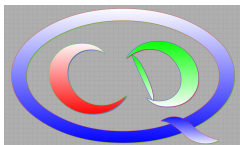


Two-pole structures in QCD: Facts, not fantasy!

Ulf-G. Meißner, Univ. Bonn & FZ Jülich

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by CAS, PIFI



by VolkswagenStiftung



by EU



CONTENTS

- Short introduction to QCD
- The story of the $\Lambda(1405)$
- Two-pole structures in the meson sector
- Amplitude analysis of $B \rightarrow D\pi\pi$
- Summary & outlook

Details in: UGM, *Symmetry* **12** (2020) 981 [2005.06909 [hep-ph]]

Short Introduction

LIMITS of QCD

- **light quarks:** $\mathcal{L}_{\text{QCD}} = \bar{q}_L i\not{D}q_L + \bar{q}_R i\not{D}q_R + \mathcal{O}(m_f/\Lambda_{\text{QCD}})$ [$f = u, d, s$]
 - L and R quarks decouple \Rightarrow chiral symmetry
 - spontaneous chiral symmetry breaking \Rightarrow pseudo-Goldstone bosons
 - pertinent EFT \Rightarrow chiral perturbation theory (CHPT)

- **heavy quarks:** $\mathcal{L}_{\text{QCD}} = \bar{Q}_f i v \cdot D Q_f + \mathcal{O}(\Lambda_{\text{QCD}}/m_f)$ [$f = c, b$]
 - independent of quark spin and flavor
 - \Rightarrow SU(2) spin and SU(2) flavor symmetries (HQSS and HQFS)
 - pertinent EFT \Rightarrow heavy quark effective field theory (HQEFT)

- **heavy-light systems:**
 - heavy quarks act as matter fields coupled to light pions
 - combine CHPT and HQEFT

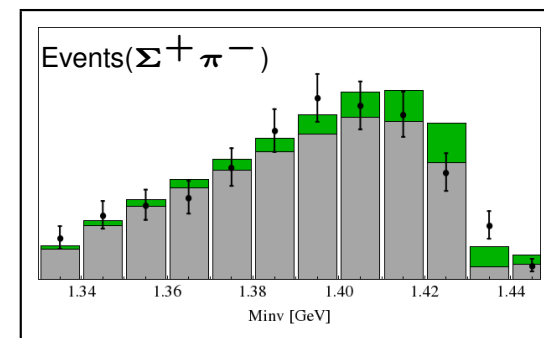
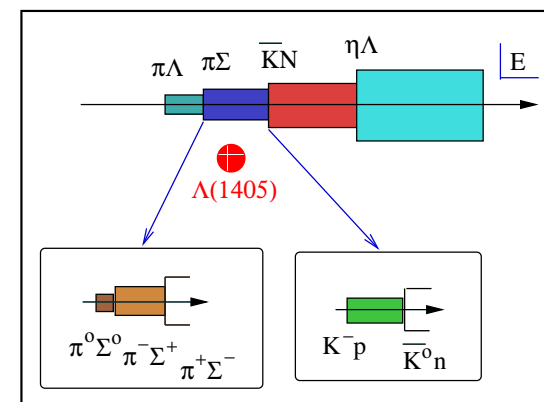
The story of the $\Lambda(1405)$

BASICS of the $\Lambda(1405)$

- Quark model: uds excitation with $J^P = \frac{1}{2}^-$,
a few hundred MeV above the $\Lambda(1116)$
 $m = 1405.1_{-1.0}^{+1.3}$ MeV, $\Gamma = 50.5 \pm 2.0$ MeV [PDG 2019]
- Prediction as early as 1959 by Dalitz and Tuan:
Resonance between the coupled $\pi\Sigma$ and $\bar{K}N$ channels
Dalitz, Tuan, Phys. Rev. Lett. **2** (1959) 425; J.K. Kim, PRL **14** (1965) 29
- Clearly seen in $K^-p \rightarrow \Sigma 3\pi$ reactions at 4.2 GeV at CERN
Hemingway, Nucl.Phys. B **253** (1985) 742
- An enigma: Too low in mass for the quark model,
but well described in models (hadron exchanges, cloudy bags, ...)
- Problems:

★ models are uncontrolled (theory like experiment **must** have errors!)

★ connections to QCD?



many authors incl. some in the audience

CHIRAL SU(3) DYNAMICS: A NEW TWIST

- Re-analysis of coupled-channel K^-p scattering and the $\Lambda(1405)$

Oller, UGM Phys. Lett. B **500** (2001) 263

- Technical improvements:

- Subtracted meson-baryon loop with dim reg \leftrightarrow **standard method**
- Coupled-channel approach to the $\pi\Sigma$ mass distribution
- Matching formulas to any order in chiral perturbation theory established

- Most significant finding:

“Note that the $\Lambda(1405)$ resonance is described by **two poles** on sheets II and III with rather different imaginary parts indicating a clear departure from the Breit-Wigner situation...”

[pole 1: (1379.2 -i 27.6) MeV, pole 2: (1433.7 -i 11.0) MeV on RS II]

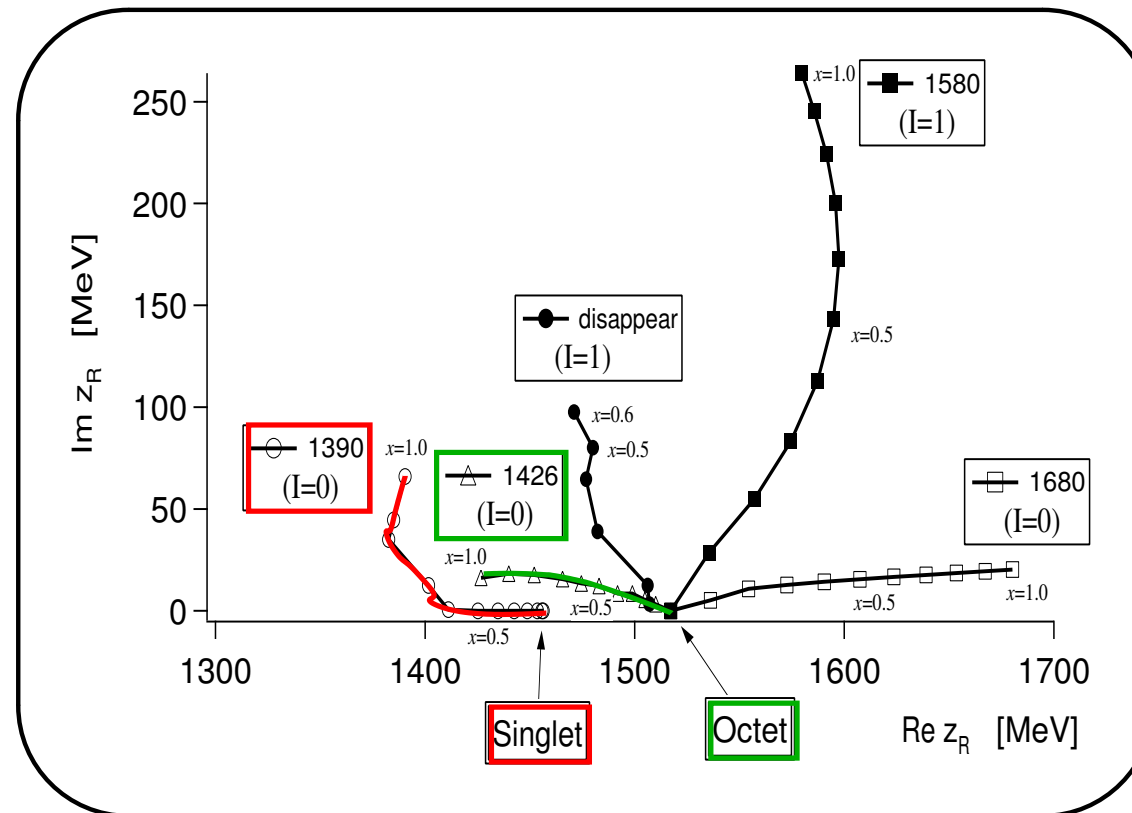
- Scrutinized through further calculations & group theory arguments 2 years later

Jido, Oller, Oset, Ramos, UGM, Nucl. Phys. A **725** (2003) 181

SU(3) SYMMETRY CONSIDERATIONS

- Group theory: $8 \otimes 8 = \underbrace{1 \oplus 8_s \oplus 8_a}_{\text{binding at LO}} \oplus 10 \oplus \overline{10} \oplus 27$

- Follow the pole movement from the SU(3) limit to the physical masses:



INCLUDING KAONIC ATOM DATA

- Improved calculation with all NLO terms and constraints from kaonic hydrogen using precise theory for kaonic atoms based on NREFT

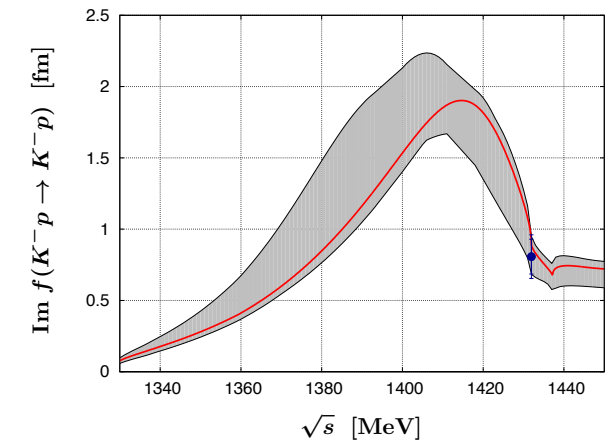
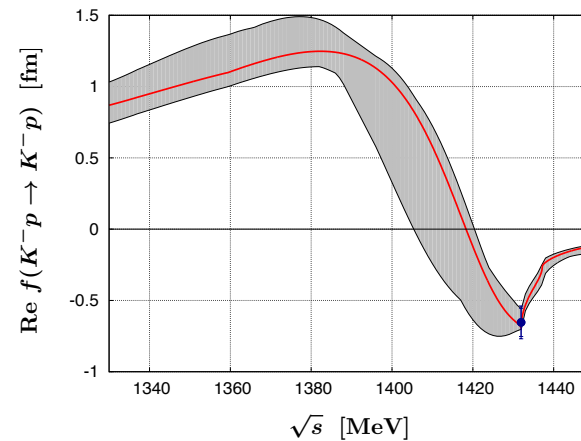
Ikeda, Hyodo, Weise, Nucl. Phys. A **881** (2012) 98

UGM, Raha, Rusetsky, Eur. Phys. J. C **35** (2004) 349

→ Precise proton amplitudes

→ Predictions for neutron amps.

● M. Bazzi *et al.* [SIDDHARTA Collaboration],
Phys. Lett. B **704** (2011) 113

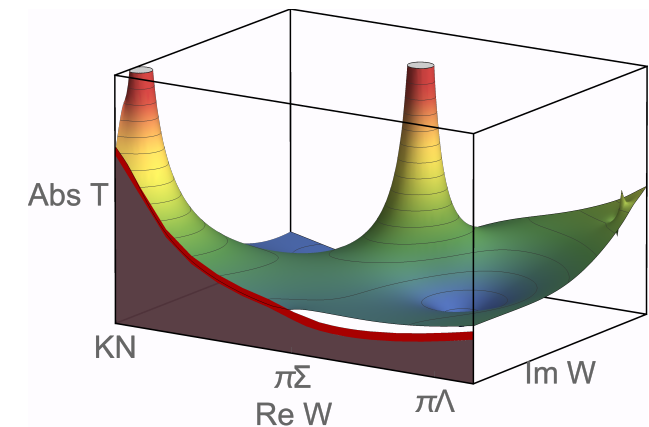


- Similar developments by the Bonn & Murcia groups

Mai, UGM, Nucl. Phys. A **900** (2013) 51

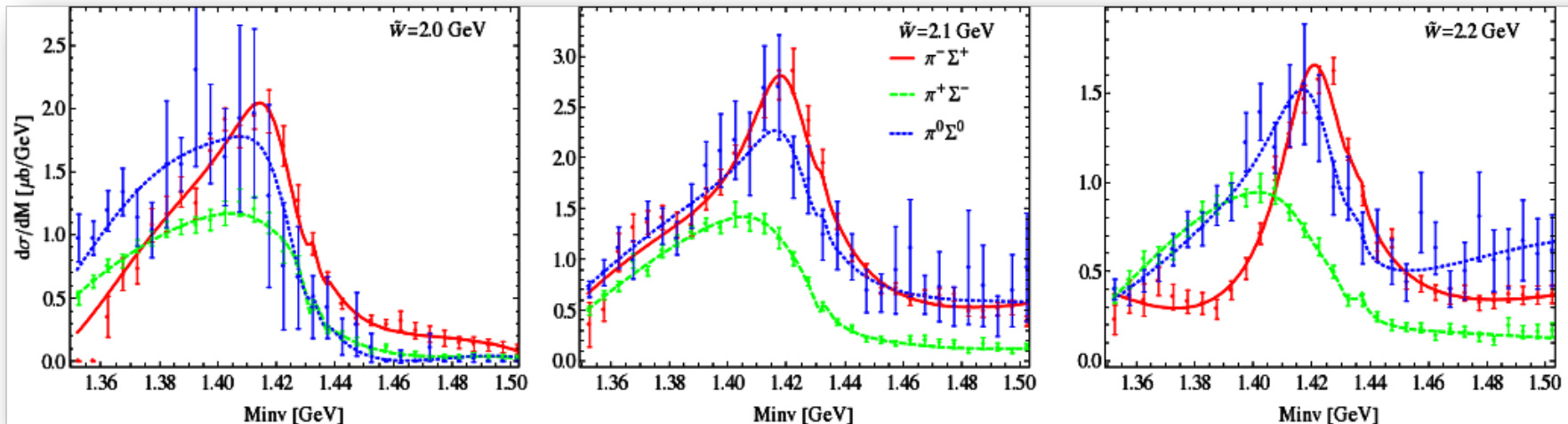
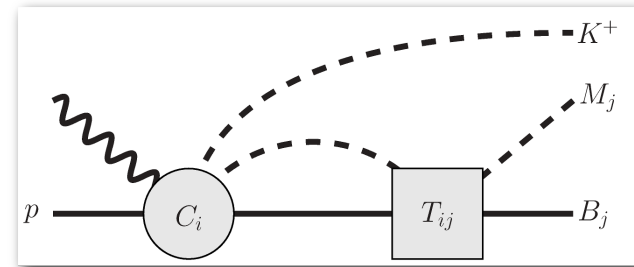
Oller, Guo, Phys. Rev. C **87** (2013) 035202

↪ Confirms two-pole structure

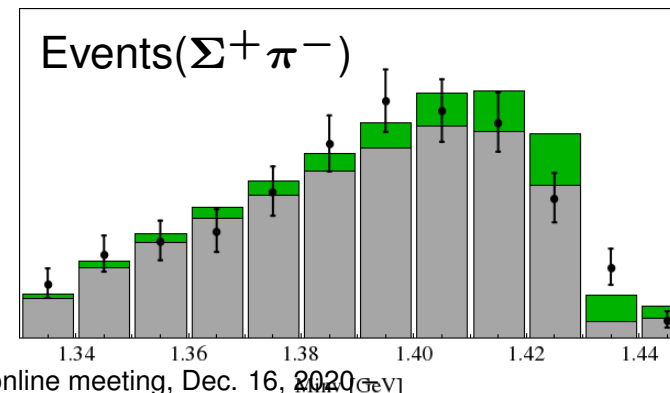


INCLUDING PHOTOPRODUCTION DATA

- Simple model for $\gamma p \rightarrow K^+ \Sigma \pi \rightarrow$ CLAS data
 CLAS, Phys. Rev. C 87, 035206 (2013)
 Roca, Oset, Phys. Rev. C 87, 055201 (2013)
- CLAS data prefer solution 4

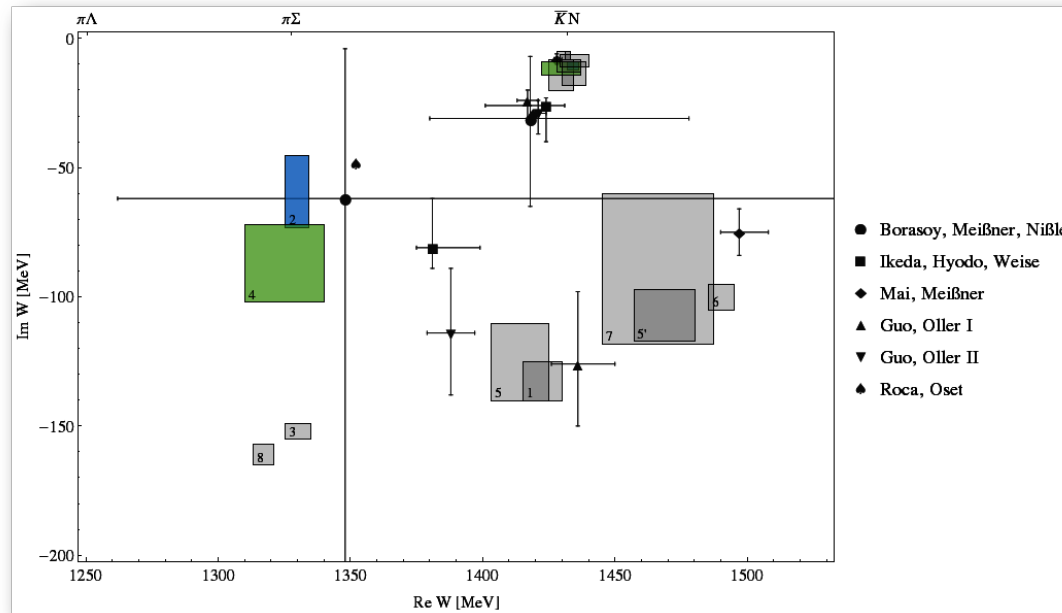


- also good description of $\Sigma^+ \pi^-$ distribution from $K^- p \rightarrow \Sigma^+ \pi^- \pi^+ \pi^-$ (not fitted)
- solution 2 also acceptable



STATUS of the TWO-POLE SCENARIO

- Two poles from scattering plus CLAS data:



→ PDG 2016: <http://pdg.lbl.gov/2015/reviews/rpp2015-rev-lam-1405-pole-struct.pdf>

POLE STRUCTURE OF THE $\Lambda(1405)$ REGION
Written November 2015 by Ulf-G. Meißner and Tetsuo Hyodo

→ return to the RPP in the summary!

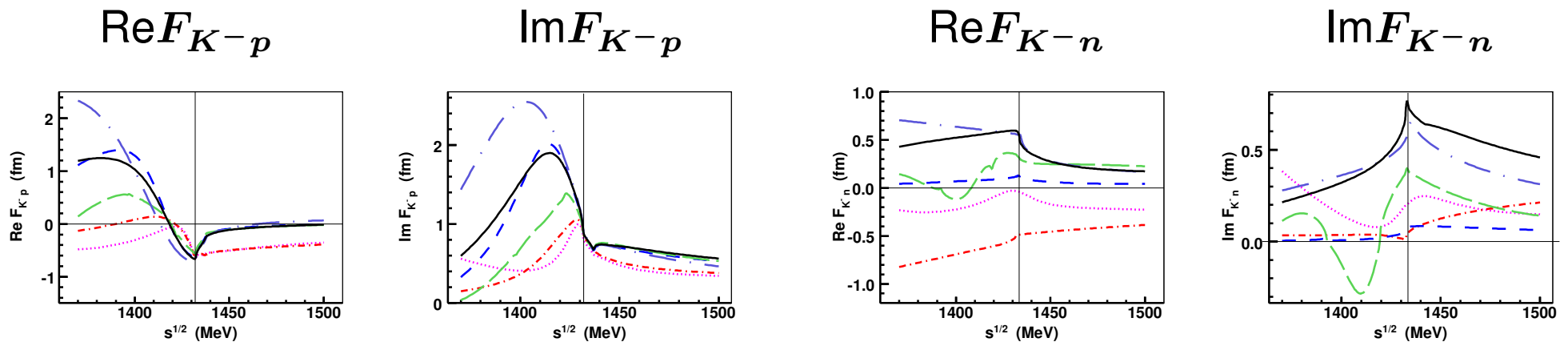
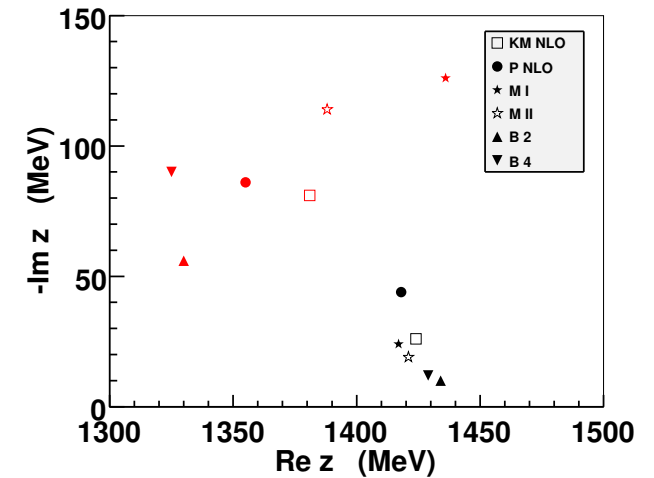
OPEN ENDS

- The story is not yet told to the end:

Consider various NLO approaches

- ★ precise location of the lighter pole
- ★ subthreshold amp's not yet well determined

Cieply, Mai, UGM, Smejkal, Nucl. Phys. A **954** (2016) 17



Kyoto-Munich **Bonn 2** **Bonn 4** **Murcia 1** **Murcia 2** — • — Prague

Prague: Cieply, Smejkal, Nucl. Phys. A **881** (2012) 115

INCLUDING P-WAVES

- First UCHPT calc. with S- and P-waves & fitting to differential XS data

- Various tests of the scattering amp:

↪ $\pi\Sigma$ inv. mass. distribution ✓

↪ CLAS photoproduction data ✓

↪ multiple fits w/ constraints on the LECs

- Two-pole scenario again validated

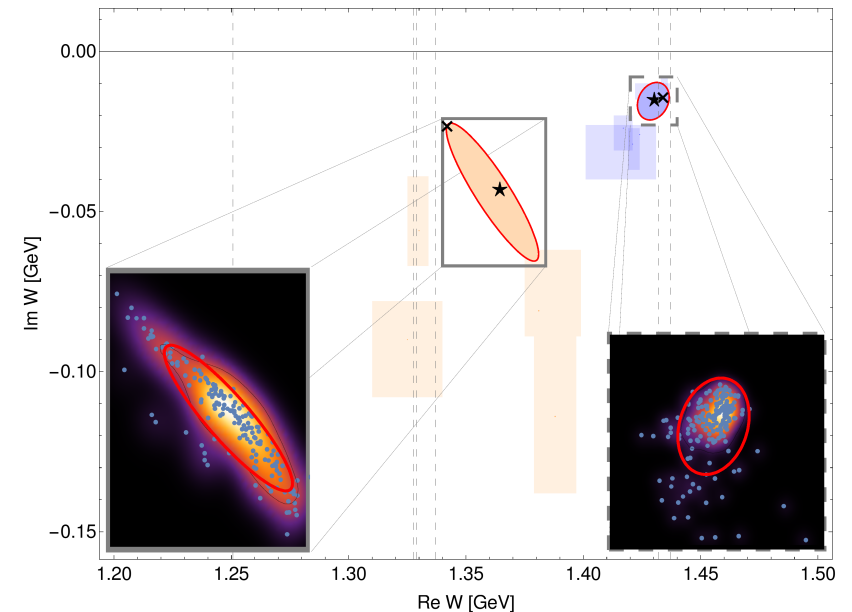
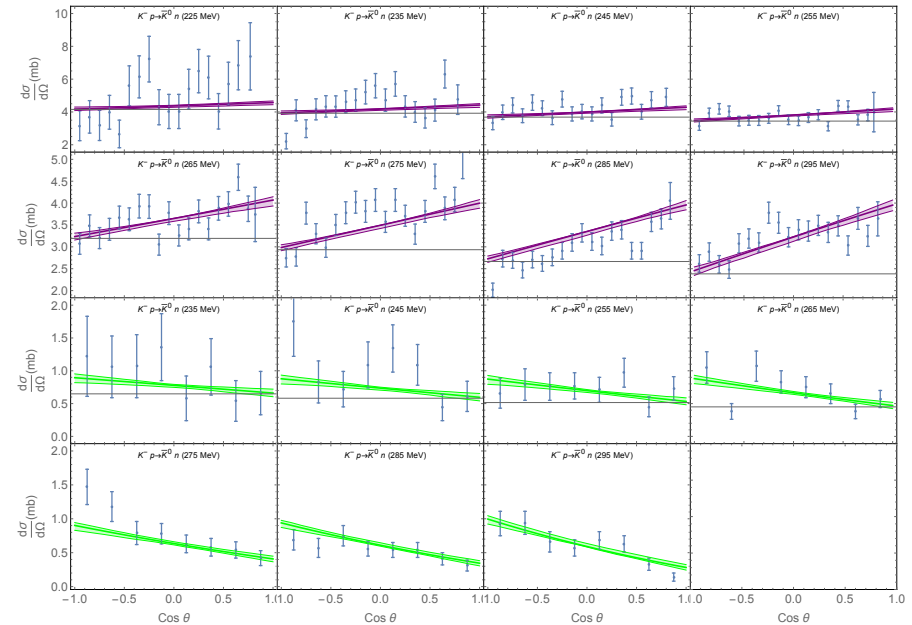
pole I: $(1430(5) - i15(4))$ MeV

pole II: $(1360(13) - i43(14))$ MeV

Sadavasian, Mai, Döring, Phys. Lett. B789 (2019) 329

- Update of the two-pole plot available

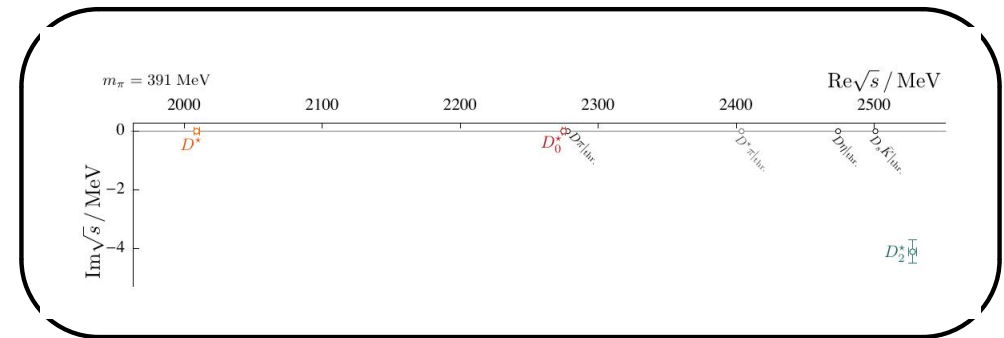
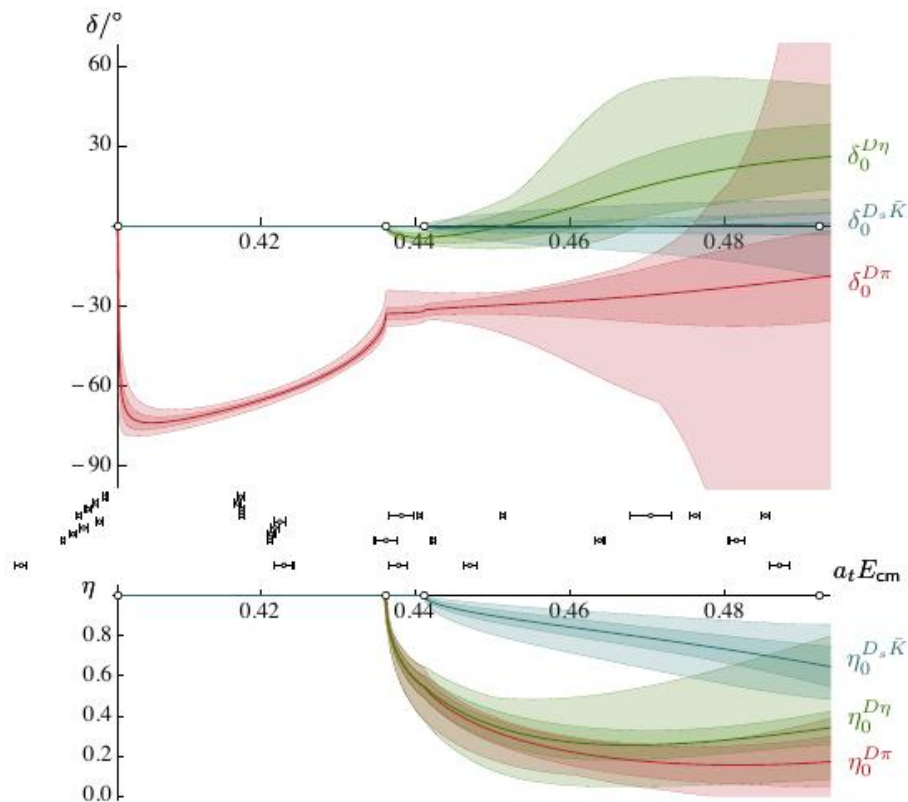
Mai, arXiv:2010.00056 [nucl-th]



Two-pole structures in the meson sector

Moir, Peardon, Ryan, Thomas, Wilson, JHEP **1610** (2016) 011

- $D\pi$, $D\eta$, $D_s\bar{K}$ scattering with $I = 1/2$:
- 3 volumes, one a_s , one a_t , $M_\pi \simeq 390$ MeV, various K-matrix type extrapolations

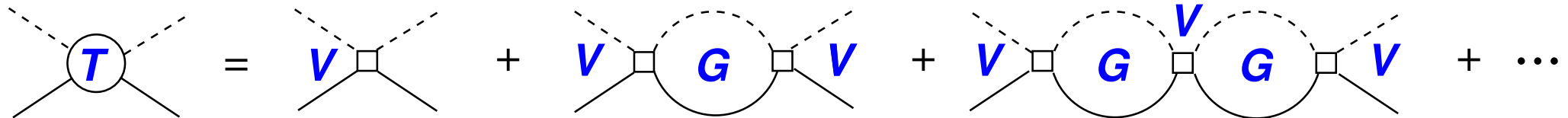


- S-wave pole at (2275.9 ± 0.9) MeV
- close to the $D\pi$ threshold
- consistent w/ $D_0^*(2300)$ of PDG
- BUT: chiral symmetry ignored... :-)

COUPLED CHANNEL DYNAMICS

Kaiser, Weise, Siegel (1995), Oset, Ramos (1998), Oller, UGM (2001), Kolomeitsev, Lutz (2002), Jido et al. (2003), Guo et al. (2006), . . .

- $D\phi$ bound states: Poles of the T-matrix (potential from CHPT and unitarization)



- Unitarized CHPT as a non-perturbative tool:

$$T^{-1}(s) = V^{-1}(s) - G(s)$$

- $V(s)$: derived from the SU(3) chiral Lagrangian, 6 LECs up to NLO → next slide
- $G(s)$: 2-point scalar loop function, regularized w/ a subtraction constant $a(\mu)$
- T, V, G : all these are matrices, channel indices suppressed

COUPLED CHANNEL DYNAMICS cont'd

Barnes et al. (2003), van Beveren, Rupp (2003), Kolomeitsev, Lutz (2004), Guo et al. (2006), ...

- NLO effective chiral Lagrangian for coupled channel dynamics

Guo, Hanhart, Krewald, UGM, Phys. Lett. B **666** (2008) 251

$$\mathcal{L}_{\text{eff}} = \mathcal{L}^{(1)} + \mathcal{L}^{(2)}$$

$$\mathcal{L}^{(1)} = \mathcal{D}_\mu D \mathcal{D}^\mu D^\dagger - M_D^2 D D^\dagger, \quad D = (D^0, D^+, D_s^+)$$

$$\mathcal{L}^{(2)} = D [-h_0 \langle \chi_+ \rangle - h_1 \chi_+ + h_2 \langle u_\mu u^\mu \rangle - h_3 u_\mu u^\mu] D \\ + \mathcal{D}_\mu D [h_4 \langle u^\mu u^\nu \rangle - h_5 \{u^\mu, u^\nu\}] \mathcal{D}_\nu D$$

with $u_\mu \sim \partial_\mu \phi$, $\chi_+ \sim \mathcal{M}_{\text{quark}}$, ...

- LECs:

$\hookrightarrow h_0$ absorbed in masses

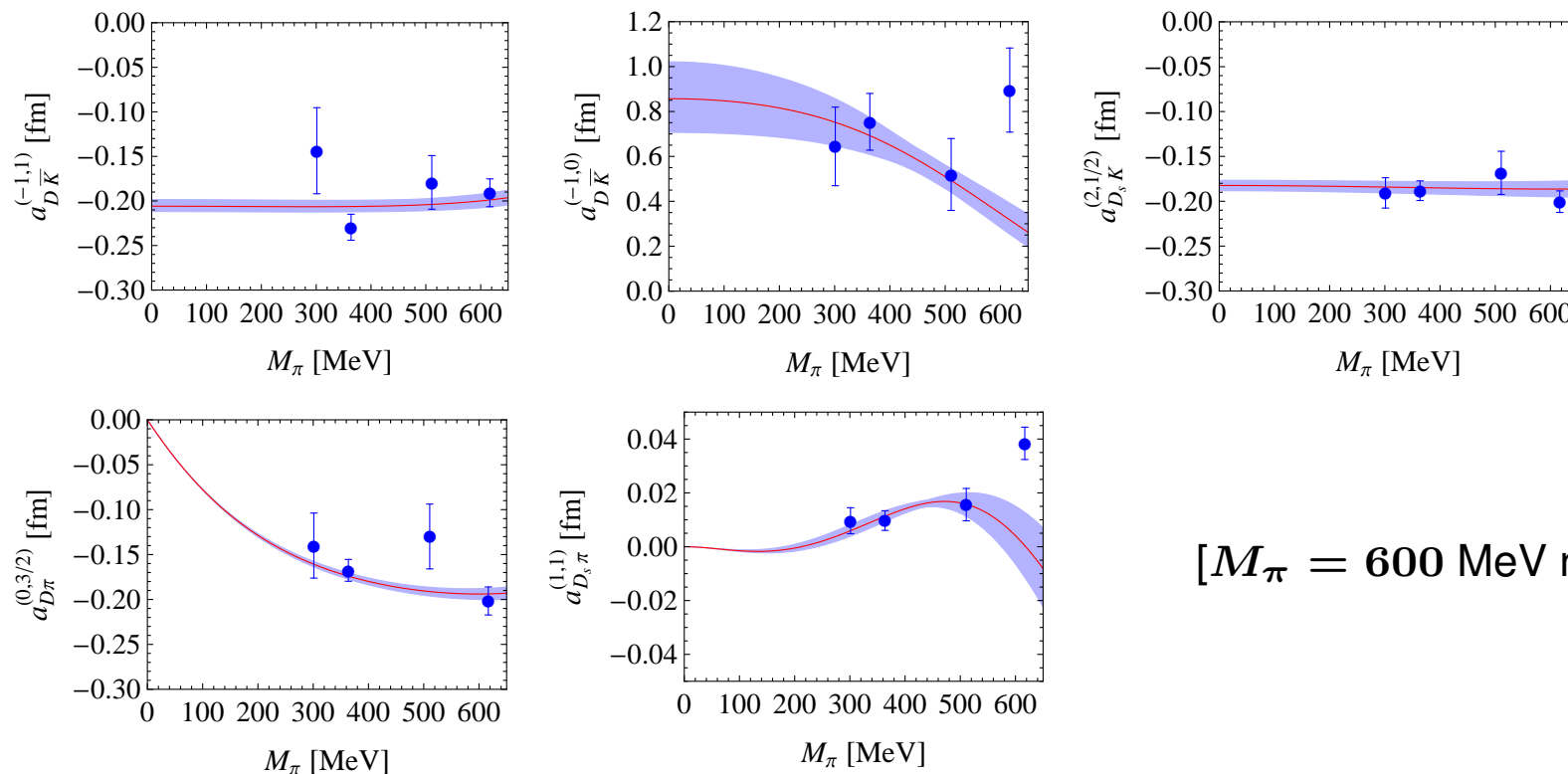
$\hookrightarrow h_1 = 0.42$ from the D_s - D splitting

$\hookrightarrow h_{2,3,4,5}$ from a fit to lattice data ($D\pi \rightarrow D\pi, D\bar{K} \rightarrow D\bar{K}, \dots$)

Liu, Orginos, Guo, Hanhart, UGM, Phys. Rev. D **87** (2013) 014508

Liu, Orginos, Guo, Hanhart, UGM, PRD **87** (2013) 014508

- Fit to lattice data in 5 “simple” channels: no disconnected diagrams



[$M_\pi = 600$ MeV not fitted]

- Prediction: Pole in the $(S, I) = (1, 0)$ channel: 2315^{+18}_{-28} MeV

Experiment:

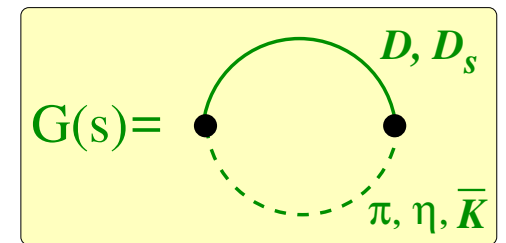
$$M_{D_{s0}^*}(2317) = (2317.8 \pm 0.5) \text{ MeV} \quad \text{PDG2019}$$

FINITE VOLUME FORMALISM

- Goal: postdict the finite volume (FV) energy levels for $I = 1/2$ and compare with the recent LQCD results from Moir et al. using the already fixed LECs
→ parameter-free insights into the $D_0^*(2300)$

- In a FV, momenta are quantized: $\vec{q} = \frac{2\pi}{L}\vec{n}$, $\vec{n} \in \mathbb{Z}^3$

⇒ Loop function $G(s)$ gets modified: $\int d^3\vec{q} \rightarrow \frac{1}{L^3} \sum_{\vec{q}}$



$$\tilde{G}(s, L) = G(s) = \lim_{\Lambda \rightarrow \infty} \left[\frac{1}{L^3} \sum_{|\vec{q}| < \Lambda} I(\vec{q}) - \int_0^\Lambda \frac{q^2 dq}{2\pi^2} I(\vec{q}) \right]$$

Döring, UGM, Rusetsky, Oset, Eur. Phys. J. A47 (2011) 139

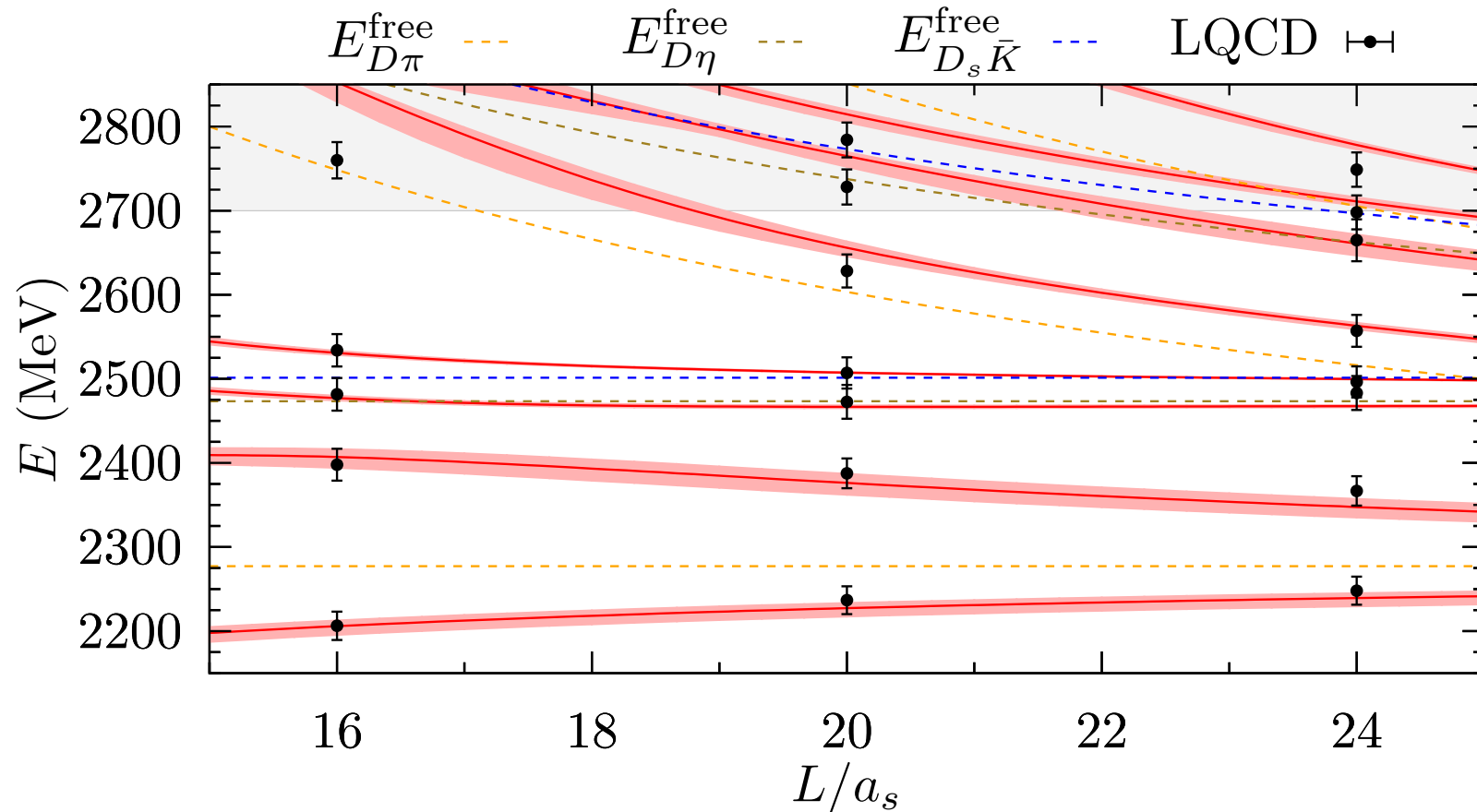
- FV energy levels from the poles of $\tilde{T}(s, L)$:

$$\tilde{T}^{-1}(s, L) = V^{-1}(s) - \tilde{G}(s, L)$$

WHAT ABOUT the $D_0^*(2300)$?

- Results for $I = 1/2$ $D\phi$ scattering

Albaladejo, Fernandez-Soler, Guo, Nieves, Phys. Lett. B **767** (2017) 465



- this is NOT a fit!
- all LECs taken from the earlier study of Liu et al. (discussed before)

WHAT ABOUT the $D_0^*(2300)$?

- reveals a two-pole scenario! [cf. $\Lambda(1405)$]

- understood from group theory

$$\bar{\mathbf{3}} \otimes \mathbf{8} = \underbrace{\bar{\mathbf{3}} \oplus \mathbf{6}}_{\text{attractive}} \oplus \bar{\mathbf{15}}$$

- this was seen earlier in various calc's

Kolomeitsev, Lutz (2004), F. Guo, Shen, Chiang, Ping, Zou (2006),
F. Guo, Hanhart, UGM (2009), Z. Guo, UGM, Yao (2009)

- Again: important role of **chiral symmetry**

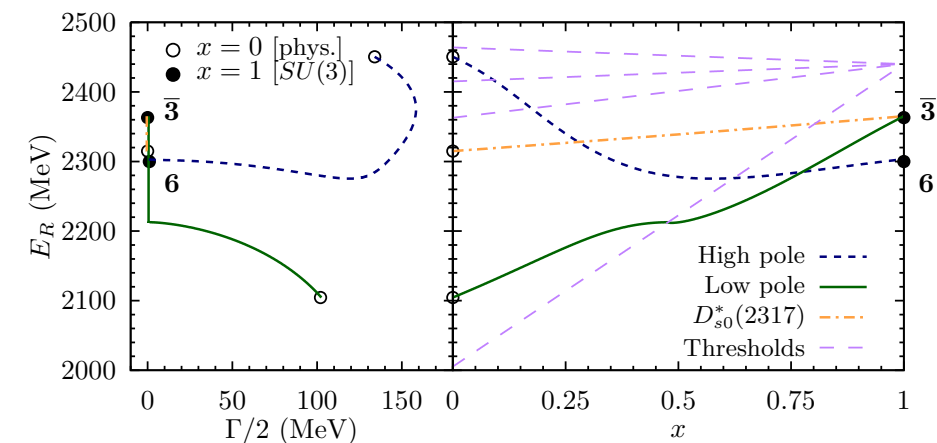
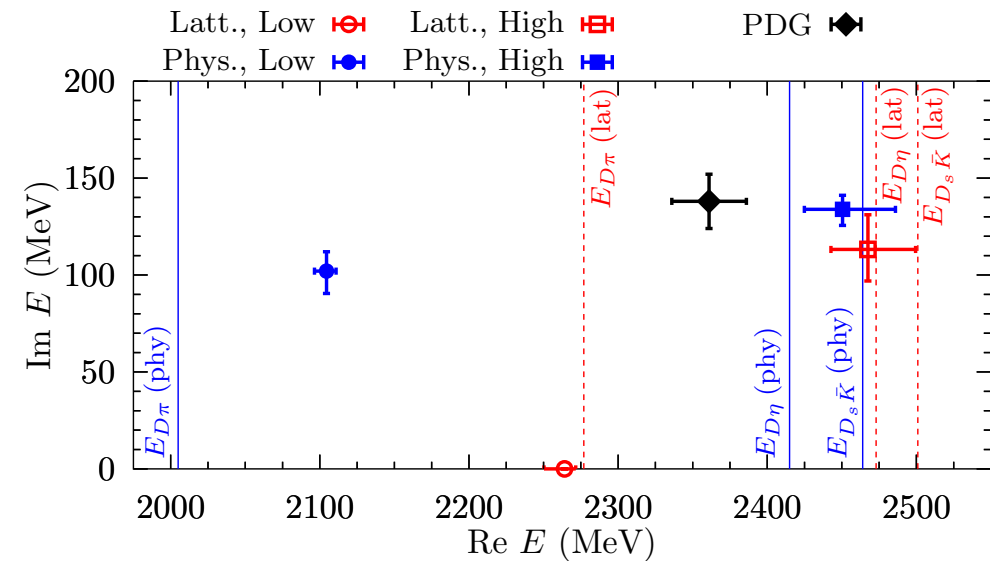
- Easy lattice QCD test:

sextet pole becomes a bound state

for $M_\phi > 575$ MeV in the SU(3) limit

Du et al., Phys.Rev. D **98** (2018) 094018

Albaladejo, Fernandez-Soler, Guo, Nieves (2017)



TWO-POLE SCENARIO in the HEAVY-LIGHT SECTOR ²²

- Two states in various $I = 1/2$ states in the heavy meson sector ($M, \Gamma/2$)

	Lower [MeV]	Higher [MeV]	PDG [MeV]
D_0^*	$(2105_{-8}^{+6}, 102_{-11}^{+10})$	$(2451_{-26}^{+36}, 134_{-8}^{+7})$	$(2318 \pm 29, 134 \pm 20)$
D_1	$(2247_{-6}^{+5}, 107_{-10}^{+11})$	$(2555_{-30}^{+47}, 203_{-9}^{+8})$	$(2427 \pm 40, 192_{-55}^{+65})$
B_0^*	$(5535_{-11}^{+9}, 113_{-17}^{+15})$	$(5852_{-19}^{+16}, 36 \pm 5)$	—
B_1	$(5584_{-11}^{+9}, 119_{-17}^{+14})$	$(5912_{-18}^{+15}, 42_{-4}^{+5})$	—

Lattice QCD: $M_{B_{s_0}^*} = 5711(13)(19)$ MeV , $M_{B_{s_1}} = 5750(17)(19)$ MeV

Lang et al., Phys.Lett. B **750** (2015) 17

→ but is there further experimental support for this?

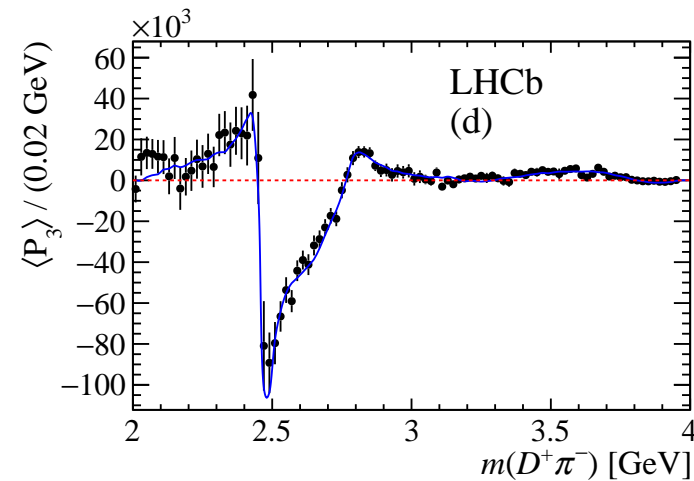
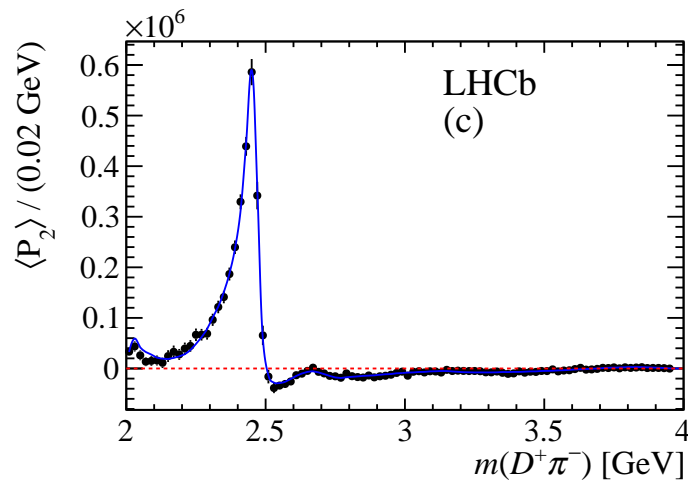
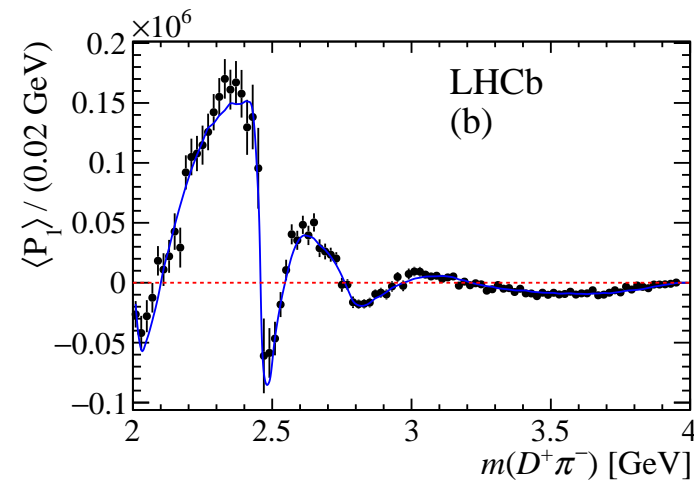
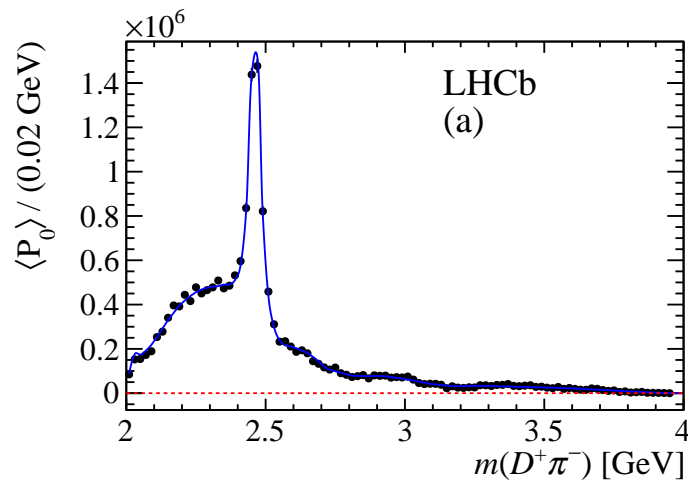
Amplitude Analysis of $B \rightarrow D\pi\pi$

DATA for $B \rightarrow D\pi\pi$

- Recent high precision results for $B \rightarrow D\pi\pi$ from LHCb

Aaji et al. [LHCb], Phys. Rev. D **94** (2016) 072001

- Spectroscopic information in the angular moments ($D\pi$ FSI):



CHIRAL LAGRANGIAN for $B \rightarrow D$ TRANSITIONS

Savage, Wise, Phys. Rev. D39 (1989) 3346

- Consider $\bar{B} \rightarrow D$ transition with the emission of two light pseudoscalars (pions)
 - \hookrightarrow chiral symmetry puts constraints on one of the two pions
 - \hookrightarrow the other pion moves fast and does not participate in the final-state interactions
- Chiral effective Lagrangian:

$$\begin{aligned} \mathcal{L}_{\text{eff}} = & \bar{B} \left[c_1 (u_\mu t M + M t u_\mu) + c_2 (u_\mu M + M u_\mu) t \right. \\ & + c_3 t (u_\mu M + M u_\mu) + c_4 (u_\mu \langle M t \rangle + M \langle u_\mu t \rangle) \\ & \left. + c_5 t \langle M u_\mu \rangle + c_6 \langle (M u_\mu + u_\mu M) t \rangle \right] \partial^\mu D^\dagger \end{aligned}$$

with

$$\bar{B} = (B^-, \bar{B}^0, \bar{B}_s^0), \quad D = (D^0, D^+, D_s^+)$$

M is the matter field for the fast-moving pion

$t = u H u$ is a spurion field for Cabbibo-allowed decays

\rightarrow only some combinations of the LECs c_i appear

$$H = \begin{pmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

THEORY of $B \rightarrow D\pi\pi$

Du, Albadajedo, Fernandez-Soler, Guo, Hanhart, UGM, Nieves, Phys. Rev. **D98** (2018) 094018

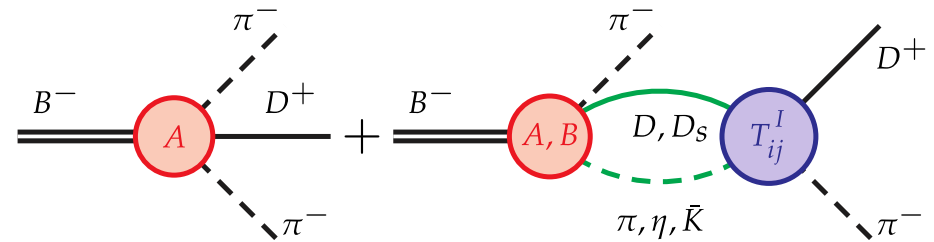
• $B^- \rightarrow D^+ \pi^- \pi^-$ contains coupled-channel $D\pi$ FSI

• consider S, P, D waves: $\mathcal{A}(B^- \rightarrow D^+ \pi^- \pi^-) = \mathcal{A}_0(s) + \mathcal{A}_1(s) + \mathcal{A}_2(s)$

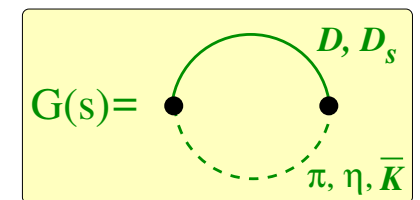
→ P-wave: $D^*, D^*(2680)$; D-wave: $D_2(2460)$ as by LHCb

→ S-wave: use coupled channel ($D\pi, D\eta, D_s \bar{K}$) amplitudes with all parameters fixed before

→ only two parameters in the S-wave (one combination of the LECs c_i and one subtraction constant in the G_{ij})



$$\begin{aligned} \mathcal{A}_0(s) \propto E_\pi & \left[2 + G_{D\pi}(s) \left(\frac{5}{3} T_{11}^{1/2}(s) + \frac{1}{3} T_{11}^{3/2}(s) \right) \right] \\ & + \frac{1}{3} E_\eta G_{D\eta}(s) T_{21}^{1/2}(s) + \sqrt{\frac{2}{3}} E_{\bar{K}} G_{D_s \bar{K}}(s) T_{31}^{1/2}(s) \\ & + C E_\eta G_{D\eta}(s) T_{21}^{1/2}(s) \end{aligned}$$



THEORY of $B \rightarrow D\pi\pi$ continued

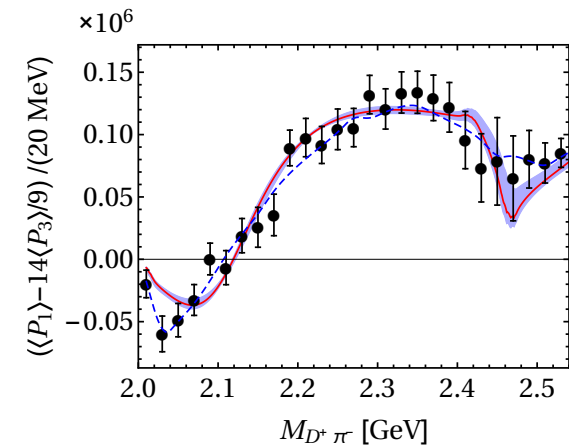
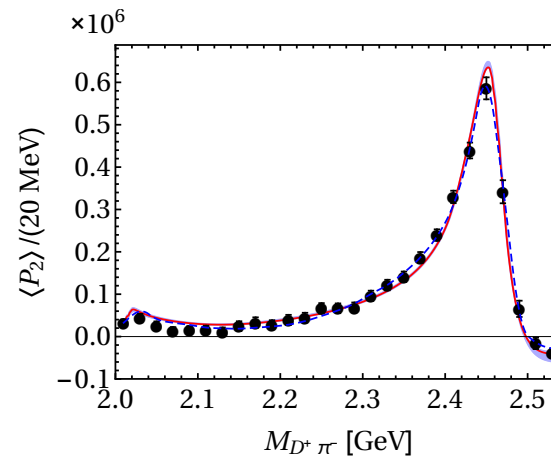
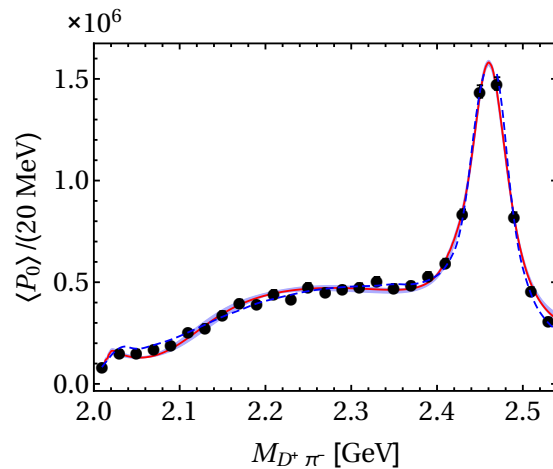
Du, Albadajedo, Fernandez-Soler, Guo, Hanhart, UGM, Nieves, Yao, Phys. Rev. **D98** (2018) 094018

- More appropriate combinations of the angular moments:

$$\langle P_0 \rangle \propto |\mathcal{A}_0|^2 + |\mathcal{A}_1|^2 + |\mathcal{A}_2|^2$$

$$\langle P_2 \rangle \propto \frac{2}{5}|\mathcal{A}_1|^2 + \frac{2}{7}|\mathcal{A}_2|^2 + \frac{2}{\sqrt{5}}|\mathcal{A}_0||\mathcal{A}_2| \cos(\delta_2 - \delta_0)$$

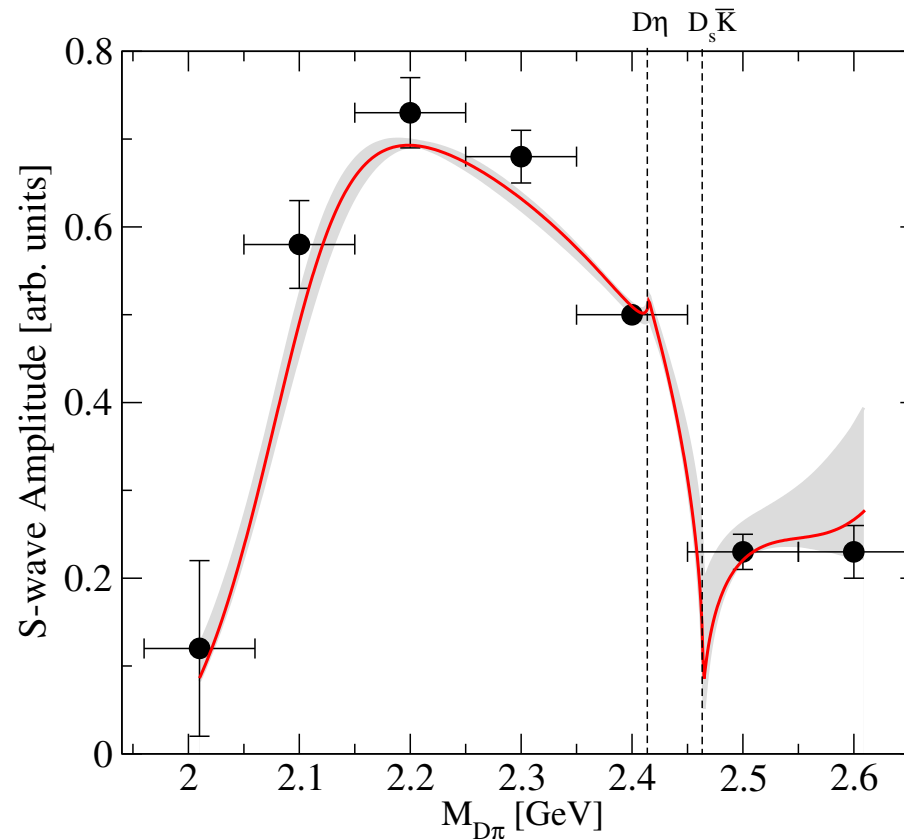
$$\langle P_{13} \rangle = \langle P_1 \rangle - \frac{14}{9}\langle P_3 \rangle \propto \frac{2}{\sqrt{3}}|\mathcal{A}_0||\mathcal{A}_1| \cos(\delta_1 - \delta_0)$$



- The **S-wave** $D\pi$ can be very well described using pre-fixed amplitudes
- Fast variation in [2.4,2.5] GeV in $\langle P_{13} \rangle$: cusps at the $D\eta$ and $D_s\bar{K}$ thresholds
 \hookrightarrow should be tested experimentally

A CLOSER LOOK at the S-WAVE

- LHCb provides anchor points, where the strength and the phase of the S-wave were extracted from the data and connected by cubic spline

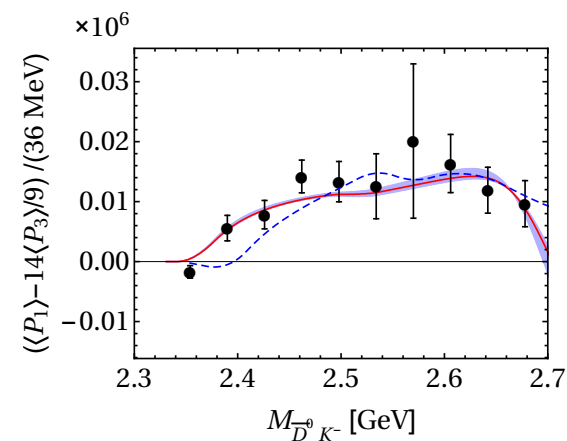
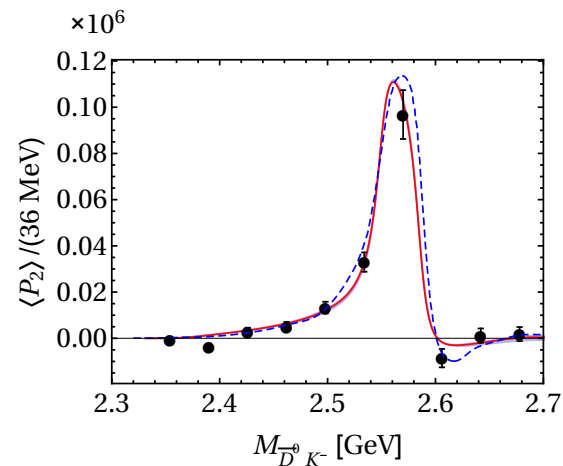
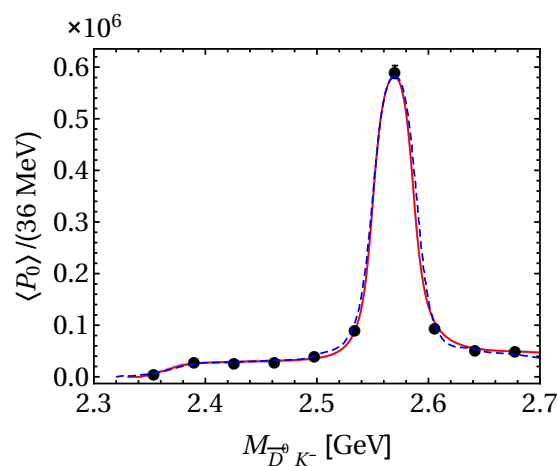


- Higher mass pole at 2.46 GeV clearly amplifies the cusps predicted in our amplitude

THEORY of $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$

Du, Albadajedo, Fernandez-Soler, Guo, Hanhart, UGM, Nieves, Yao, Phys. Rev. **D98** (2018) 094018

- LHCb has also data on $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$, but less precise
- Same formalism as before, one different combination of the LECs c_i
- same resonances in the P- and D-wave as LHCb \hookrightarrow one parameter fit!



\Rightarrow these data are also well described

\Rightarrow better data for $\langle P_{13} \rangle$ would be welcome

\Rightarrow even more channels, see Du, Guo, UGM, Phys. Rev. D **99** (2019) 114002

- It all started with the two-pole structure of the $\Lambda(1405)$
 - ↪ well established fact!
 - ↪ lighter pole still needs better determination
 - ↪ be aware of models that can not cope with this
- Clear candidates in the meson sector
 - ↪ some excited charm mesons are good candidates for molecules
 - ↪ esp. $D_0^*(2300)$, $D_{s0}^*(2317)$, $D_{s1}(2460)$, ...
 - ↪ this solves various puzzles: masses, ordering, ...
 - ↪ for further support, see the recent work [Du et al., 2012.04599 \[hep-ph\]](#)
 - ↪ testable predictions for various beauty mesons B_0^* , B_1
- All this is not properly reflected in the PDG tables
 - ↪ summary tables e.g. only lists one pole for the $\Lambda(1405)$
 - ↪ many states analyzed using BW parametrization :-)
 - ↪ **PDG needs a more serious approach to the hadron spectrum!**



- but there is some hope, two excited Λ states listed now (2020 edition):

P. A. Zyla *et al.* [Particle Data Group], PTEP **2020** (2020) 083C01

Citation: P.A. Zyla *et al.* (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

$\Lambda(1380) 1/2^-$

$J^P = \frac{1}{2}^-$ Status: **

OMITTED FROM SUMMARY TABLE

See the related review on "Pole Structure of the $\Lambda(1405)$ Region."

Citation: P.A. Zyla *et al.* (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

$\Lambda(1405) 1/2^-$

$J^P = 0(\frac{1}{2}^-)$ Status: ****

In the 1998 Note on the $\Lambda(1405)$ in PDG 98, R.H. Dalitz discussed the S-shaped cusp behavior of the intensity at the $N\bar{K}$ threshold observed in THOMAS 73 and HEMINGWAY 85. He commented that this behavior "is characteristic of S-wave coupling; the other below threshold hyperon, the $\Sigma(1385)$, has no such threshold distortion because its $N\bar{K}$ coupling is P-wave. For $\Lambda(1405)$ this asymmetry is the sole direct evidence that $J^P = 1/2^-$."

A recent measurement by the CLAS collaboration, MORIYA 14, definitively established the long-assumed $J^P = 1/2^-$ spin-parity assignment of the $\Lambda(1405)$. The experiment produced the $\Lambda(1405)$ spin-polarized in the photoproduction process $\gamma p \rightarrow K^+ \Lambda(1405)$ and measured the decay of the $\Lambda(1405)$ (polarized) $\rightarrow \Sigma^+$ (polarized) π^- . The observed isotropic decay of $\Lambda(1405)$ is consistent with spin $J = 1/2$. The polarization transfer to the Σ^+ (polarized) direction revealed negative parity, and thus established $J^P = 1/2^-$.

See the related review(s):

Pole Structure of the $\Lambda(1405)$ Region

- a new two-star resonance at 1380 MeV
- still not in the summary table
- above/below the line dubious!

\Rightarrow this general phenomenon must be accounted for!



SPARES

- QCD with three light flavors: A theoretical paradise

Leutwyler

$$\boxed{\mathcal{L}_{\text{QCD}} = \mathcal{L}_{\text{QCD}}^0 - \bar{q}\mathcal{M}q}, \quad q = \begin{pmatrix} u \\ d \\ s \end{pmatrix}, \quad \mathcal{M} = \begin{pmatrix} m_u & & \\ & m_d & \\ & & m_s \end{pmatrix}$$

⇒ Exhibits **spontaneous** and **explicit** chiral symmetry breaking

⇒ Can be analyzed **systematically** & **precisely** using EFT = **chiral perturbation theory**

Weinberg (1979) Gasser, Leutwyler (1984,1985)

⇒ Many intriguing results, but:

- often convergence problems in the presence of **strange** quarks
- limited by the appearance of **resonances** and **bound** states

- Discuss here such cases & methods that overcome these limitations

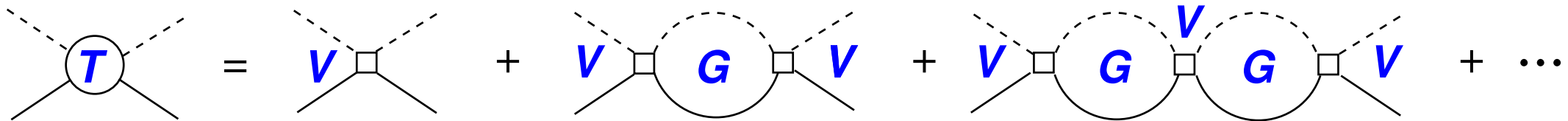
w/ particular emphasis on WW's contribution [baryon spectrum & interactions]

ENTERS CHIRAL DYNAMICS

- Great idea:

Combine (leading-order) chiral SU(3) Lagrangian with coupled-channel dynamics

Kaiser, Siegel, Weise, Nucl. Phys. A **594** (1995) 325



↔ Dominance of the Weinberg-Tomozawa term, excellent description of K^-p data and $\pi\Sigma$ mass distribution, also inclusion of NLO terms with constrained fits

↔ The $\Lambda(1405)$ appears as a **dynamically generated state** (MB molecule)

↔ Highly cited follow-ups from TUM group plus other groups, esp. “Spanish Mafia”
Oset, Ramos, Nucl. Phys. A **635** (1998) 99, ...

- But: unpleasant regulator dependence (Yukawa-type, momentum cut-off)
gauge invariance in photo-reactions?

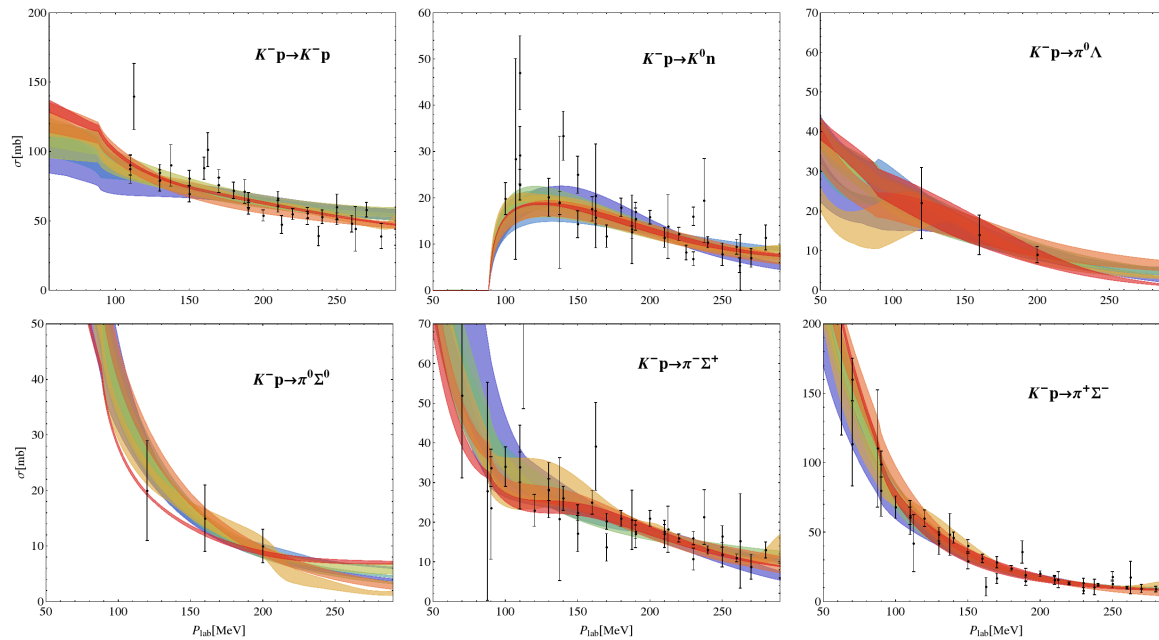
YET ANOTHER TWIST

- Looking even more closely, yet another surprise:

⇒ at least 8 solutions of similar quality w/ different pairs of poles for the $\Lambda(1405)$

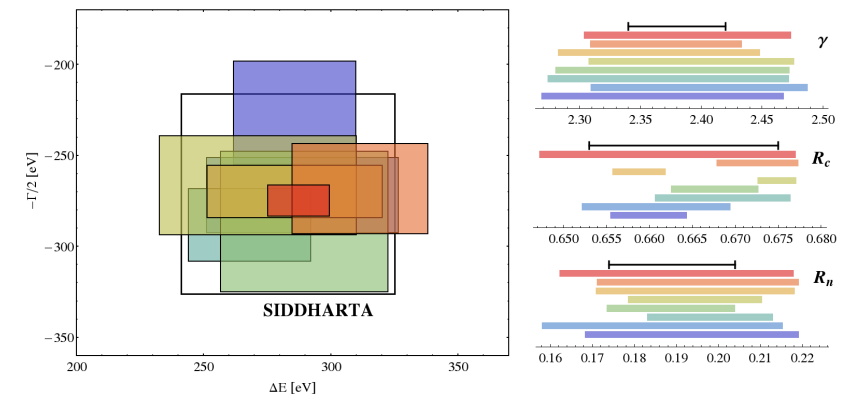
Mai and UGM, EPJ A **51** (2015) 30

- Scattering data



- Kaonic hydrogen

- Threshold ratios



SIDDHARTA: M. Bazzi et al., Phys. Lett. B **704**, 113 (2011)

Scatt. data: Ciborowski et al., J. Phys. G **8**, 13 (1982), Humphrey, Ross, Phys. Rev. **127**, 1305 (1962)

Sakitt et al., Phys. Rev. B **139**, 719 (1965), Watson et al., Phys.Rev. **131**, 2248 (1963)

