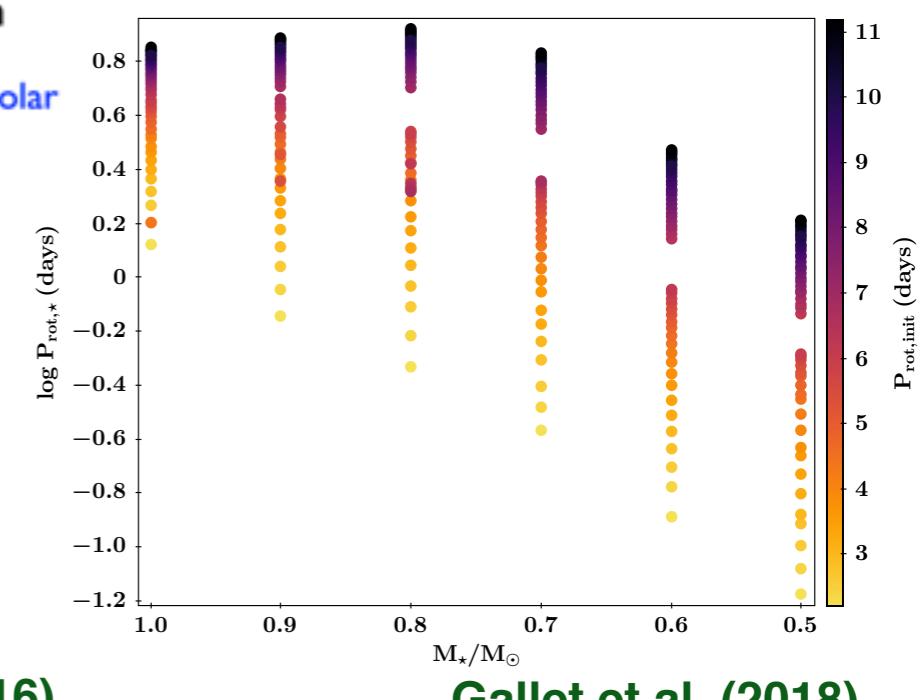
K2



Stauffer et al. (2016)



Stugarek et al. (2016)



Gallet et al. (2018)

Next step in AM modeling?

To prepare PLATO (+ Gaia DR3/DR4) data: yes!

On going work ✓

# Conclusion

## 1. Parametric models grasp the main trends of AM evolution

- fast, robust and simple: perfect for large exploration of initial conditions
- strong complementarity with stellar models
- choose model according to the mix of ingredients

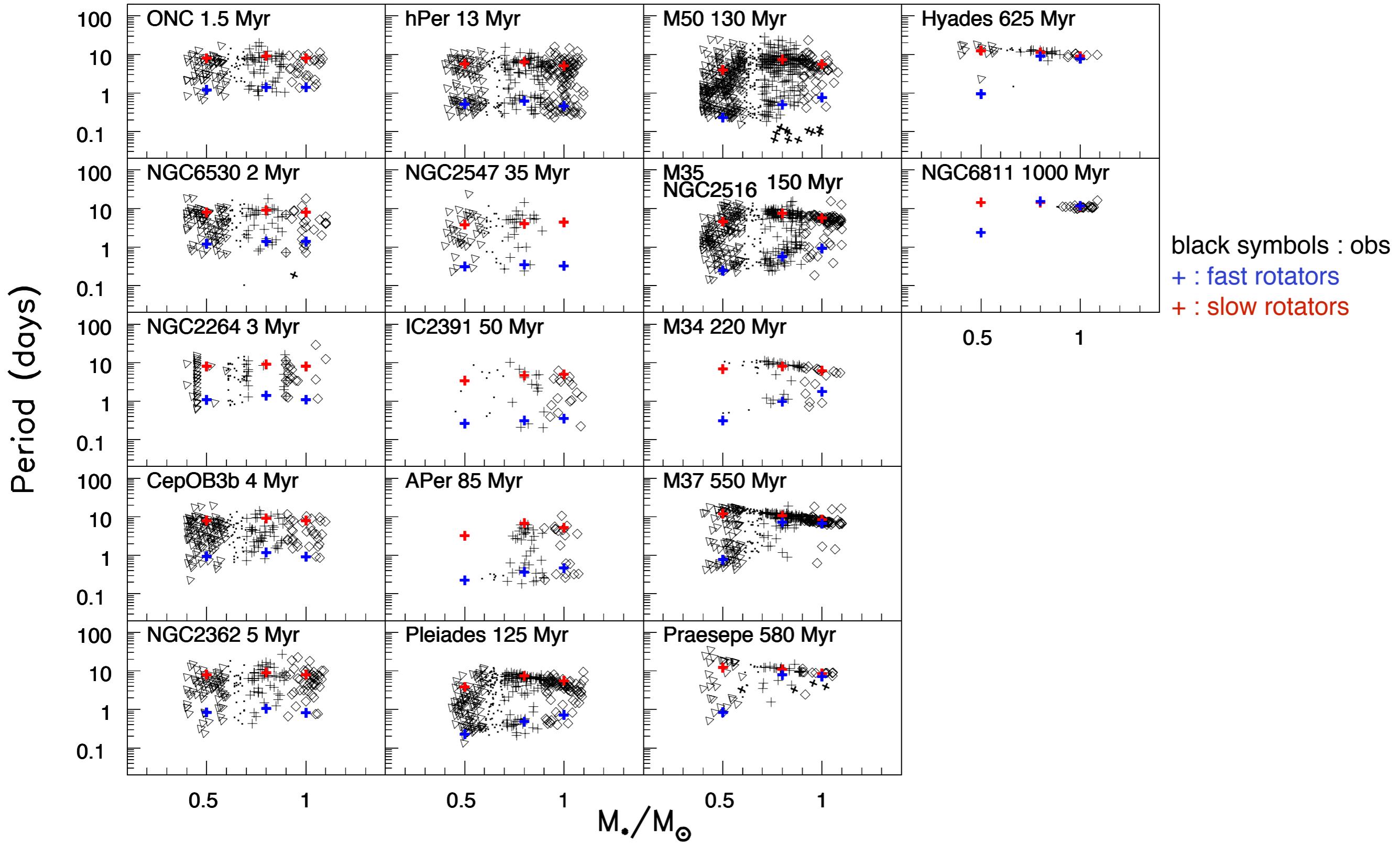
## 2. Some obs. suggest the need for an additional ingredient

- add tidal interaction (star-companion)?
- probably yes!

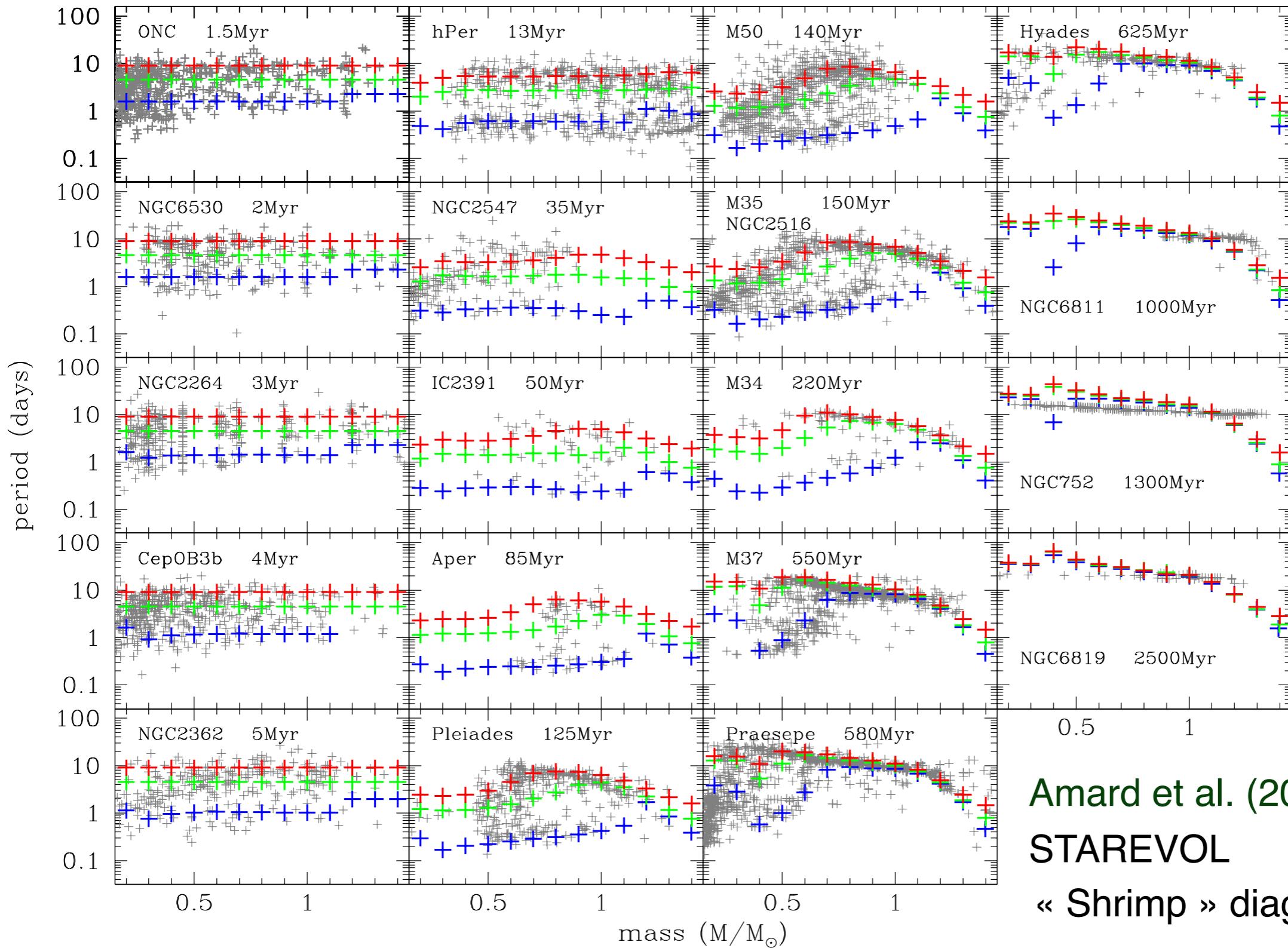
## 3. Open questions?

- star-disk interaction: what mechanism?
- magnetic braking: what quantity?
- internal transport of AM: magnetic field? internal gravity waves?

# Modeling clusters



# Modeling clusters



Amard et al. (2019)  
STAREVOL  
« Shrimp » diagram

