



Updates on the **forward modeling** of  
 **$f\sigma_8$  with ZTF**

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**CPPM, Marseille**

**ZTF Cosmo Barcelona, 11/12/2024**

→ → Linear theory! ← ←

Who is  $f\sigma_8$ ?

$$\vec{\nabla} \cdot \vec{v} = -H_0 (f\sigma_8) \delta_{\sigma_8=1}$$

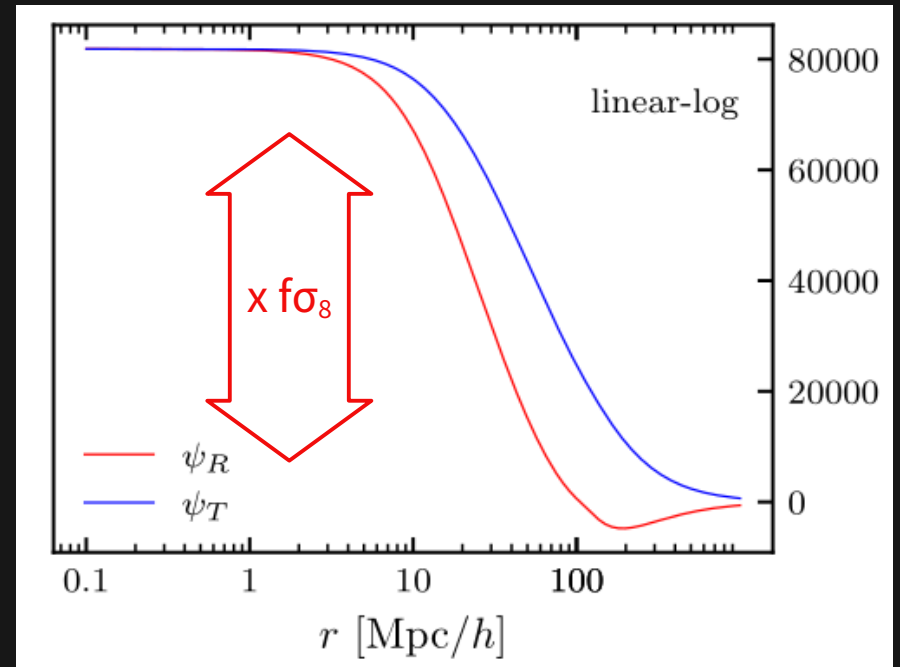
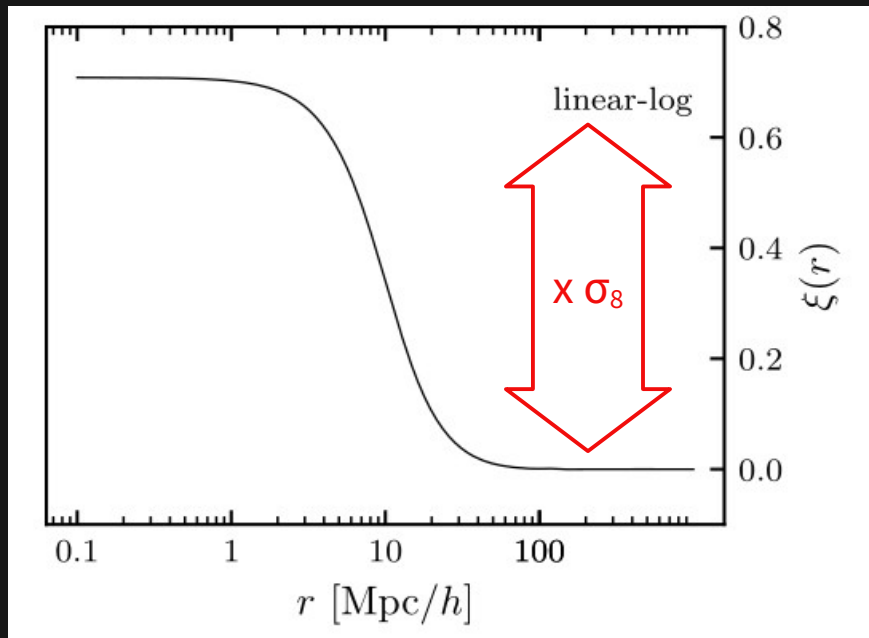
→ → Linear theory! ← ←

# Who is $f\sigma_8$ ?

$$\vec{\nabla} \cdot \vec{v} = -H_0 (f\sigma_8) \delta_{\sigma_8=1}$$

Density correlation function

Velocity correlation functions



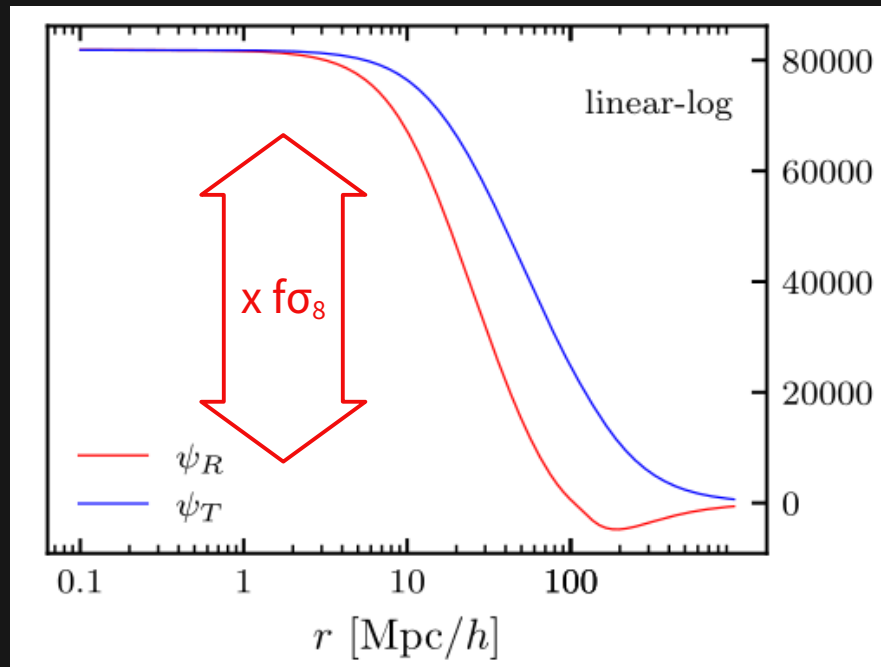
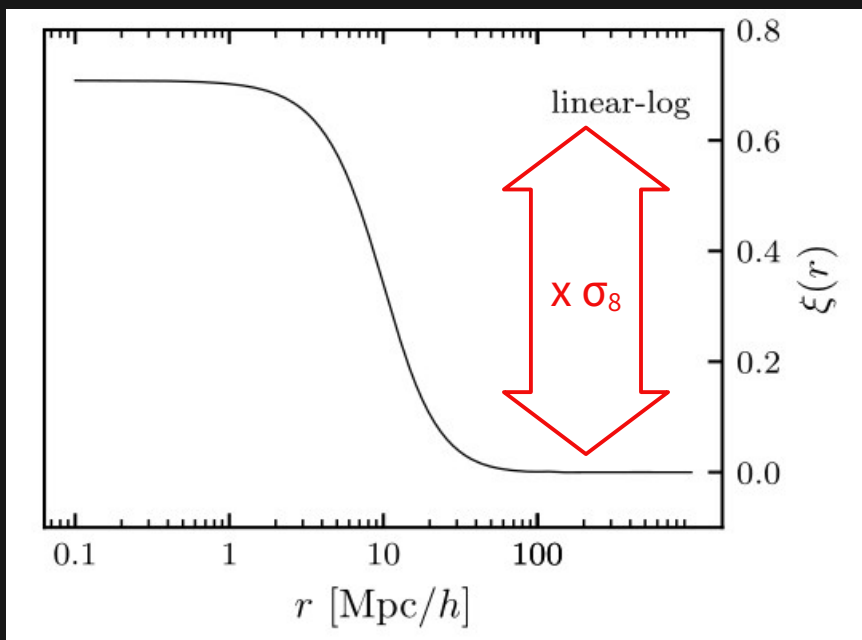
# Who is $f\sigma_8$ ?

→ → **Linear theory!** ← ←

$$\vec{\nabla} \cdot \vec{v} = -H_0 (f\sigma_8) \delta_{\sigma_8=1}$$

Density correlation function

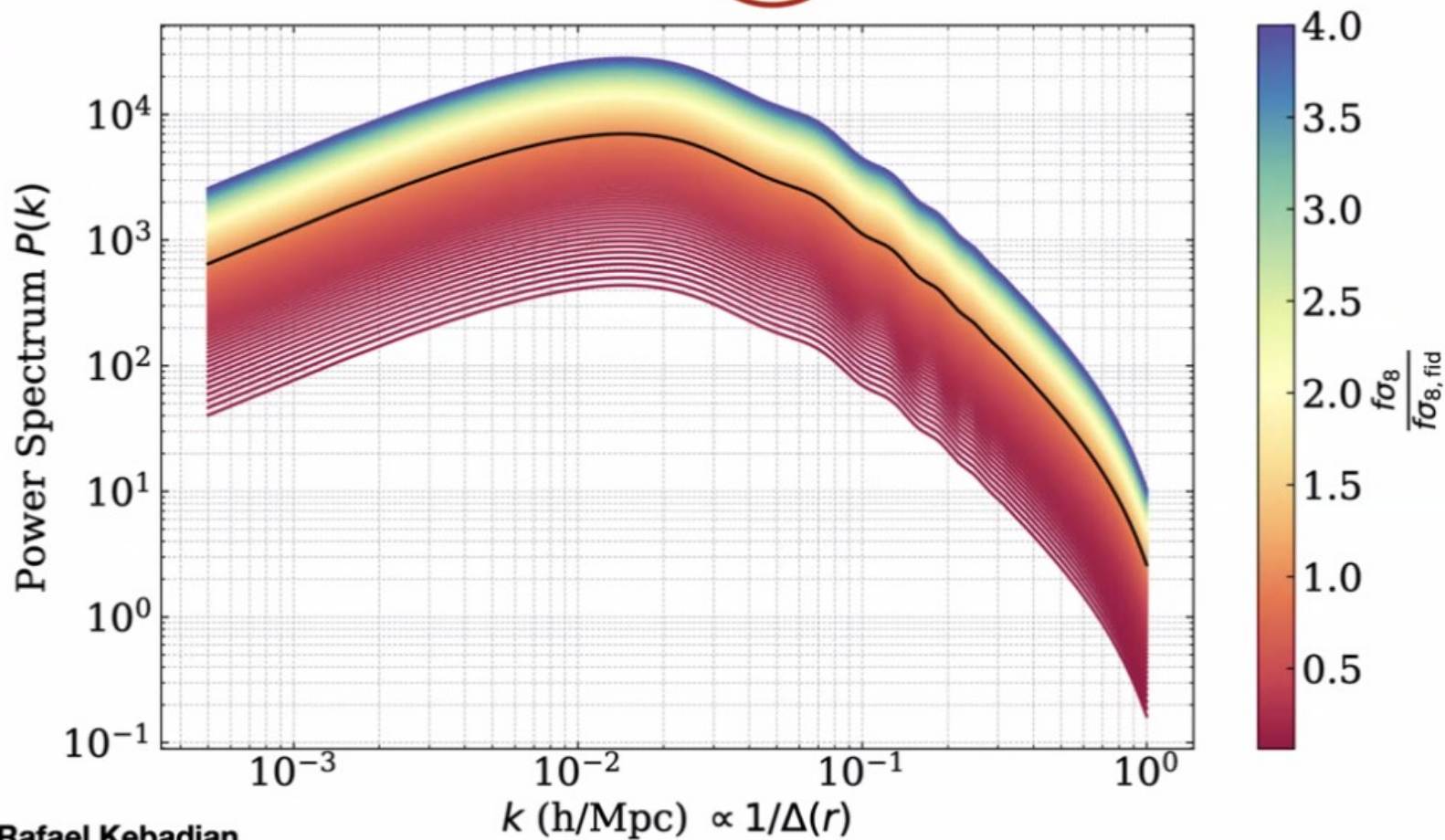
Velocity correlation functions



→ **Shape of the functions fixed**

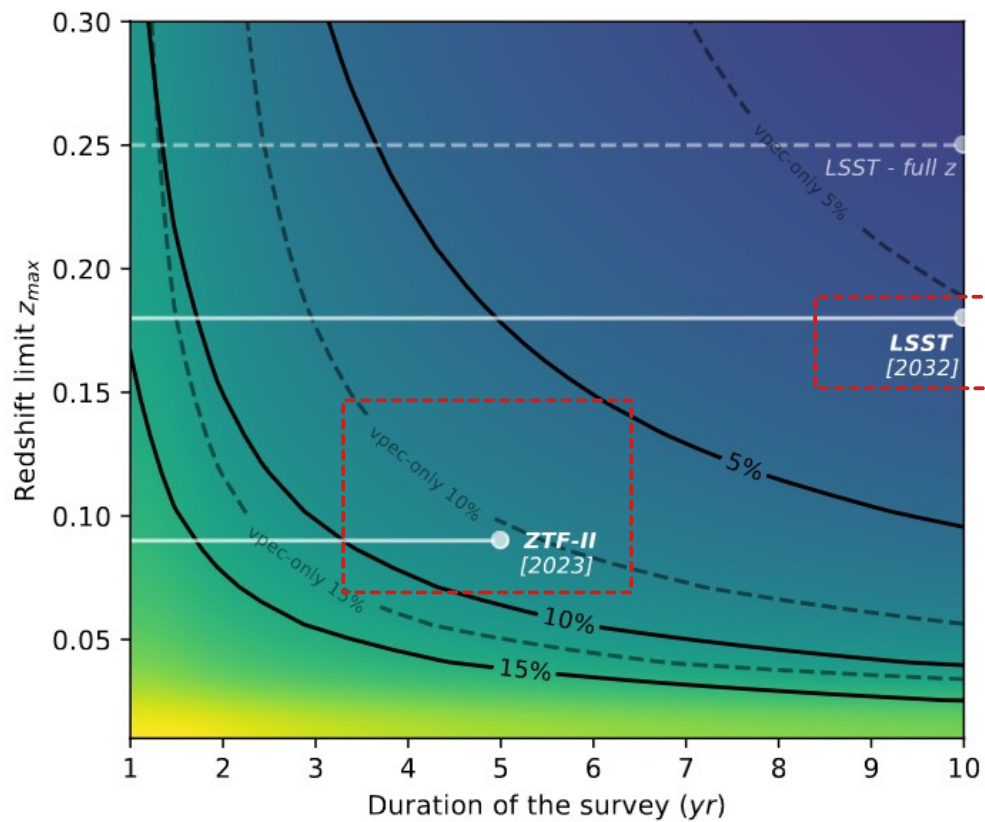
→ **degeneracy between  $f$  and  $\sigma_8$**

$$C_{ij}^{vv} = \frac{H_0^2 (f\sigma_8)^2}{2\pi^2 (f\sigma_8)_{\text{fid}}^2} \int_0^{+\infty} f_{\text{fid}}^2 P_{\theta\theta}(k) D_u^2(k) W_{ij}(k; r_i, r_j) dk$$



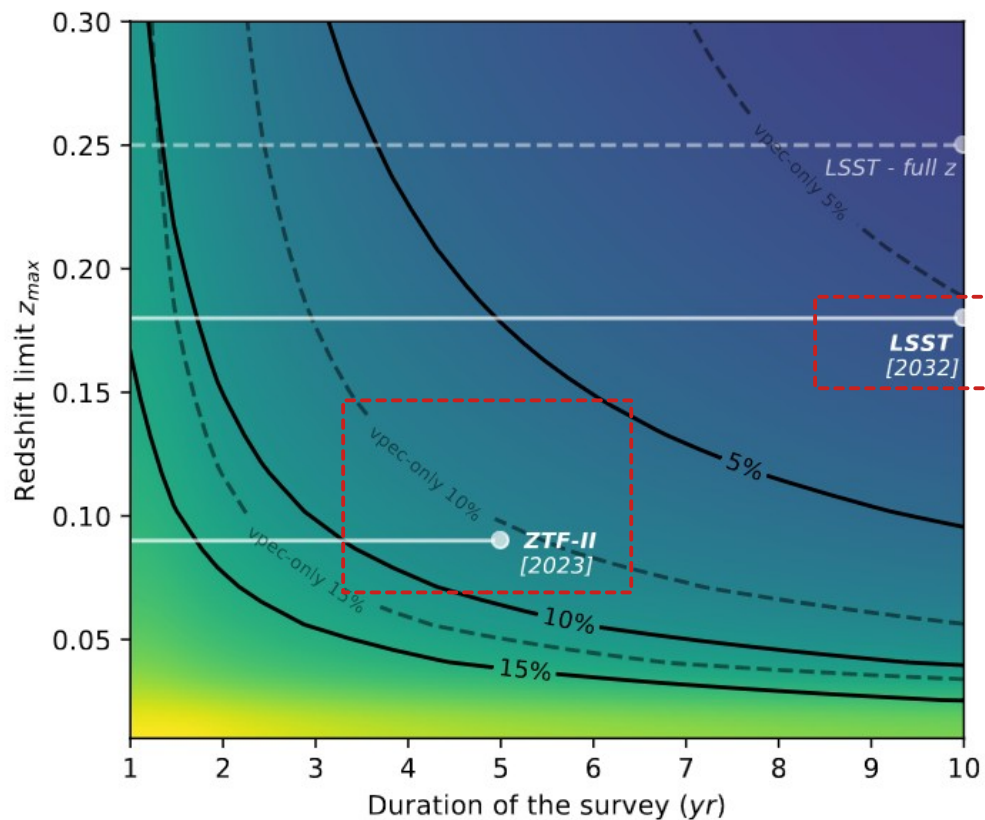
# Prospects on $f\sigma_8$

Fisher Matrix (Graziani 2020)



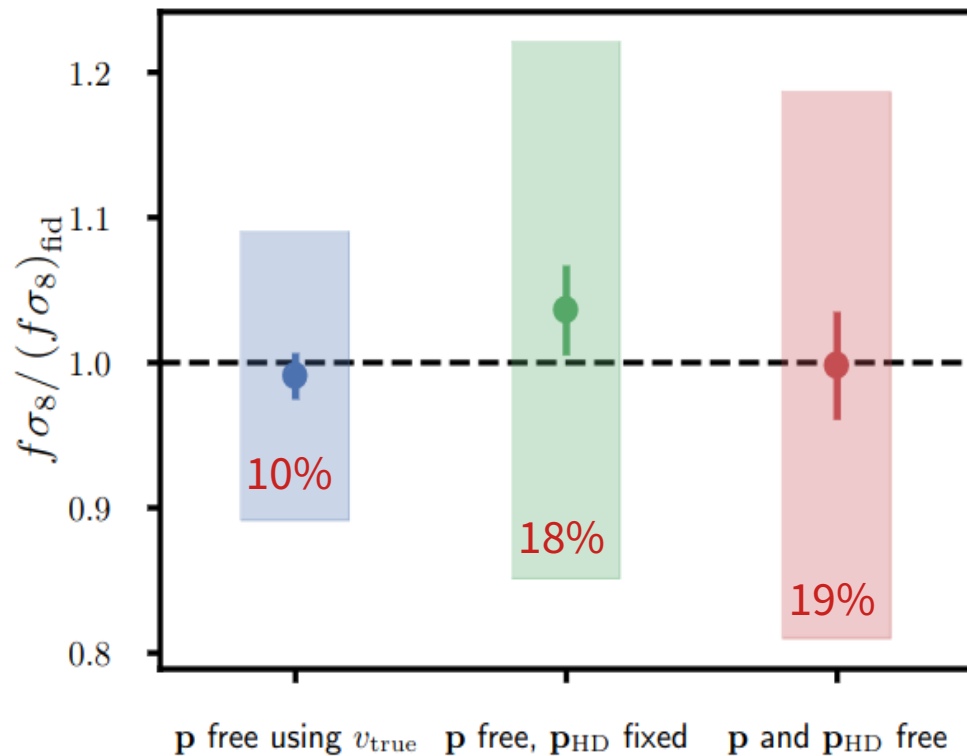
# Prospects on $f\sigma_8$

Fisher Matrix (Graziani 2020)



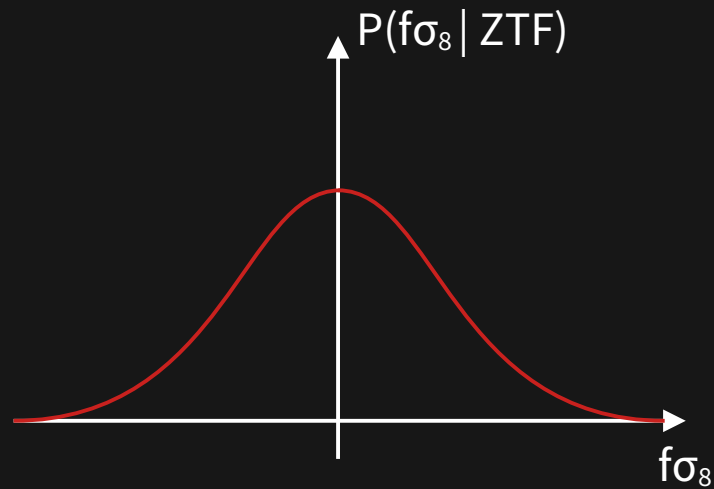
Likelihood maximization (Carreres 2023)

- 6 years
- $z < 0.06$  (complete sample)



# Forward modeling

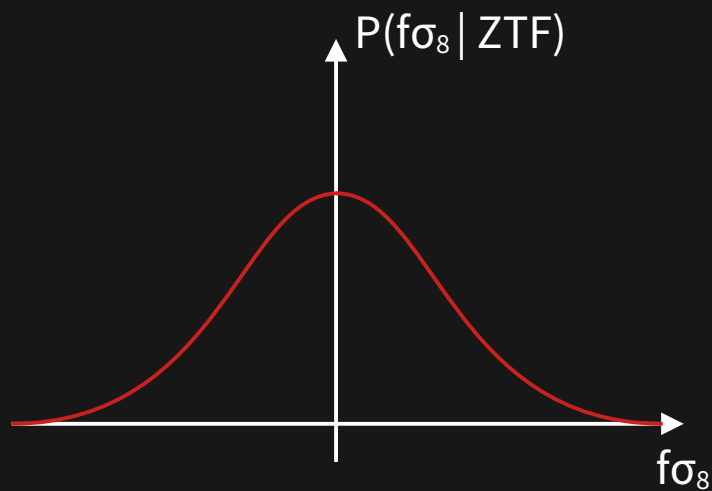
$$P(f\sigma_8, \dots | ZTF)$$





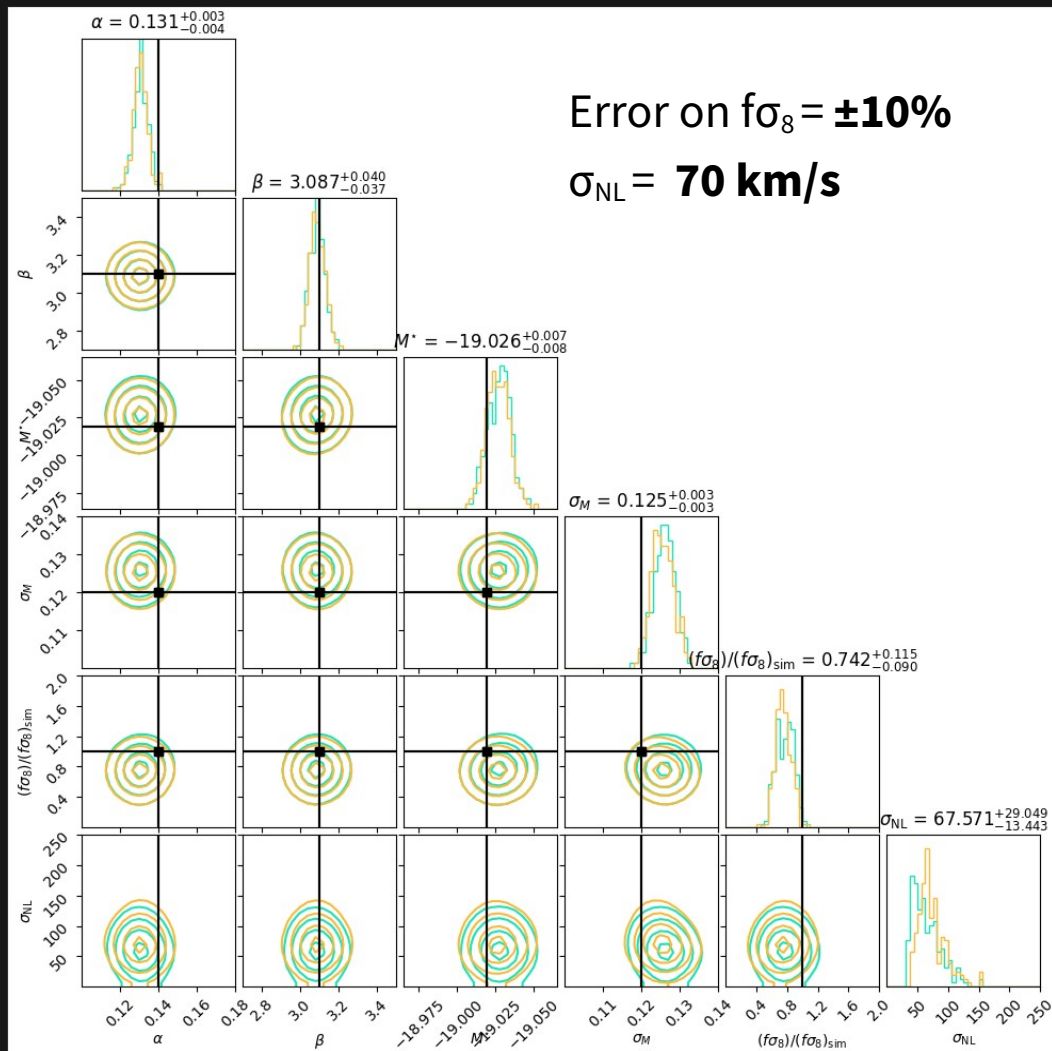
# Forward modeling

$$P(f\sigma_8, \dots | \text{ZTF}) = P(\text{ZTF} | f\sigma_8, \dots) P(f\sigma_8, \dots)$$

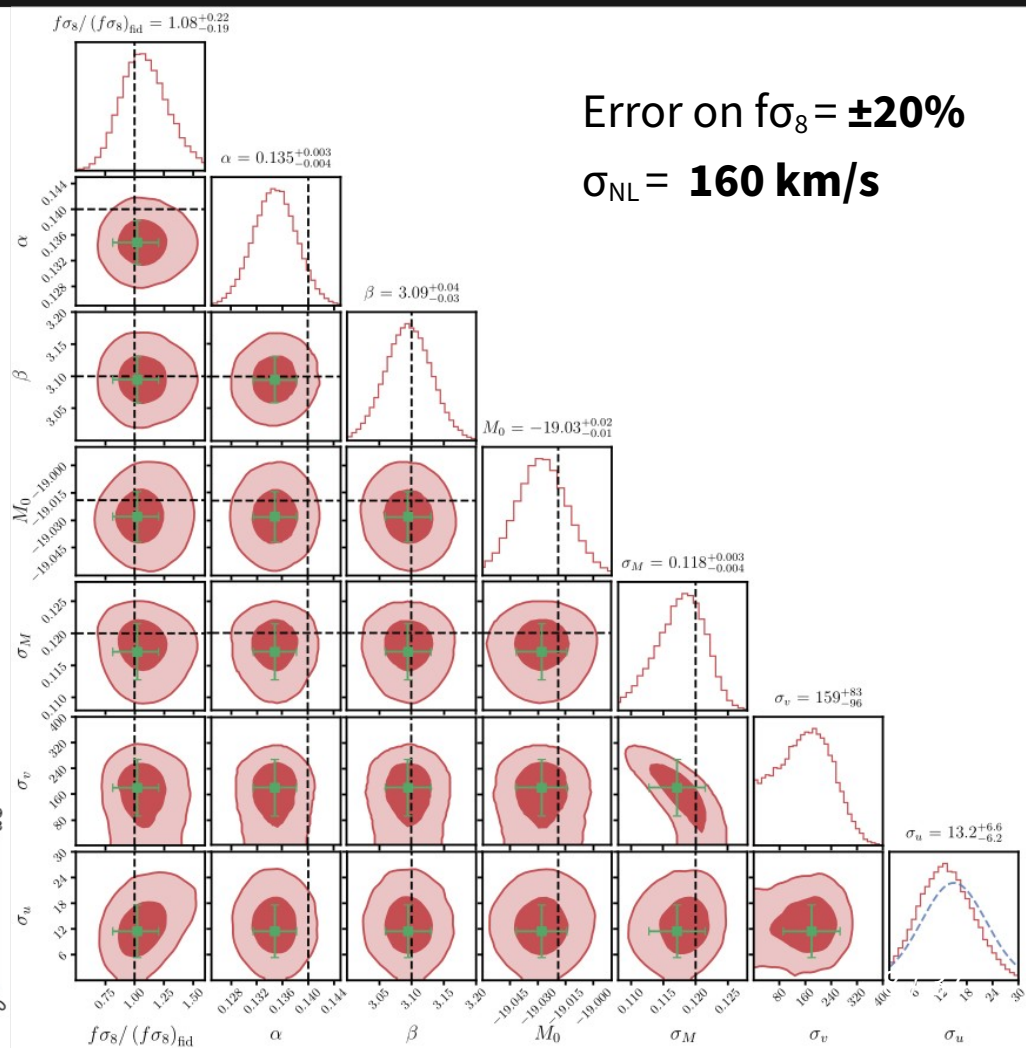




# This work (1 mock)

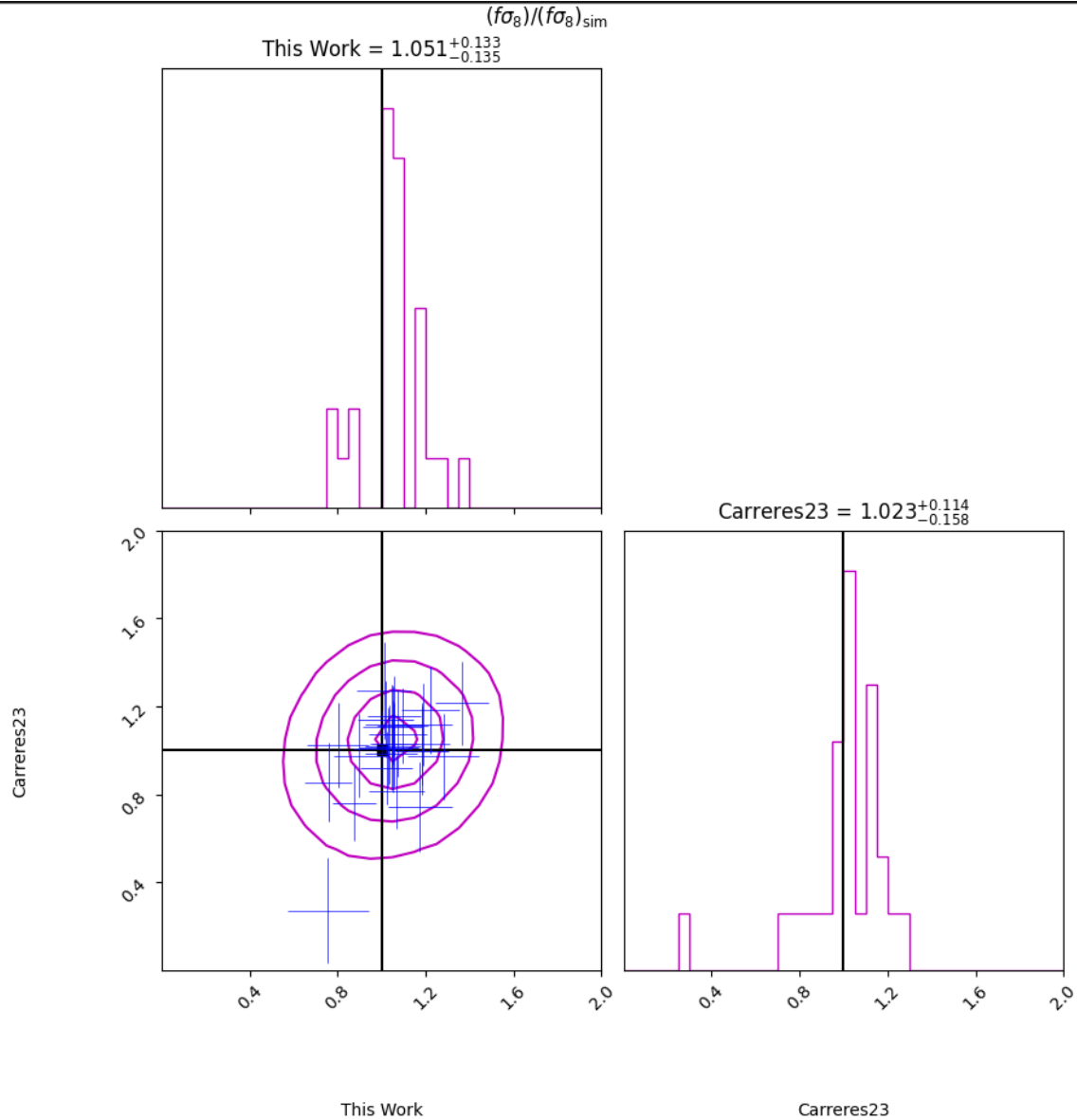


# Carreres 2023 (1 mock)



# Values $(f\sigma_8) / (f\sigma_8)_{sim}$

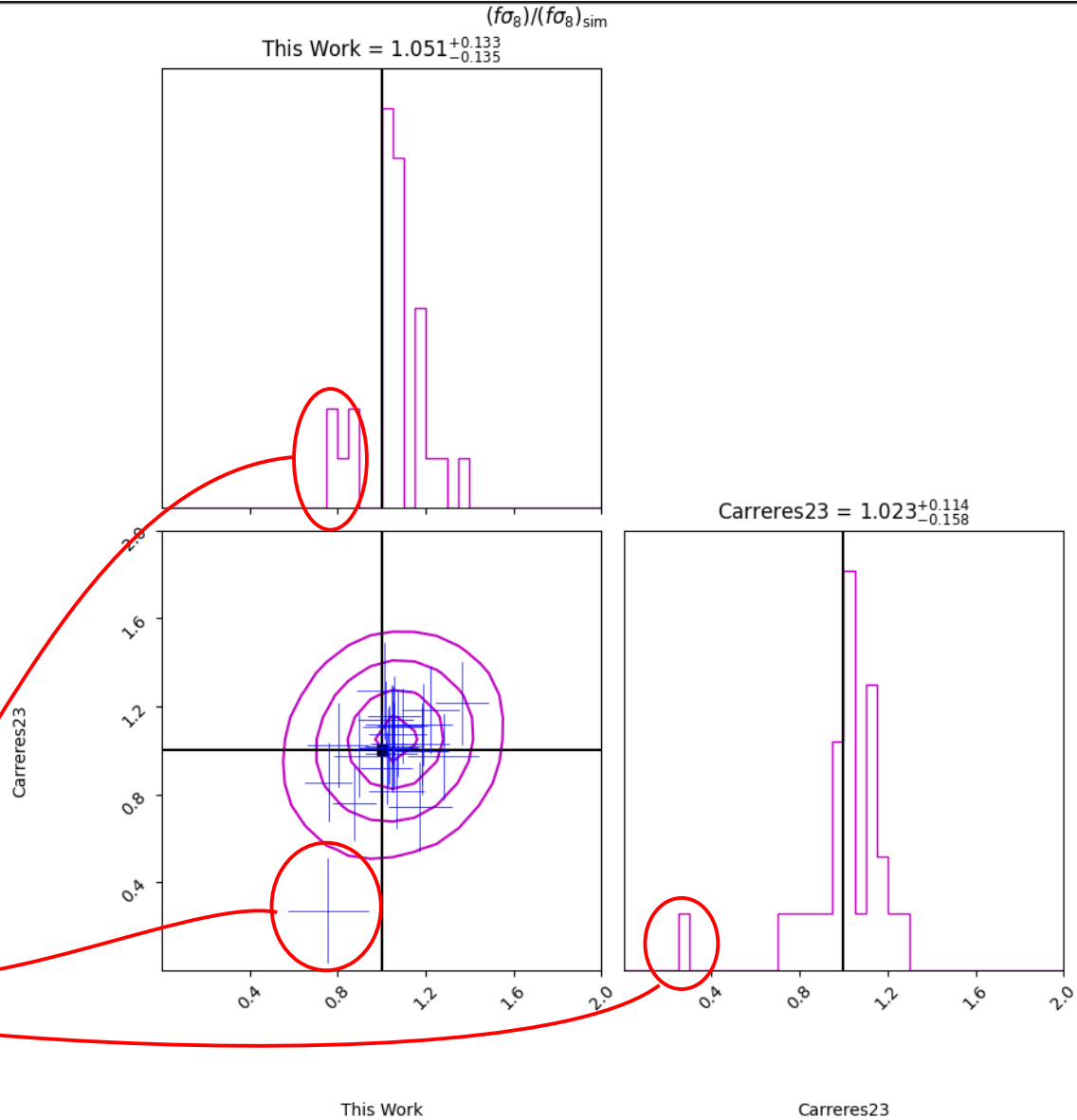
$$\rho_{C23 \leftrightarrow TW} = 0.5 \quad (0.33)$$



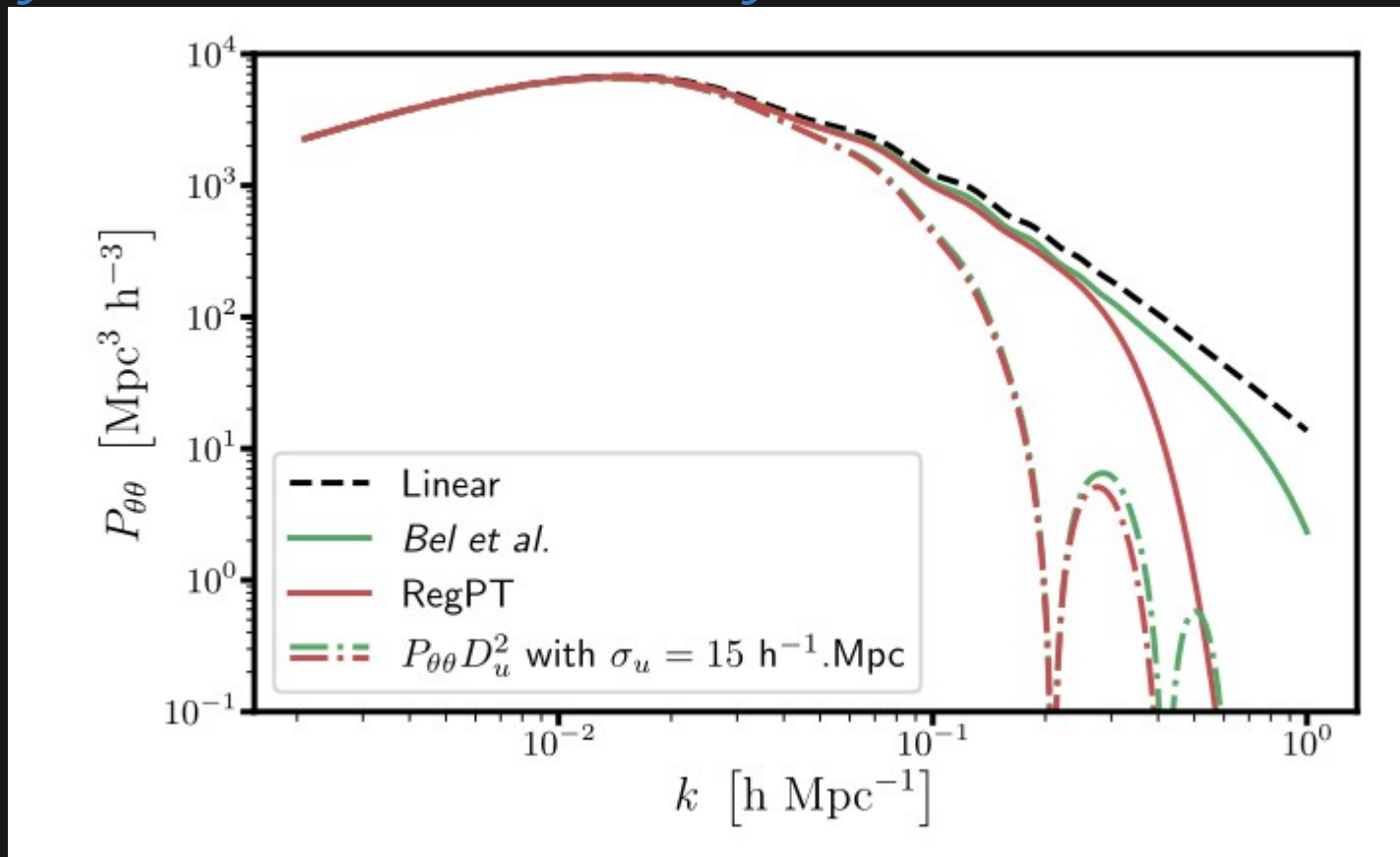
Values  $(f\sigma_8) / (f\sigma_8)_{\text{sim}}$

$$\rho_{\text{C23} \leftrightarrow \text{TW}} = 0.5 \text{ (0.33)}$$

Remove outlier (number 18)



# Go beyond linear theory?



# Linear Theory

**Frozen structure, amplification with time**



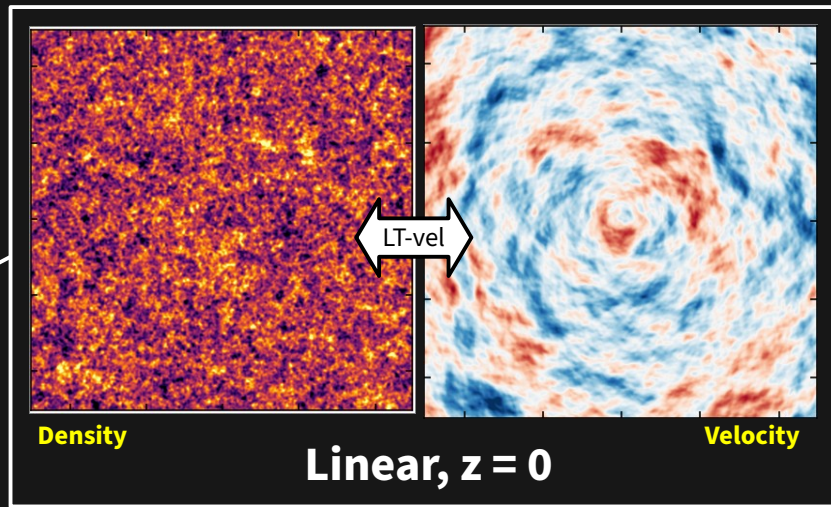
$$\delta(\vec{r}, a) = D_+(a)\delta(\vec{r}) \quad \text{(LT-evol)}$$

$$\vec{\nabla} \cdot \vec{v}(\vec{r}) = -H_0 f \delta(\vec{r}) \quad \text{(LT-vel)}$$

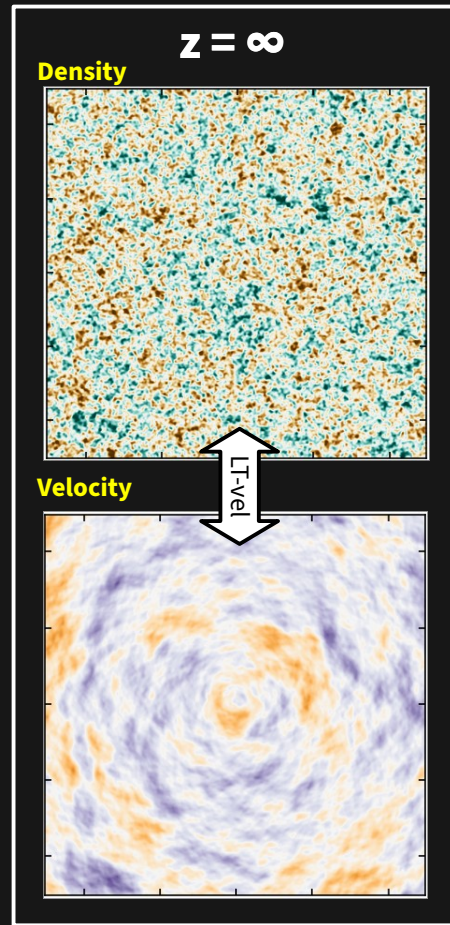


**Velocity-density fields conservation-like equation**

Velocity data  
 $z = 0$

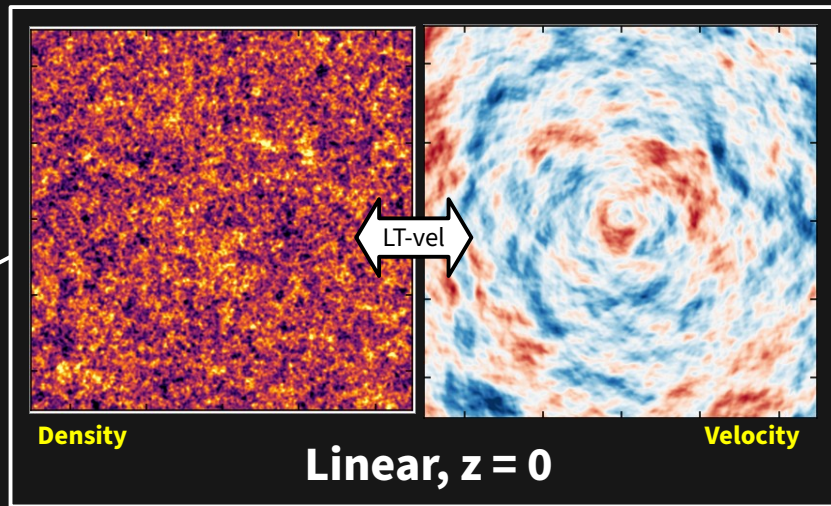


LT-evol  
←

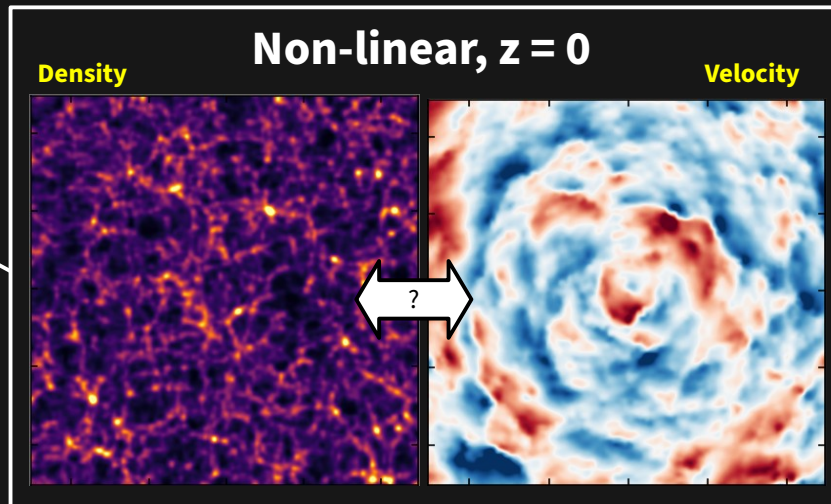




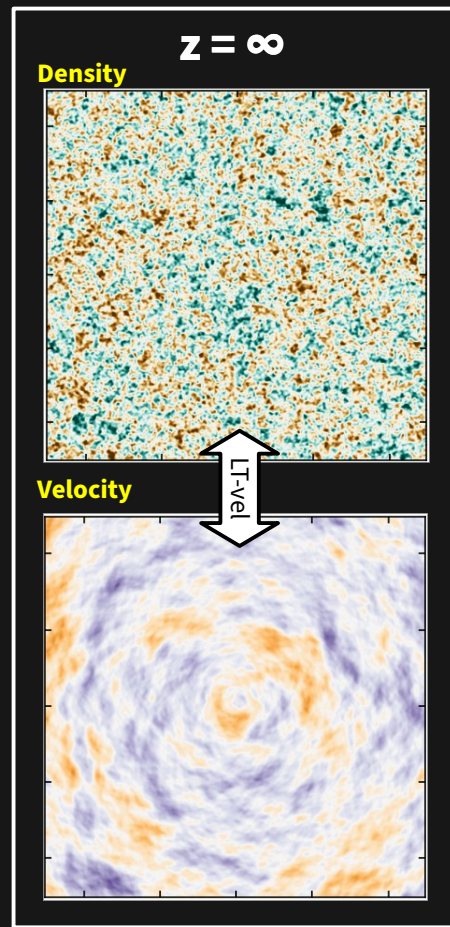
Velocity data  
 $z = 0$



LT-evol  
←



N-body  
LPT  
←



# Non-linear code requirements

- **Cheap** → evaluated about 1 000 000 times
- **Differentiable** → for the inference algorithm
- **Low resolution** → limit number of free parameters
- **GPU compatible** → inference speed-up about 1000

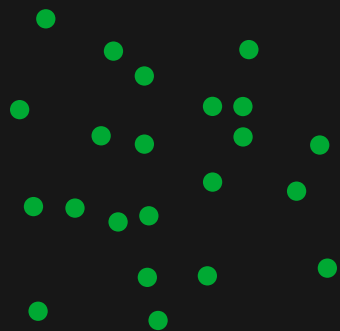


## particle mesh with derivatives

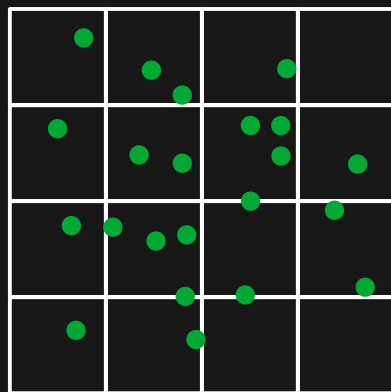
`pmwd` is a differentiable cosmological particle-mesh forward model. The  $C_2$  symmetry of the name symbolizes the reversibility of the model, which helps to dramatically reduce the memory cost when used with the adjoint method. Based on `JAX`, `pmwd` is fully differentiable, and is highly performant on GPUs.

# Particle mesh

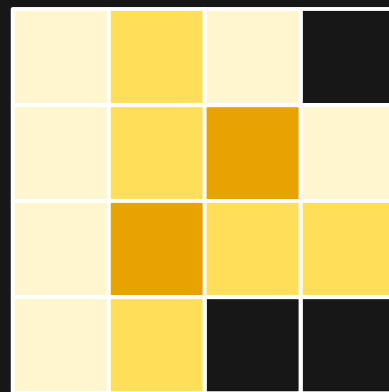
Particles



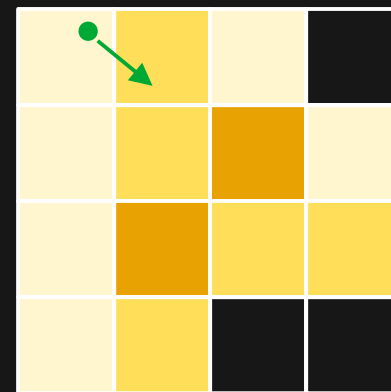
Lattice



Cloud in Cell (CiC)



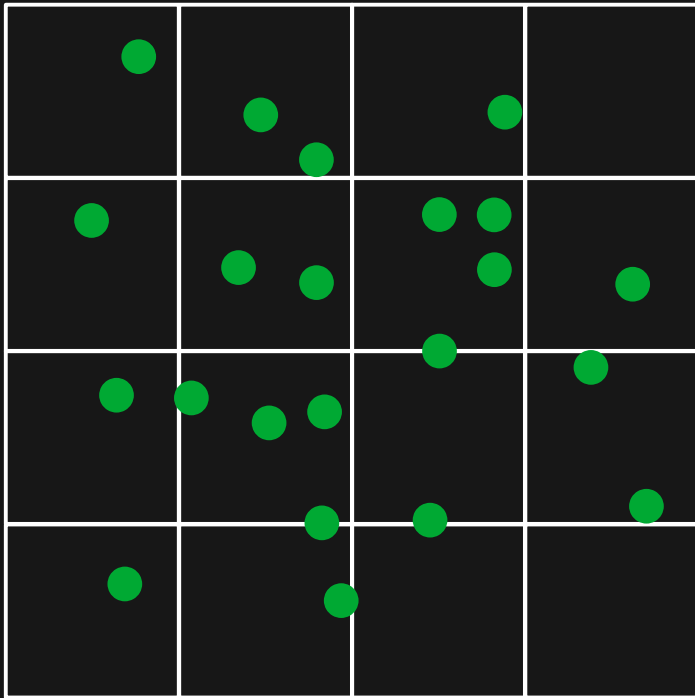
Gravitational potential



(+) fast, smoothly differentiable

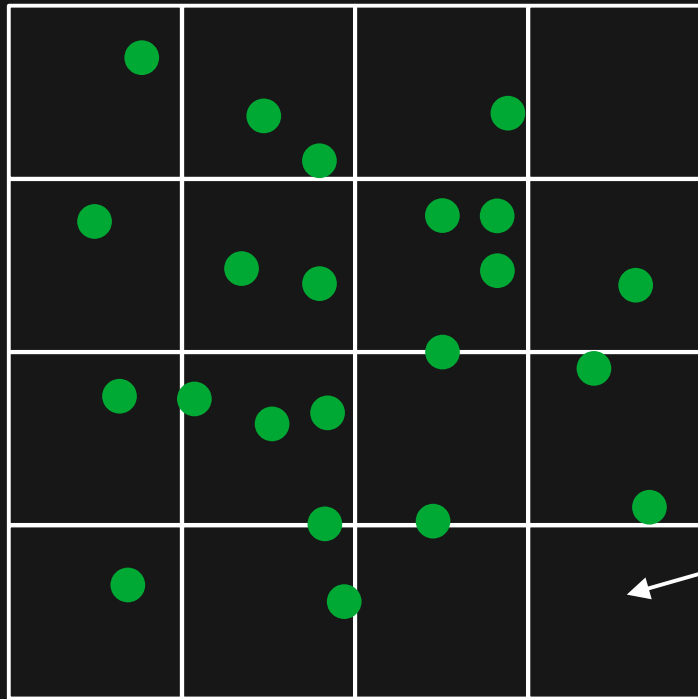
(-) inaccurate below cell size

# Computing the velocity field



$\rho = n$  particles in cell

# Computing the velocity field

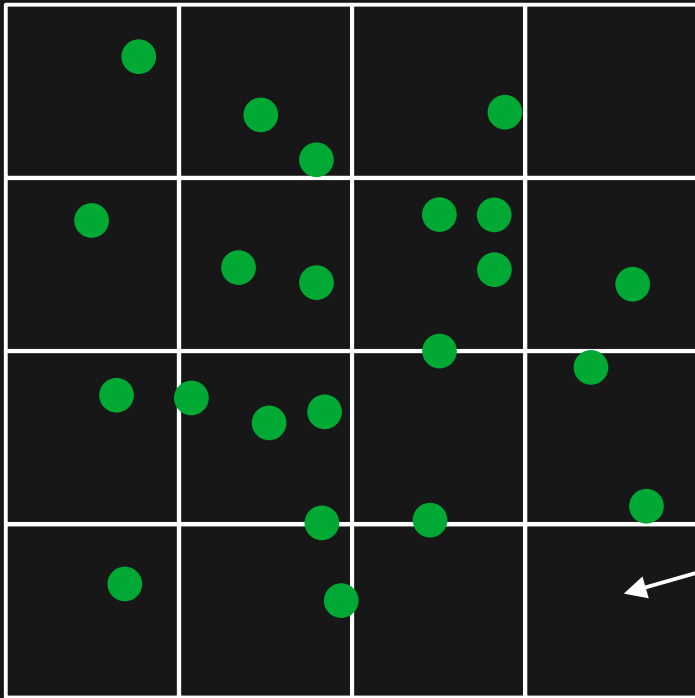


$\rho = n$  particles in cell

$\rho < 1$  particle / cell



# Computing the velocity field

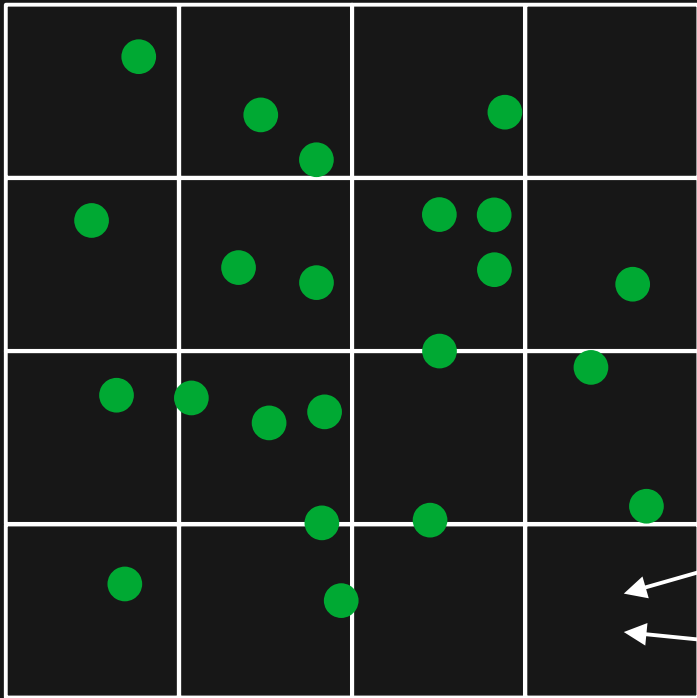


$$\rho = n \text{ particles in cell}$$

$$\vec{v} = \frac{\text{sum velocities in cell}}{n \text{ particles in cell}}$$

$$\rho < 1 \text{ particle / cell}$$

# Computing the velocity field



$\rho = n$  particles in cell

$$\vec{v} = \frac{\text{sum velocities in cell}}{\text{n particles in cell}}$$

$\rho < 1$  particle / cell

$$\vec{v} = \frac{0}{0} = \text{ill defined}$$

**+ non-differentiable!** 17 / 37



# Empty cells

Cells with less than

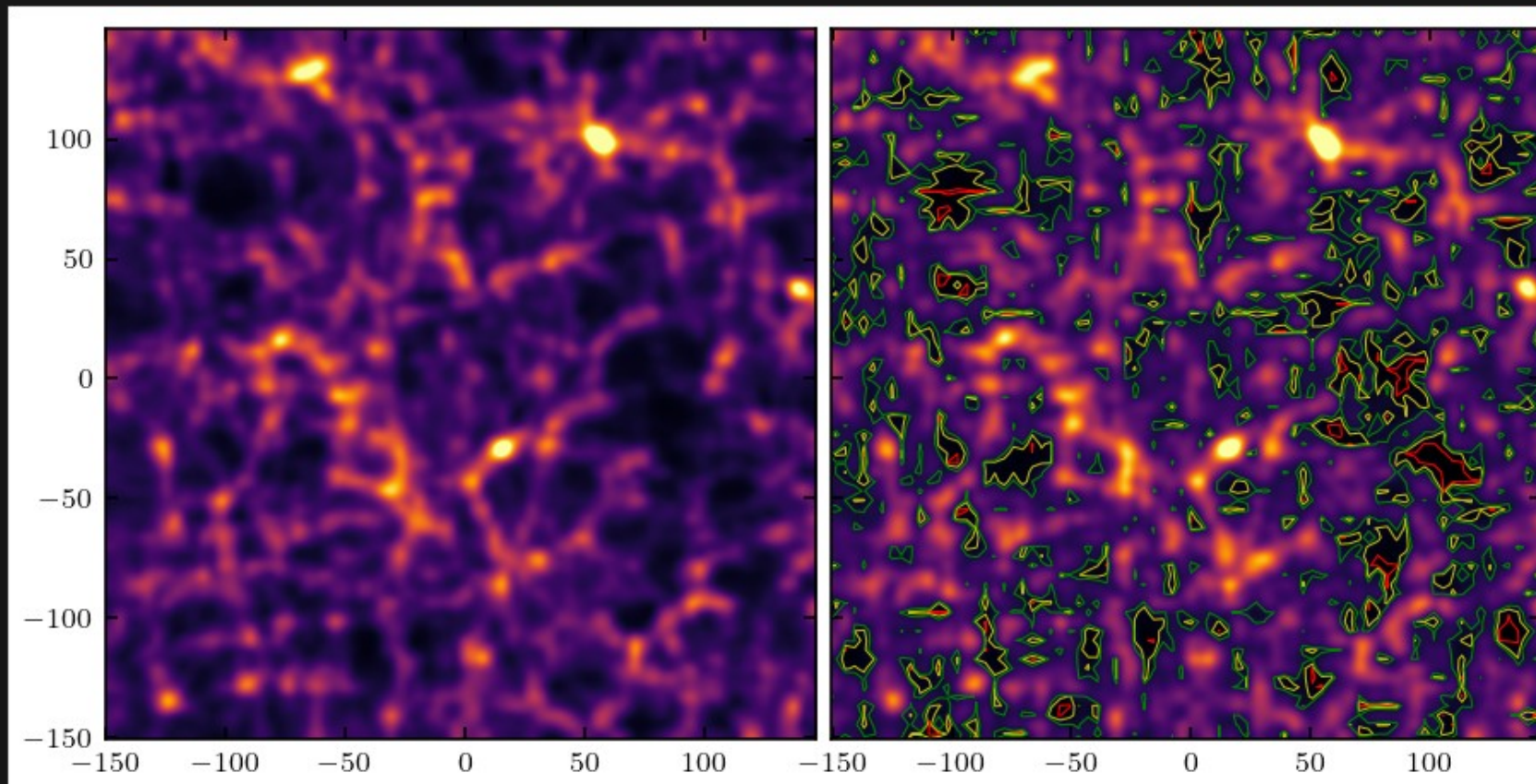
2 particles

1 particle

0.1 particle

$256^3$  particles,  $128^3$  cells

$128^3$  particles,  $128^3$  cells

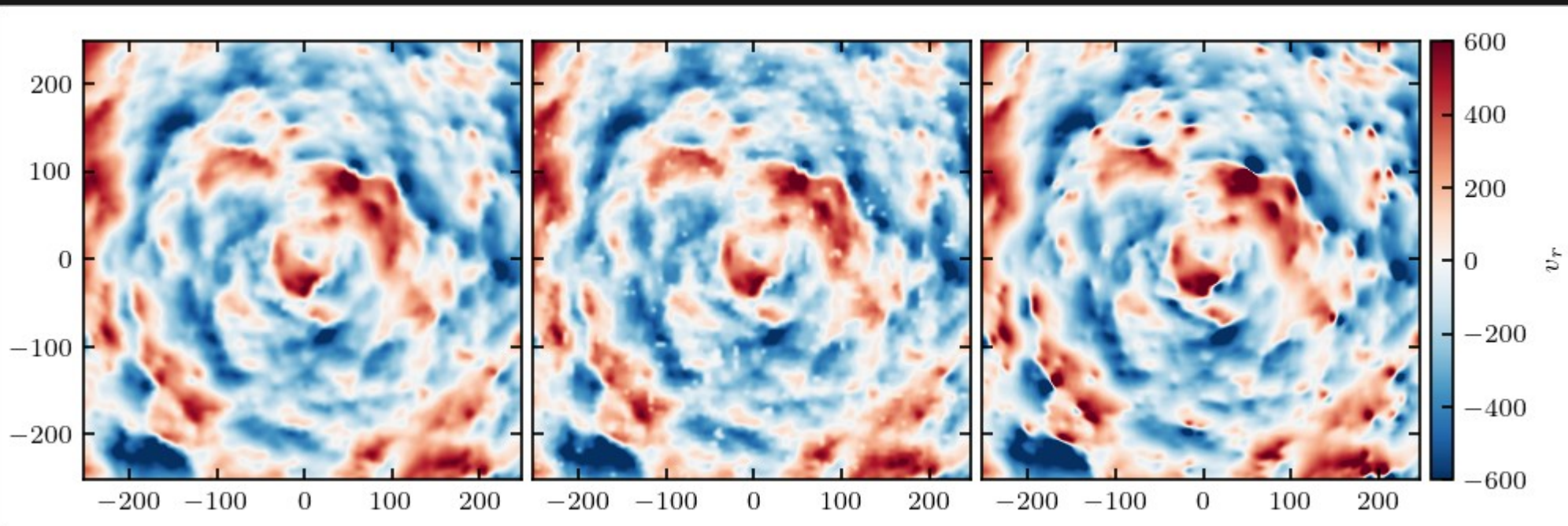


Use linear theory  $\cdot \vec{v}(\vec{r}) = -H_0 f \delta(\vec{r})$

High-res (reference)

Low-res

Low-res with  $v(\delta) \leftarrow$  linear theory

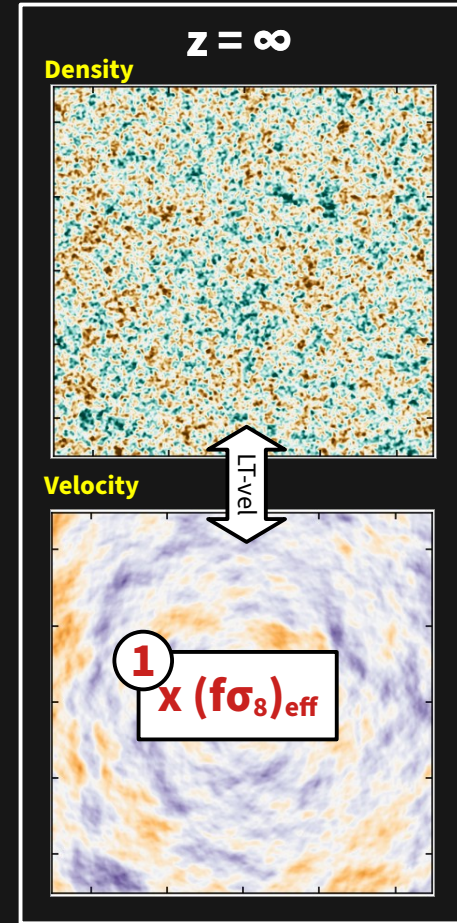




What about  $f\sigma_8$ ?

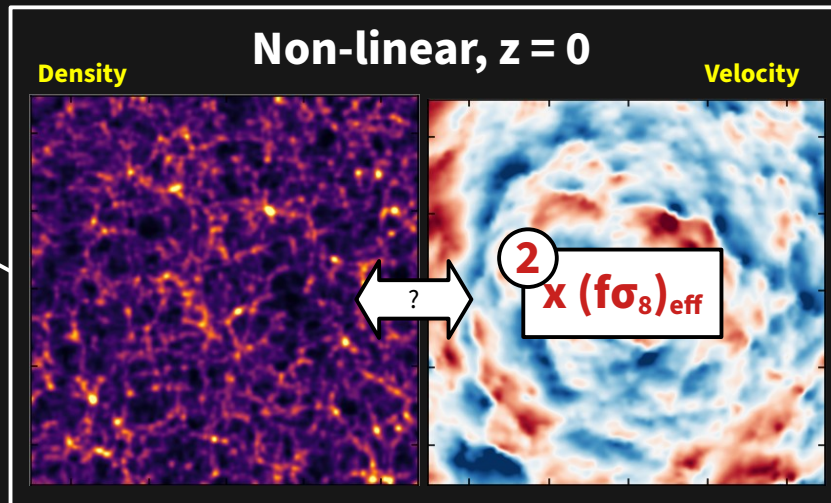
Velocity data

$z = 0$

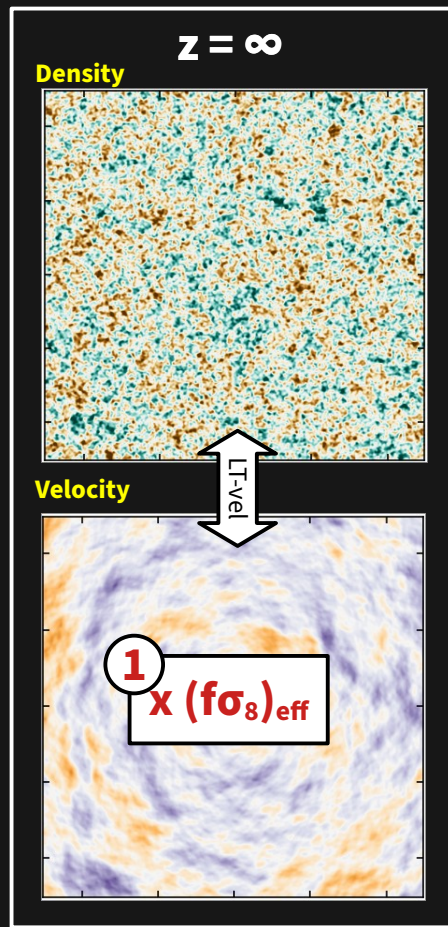


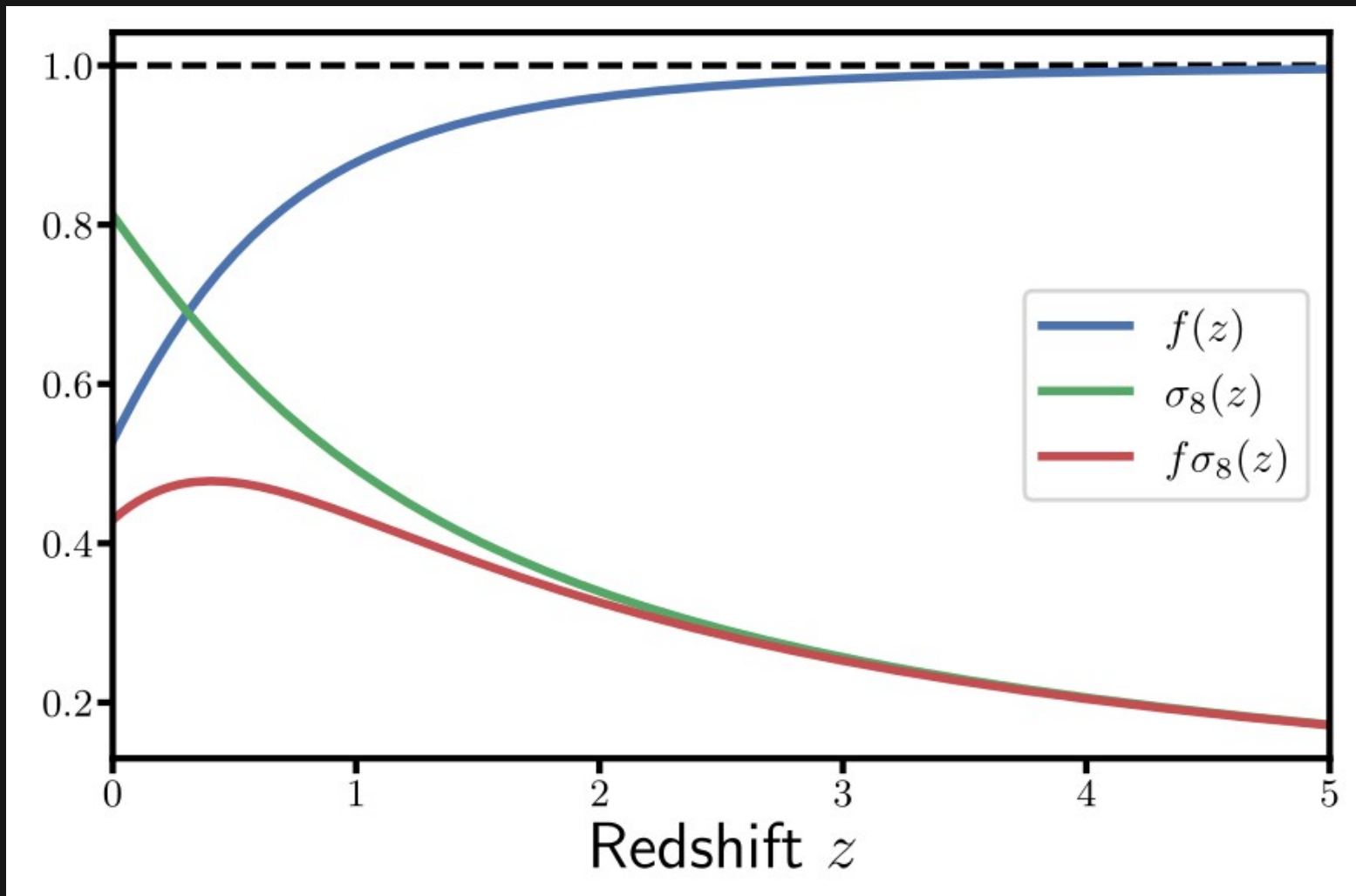


Velocity data  
 $z = 0$

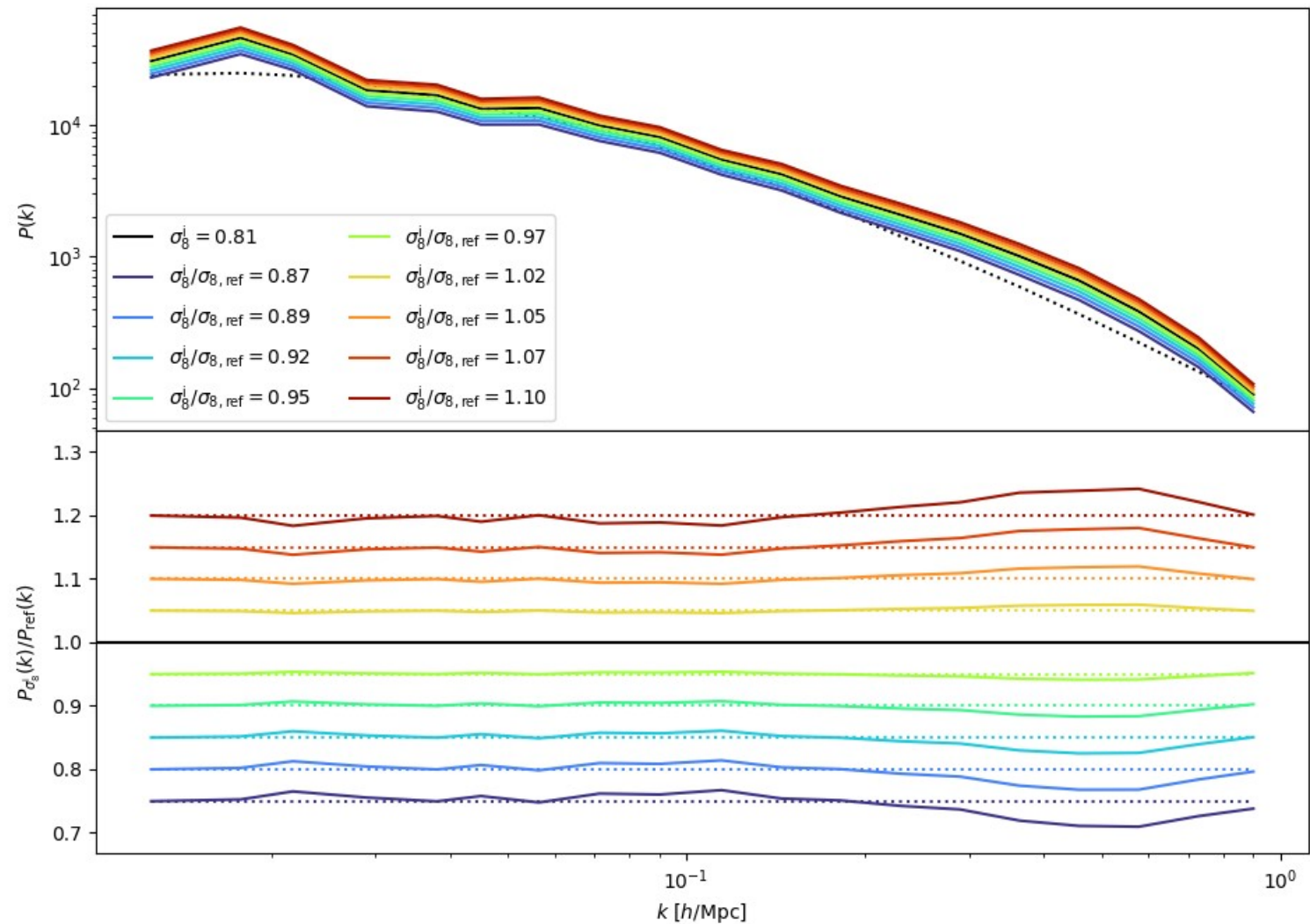


N-body  
LPT





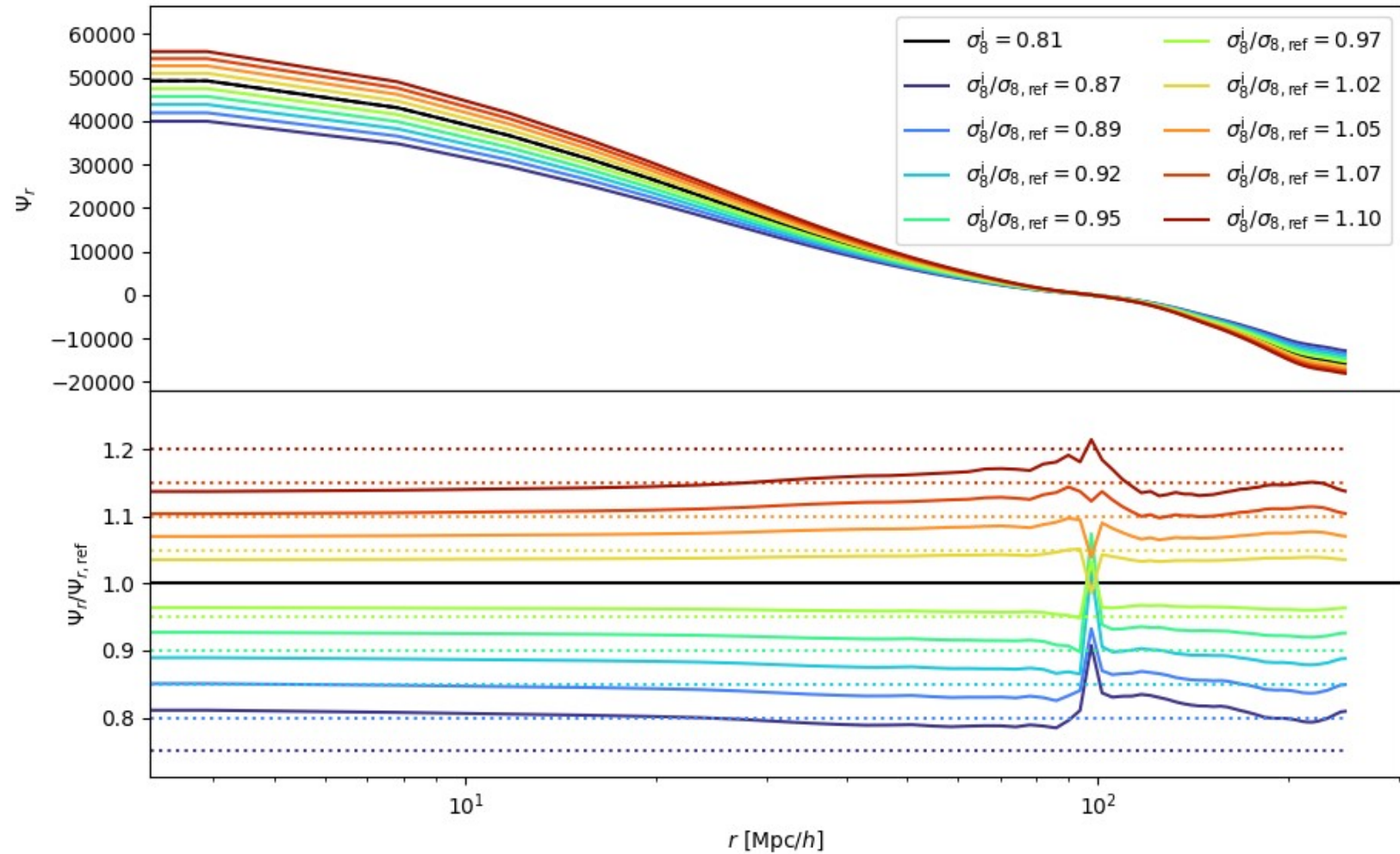
**Still linear theory!**



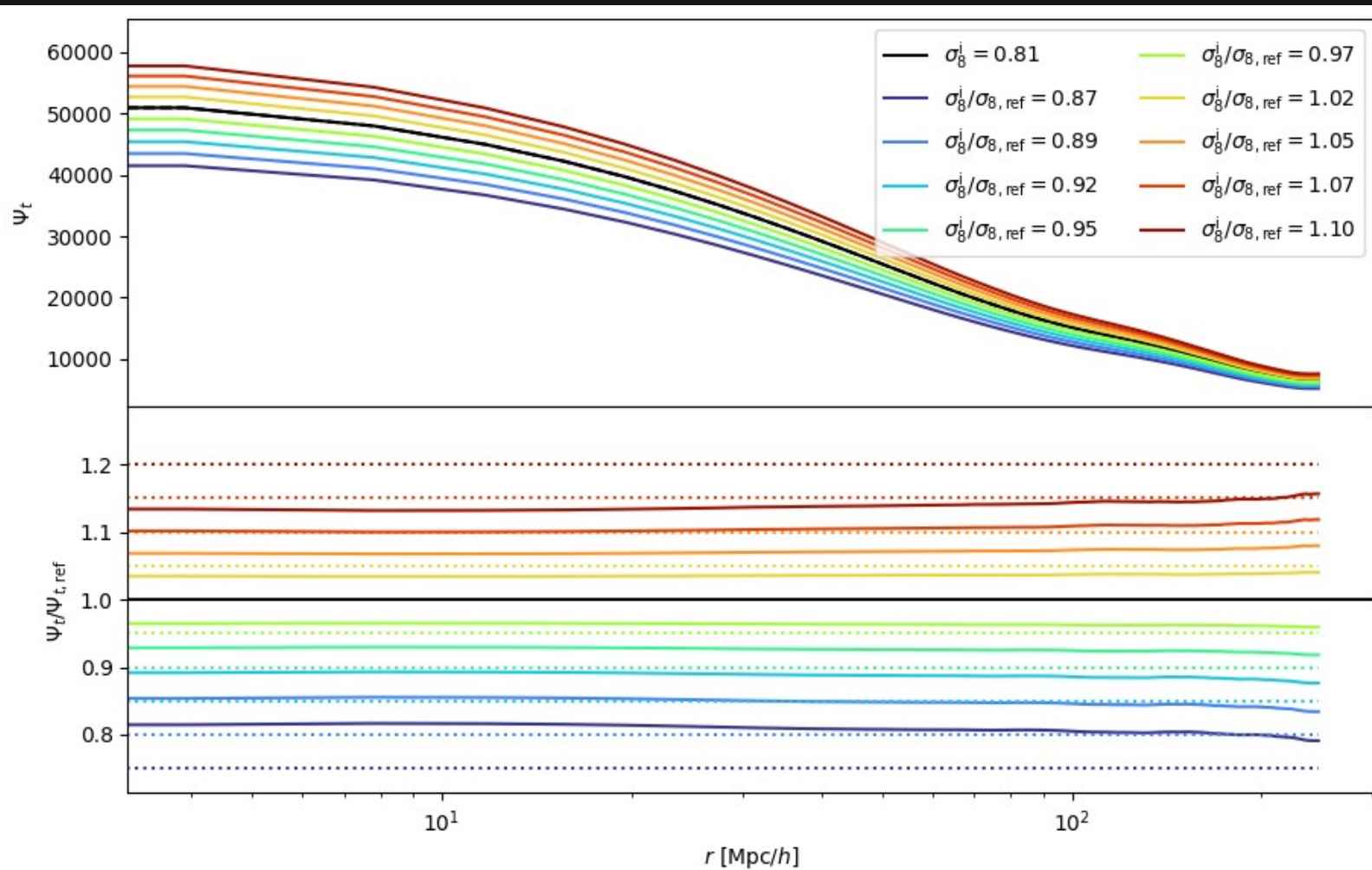
**Full lines** → case (1)  
**Dotted lines** → case (2)



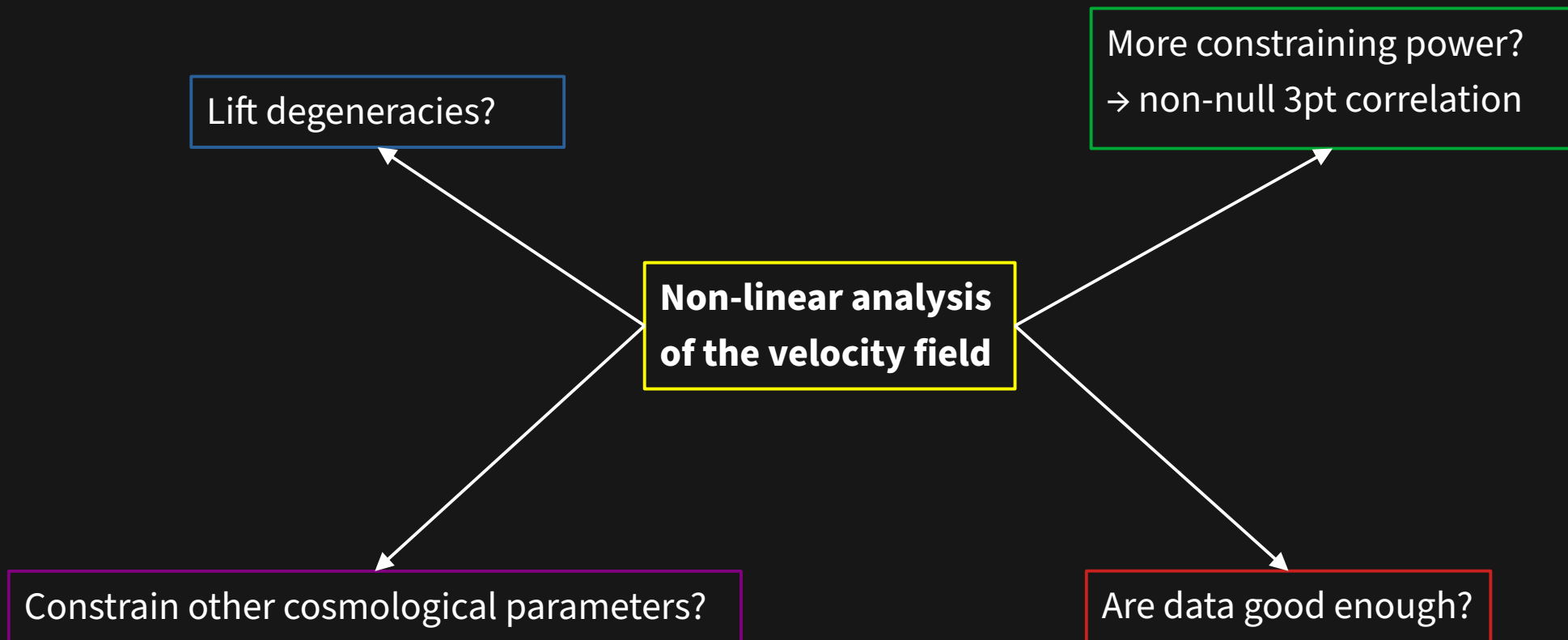
# Velocity correlation function (radial)



# Velocity correlation function (transversal)



# Open questions



# Skysurvey + pmwd = mocks from evolved random universes

1 → initialize (once)

```
EU = EvolvedUniverse(  
    pmwd_cosmo_kwargs={},  
    pmwd_conf_kwargs=dict(  
        ptcl_grid_shape=(n_ptcl_per_side,) * 3,  
        ptcl_spacing=L_box / n_ptcl_per_side,  
        mesh_shape=mesh_shape,  
        a_start=1 if just_2lpt else 1 / 64,  
    ),  
)
```

# Skysurvey + pmwd = mocks from evolved random universes

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)
```

2 → run (on GPU)

```
ptcl = EU.run_PM(seed=0)
```

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    ),  
)
```

2 → run (on GPU)

```
ptcl = EU.run_PM(seed=0)
```

3 → build halos (slow...)

```
halos_xyz, halos_v_xyz, halos_mass = EU.build_halos(  
    ptcl_xyz,  
    ptcl_v_xyz,  
    linking_length=halos_linking_length,  
)
```

# Skysurvey + pmwd = mocks from evolved random universes

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    ptcl_xyz,  
    ptcl_v_xyz,  
    linking_length=halos_linking_length,  
)
```

## 4 → observe

```
ra, dec, z_cos, v_r = EU.observe(  
    halos_xyz,  
    halos_v_xyz,  
    obs_xyz=obs_xyz,  
    obs_v_xyz=obs_v_xyz,  
    box_coords="celestial",  
)
```

# Skysurvey + pmwd = mocks from evolved random universes

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        ptcl_spacing=L_box / n_ptcl_per_side,  
        mesh_shape=mesh_shape,  
        a_start=1 if just_2lpt else 1 / 64,  
    ),  
)
```

## 2 → run (on GPU)

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ptcl = EU.run_PM(seed=0)
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## 3 → build halos (slow...)

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halos_xyz, halos_v_xyz, halos_mass = EU.build_halos(  
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## 4 → observe

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    obs_xyz=obs_xyz,  
    obs_v_xyz=obs_v_xyz,  
    box_coords="celestial",  
)
```

## 5 → quick overview

```
rho, v_xyz = EU.build_CiCs(ptcl, cic_log2_refine)  
fig_rho, fig_v_r, fig_ps = EU.analyze_CiCs(rho, v_xyz)  
fig_obs = EU.analyze_obs(ra, dec, z_cos, v_r)
```



# Halos or particles?

